Package 'ACDm'

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Description Provides tools for autoregressive conditional duration (ACD, Engle and Russell, 1998) models. Functions to create trade, price, or volume durations from transaction data, perform diurnal adjustments, fit various ACD models, and test them.
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Description

ACDm-package

Package for Autoregressive Conditional Duration (ACD, Engle and Russell, 1998) models. Creates trade, price or volume durations from transactions (tic) data, performs diurnal adjustments, fits various ACD models and tests them.

Credit

The author would like to thank the department of statistics at Hanken School of Economics, as the bulk of this work was done there while working as a research assistant.

Author(s)

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ACD Modelling

References

Engle R.F, Russell J.R. (1998) *Autoregressive Conditional Duration: A New Model for Irregularly Spaced Transaction Data*, Econometrica, 66(5): 1127-1162.

acdFit	ACD (Autoregressive Conditional Duration) Model Fitting

Description

This function estimates various ACD models with various assumed error term distributions, using Maximum Likelihood Estimation.

The currently available models (conditional mean specifications) are: Standard ACD, Log-ACD (two alternative specifications), AMACD, ABACD, BACD, BCACD, AACD, EXACD, SNIACD, LSNIACD, TACD, and TAMACD.

The currently available distributions are: Exponential (also used for QML), Weibull, Burr, generalized Gamma, generalized F, Q-Weibull, and Mixture inverse Gaussian.

Usage

```
acdFit(durations = NULL, model = "ACD", dist = "exponential",
    order = NULL, startPara = NULL, dailyRestart = FALSE, optimFnc = "optim",
    method = "Nelder-Mead", output = TRUE, bootstrapErrors = FALSE,
    forceErrExpec = TRUE, fixedParamPos = NULL, bp = NULL,
    exogenousVariables = NULL, optimFncArgs = list(),
    control = list())
```

Arguments

durations	either (1) a data frame including, at least, a column named 'durations' or 'adj- Dur' (for adjusted durations), or (2) a vector of durations
model	the conditional mean model specification. Must be one of "ACD", "LACD1", "LACD2", "AMACD", "BACD", "ABACD", "SNIACD" or "LSNIACD". See 'Details' for detailed model specification.
dist	the assumed error term distribution. Must be one of "exponential", "weibull", "burr", "gengamma", "genf", "qweibull", "mixqwe", "mixqww", or "mixinvgauss" See 'Details' for detailed model specification.
order	a vector detailing the order of the particular ACD model. For example an $ACD(p, q)$ specification should have order = $c(p, q)$.
startPara	a vector with parameter values to start the maximization algorithm from. Must be in the correct order according to the model specification (see Details).
dailyRestart	if TRUE the conditional duration will start fresh every new trading day. Can only be used if the durations arguments included the clock time of the durations, or if the time argument was provided.
optimFnc	Specifies which optimization function to use for the estimation. "optim", "nlminb", "solnp", and "optimx" are available.
method	Argument passed to the optimization function if optimFnc = "optim" or optimFnc = "optimx" were chosen. Specifies the optimization algorithm. See the help files for optim, nlminb or solnp.

output if FALSE the estimation results won't be printed.

bootstrapErrors

if TRUE the standard errors will be computed by using bootstrap simulations.

Currently only works with the standard ACD model.

forceErrExpec if TRUE the expectation of the error terms' distribution will be forced to be 1, oth-

erwise the distribution parameter specifying the mean will be set to 1 to ensure

identification.

fixedParamPos a logical vector of TRUE and FALSE. Can only be used if the argument startPara

was provided, and should be of the same length. Each element represents the respective start parameter and if TRUE, this parameter will be held fixed when

estimating the other parameters.

bp a numeric vector of breakpoints, used if the model is any of "SNIACD", "LSNIACD",

"TACD", "TAMACD". The default is a single breakpoint at 1.

exogenousVariables

specifies the columns in the durations data.frame that should be used as exogenous variables when fitting the model. Must be a vector, either with the column positions or the names of the columns. It is highly recommended to standardize the exogenous variables before running the estimation. The models use the

current exogenous variable and not their lagged values.

optimFncArgs a list of values passed to the optimaization function.

control a list of control values:

maxit maximum number of iterations performed by the numerical maximization algorithm.

trace An integer. If set to a non-zero value, the parameter values at each call of the log-likelihood function during optimization will be recorded, and the resulting search path of the maximum-likelihood estimate will be plotted. This argument is also passed on to the underlying optimizer; see the help files for optim, nlminb or solnp for details.

B number of bootstrap samples

Details

The startPara argument is a vector of the parameter values to start from. The length of the vector naturally depends on the model and distribution. The first elements represent the model parameters, and the last elements the distribution parameters. For example for an ACD(1,1) with Weibull errors the first 3 elements are $\omega, \alpha_1, \beta_1$ for the model, and the last is γ for the Weibull distribution.

The family of ACD models are

$$x_i = \mu_i \epsilon_i$$

where different specifications of the conditional mean duration μ_i and the error term ϵ_i give rise to different models as shown below.

When exogenous variables are used, they are added in the form of

$$\sum_{j=1}^{k} \xi_j z_j$$

to the right hand side of the equations, where z_i are the exogenous variables.

Conditional mean duration μ_i specifications according to the model argument:

ACD(p, q) specification: (Engle and Russell, 1998)

$$\mu_i = \omega + \sum_{j=1}^{p} \alpha_j x_{i-j} + \sum_{j=1}^{q} \beta_j \mu_{i-j}$$

The element order of the startPara vector is $(\omega, \alpha_j ..., \beta_j ...)$.

LACD1(p, q): (Bauwens and Giot, 2000)

$$\ln \mu_i = \omega + \sum_{j=1}^p \alpha_j \ln \epsilon_{i-j} + \sum_{j=1}^q \beta_j \ln \mu_{i-j}$$

The element order of the startPara vector is $(\omega, \alpha_j ..., \beta_j ...)$.

LACD2(p, q): (Lunde, 1999)

$$\ln \mu_i = \omega + \sum_{j=1}^p \alpha_j \epsilon_{i-j} + \sum_{j=1}^q \beta_j \ln \mu_{i-j}$$

The element order of the startPara vector is $(\omega, \alpha_j ..., \beta_j ...)$.

AMACD(p, r, q) (Additive and Multiplicative ACD): (Hautsch, 2012)

$$\mu_i = \omega + \sum_{j=1}^{p} \alpha_j x_{i-j} + \sum_{j=1}^{r} \nu_j \epsilon_{i-j} + \sum_{j=1}^{q} \beta_j \mu_{i-j}$$

The element order of the startPara vector is $(\omega, \alpha_j..., \nu_j..., \beta_j...)$.

ABACD(p, q) (Augmented Box-Cox ACD): (Hautsch, 2012)

$$\mu_i^{\delta_1} = \omega + \sum_{j=1}^p \alpha_j \left(|\epsilon_{i-j} - \nu| + c |\epsilon_{i-j} - \nu| \right)^{\delta_2} + \sum_{j=1}^q \beta_j \mu_{i-j}^{\delta_1}$$

The element order of the startPara vector is $(\omega, \alpha_j ..., \beta_j ..., c, \nu, \delta_1, \delta_2)$.

BACD(p, q) (Box-Cox ACD): (Hautsch, 2003)

$$\mu_i^{\delta_1} = \omega + \sum_{j=1}^p \alpha_j \epsilon_{i-j}^{\delta_2} + \sum_{j=1}^q \beta_j \mu_{i-j}^{\delta_1}$$

The element order of the startPara vector is $(\omega, \alpha_j ..., \beta_j ...)$.

EXACD(p, q) (Exponential ACD): (Dufour and Engle, 2000)

$$\ln \mu_i = \omega + \sum_{j=1}^p \left(\alpha_j \epsilon_{i-j} + \delta_j |\epsilon_{i-j} - 1| + \sum_{j=1}^q \beta_j \mu_{i-j} \right)$$

SNIACD(p, q, M) (Spline News Impact ACD): (Hautsch, 2012, with a slight difference)

$$\mu_i = \omega + \sum_{j=1}^p (\alpha_{j-1} + c_0)\epsilon_{i-j} + \sum_{j=1}^p \sum_{k=1}^M (\alpha_{j-1} + c_k) 1_{(\epsilon_{i-j} \le \bar{\epsilon_k})} + \sum_{j=1}^q \beta_j \mu_{i-j},$$

where $1_{()}$ is an indicator function and $\alpha_0 = 0$.

The element order of the startPara vector is $(\omega, c_k..., \alpha_j..., \beta_j...)$ (The number of α -parameters are p-1).

The distribution of the error term ϵ_i specifications according to the dist argument:

Exponential distribution, dist = "exponential":

$$f(\epsilon) = \exp(-\epsilon)$$

Weibull distribution, dist = "weibull":

$$f(\epsilon) = \theta \gamma \epsilon^{\gamma - 1} e^{-\theta \epsilon^{\gamma}},$$

where $\theta = [\Gamma(\gamma^{-1} + 1)]^{\gamma}$ if forceErrExpec = TRUE.

Note that this is a diffrent parameterization then the one in stats::dweibull. While the shape parameter in stats::dweibull is the same as γ , the scale parameter is equal to $\theta^{-\gamma}$.

Burr distribution, dist = "burr":

$$f(\epsilon) = \frac{\theta \kappa \epsilon^{\kappa - 1}}{(1 + \sigma^2 \theta \epsilon^{\kappa})^{\frac{1}{\sigma^2} + 1}},$$

where,

$$\theta = \sigma^{2\left(1+\frac{1}{\kappa}\right)} \frac{\Gamma\left(\frac{1}{\sigma^2} + 1\right)}{\Gamma\left(\frac{1}{\kappa} + 1\right)\Gamma\left(\frac{1}{\sigma^2} - \frac{1}{\kappa}\right)},$$

if forceErrExpec = TRUE.

The element order of the startPara vector is $(model parameters, \kappa, \sigma^2)$.

Generalized Gamma distribution, dist = "gengamma":

$$f(\epsilon) = \frac{\gamma \epsilon^{\kappa \gamma - 1}}{\lambda^{\kappa \gamma} \Gamma(\kappa)} \exp\left\{-\left(\frac{\epsilon}{\lambda}\right)^{\gamma}\right\}$$

where $\lambda = \frac{\Gamma(\kappa)}{\Gamma(\kappa + \frac{1}{\gamma})}$ if forceErrExpec = TRUE. The element order of the startPara vector is $(modelparameters, \kappa, \gamma)$.

Generalized F distribution, dist = "genf":

$$f(\epsilon) = \frac{\gamma \epsilon^{\kappa \gamma - 1} [\eta + (\epsilon/\lambda)^{\gamma}]^{-\eta - \kappa} \eta^{\eta}}{\lambda^{\kappa \gamma} B(\kappa, \eta)},$$

where $B(\kappa,\eta)=\frac{\Gamma(\kappa)\Gamma(\eta)}{\Gamma(\kappa+\eta)},$ and if forceErrExpec = TRUE,

$$\lambda = \frac{\Gamma(\kappa)\Gamma(\eta)}{\eta^{1/\gamma}\Gamma(\kappa + 1/\gamma)\Gamma(\eta - 1/\gamma)}.$$

The element order of the startPara vector is $(model parameters, \kappa, \eta, \gamma)$.

q-Weibull distribution, dist = "qweibull":

$$f(\epsilon) = (2 - q) \frac{a}{b^a} \epsilon^{a-1} \left[1 - (1 - q) \left(\frac{\epsilon}{b} \right)^a \right]^{\frac{1}{1 - q}}$$

where if forceErrExpec = TRUE,

$$b = \frac{(q-1)^{\frac{1+a}{a}}}{2-q} \frac{a\Gamma(\frac{1}{q-1})}{\Gamma(\frac{1}{a})\Gamma(\frac{1}{q-1} - \frac{1}{a} - 1)}.$$

The element order of the startPara vector is (model parameters, a, q).

Value

a list of class "acdFit" with the following slots:

durations the durations object used to fit the model.

muHats a vector of the estimated conditional mean durations

residuals the residuals from the fitted model, calculated as durations/mu

model the model for the conditional mean durations

order the order of the model

distribution the assumed error term distribution

distCode the internal code used to represent the distribution

mPara a vector of the estimated conditional mean duration parameters

dPara a vector of the estimated error distribution parameters

Npar total number of parameters

goodnessOfFit a data.frame with the log likelihood, AIC, BIC, and MSE calculated as the mean

squared deviation of the durations and the estimated conditional durations.

parameterInference

a data.frame with the estimated coefficients and their standard errors and p-

values

forcedDistPara the value of the unfree distribution parameter. If forceErrExpec = TRUE were

used, this parameter is a function of the other distribution parameters, to force the mean of the distribution to be one. Otherwise the parameter was fixed at 1

to ensure identification.

comments

hessian the numerical hessian of the log likelihood evaluated at the estimate

N number of observations

evals number of log-likelihood evaluations needed for the maximization algorithm

convergence if the maximization algorithm converged, this value is zero. (see the help file

optim, nlminb or solnp)

estimationTime time required for estimation description who fitted the model and when

robustCorr only available for QML estimation (choosing the exponential distribution) for

the standard ACD(p, q) model. The robust correlation matrix of the parameter

estimates.

Author(s)

Markus Belfrage

References

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Dufour, A., & Engle, R. F. (2000) *The ACD Model: Predictability of the Time Between Consecutive Trades* (Discussion Papers in Finance: 2000-05). ISMA Centre, University of Reading.

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Lunde, A. (1999): A generalized gamma autoregressive conditional duration model, Working paper, Alborg University.

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acdFit-methods

Methods for class acdFit

Description

residuals.acdFit() returns the residuals and coef.acdFit() returns the coefficients of a fitted ACD model of class 'acdFit', while print.acdFit() prints the essential information. predict.acdFit() predicts the next N durations by thier expected value.

Usage

```
## S3 method for class 'acdFit'
residuals(object, ...)
## S3 method for class 'acdFit'
coef(object, returnCoef = "all", ...)
## S3 method for class 'acdFit'
print(x, ...)
## S3 method for class 'acdFit'
predict(object, N = 10, ...)
```

Arguments

object the fitted ACD model of class 'acdFit' (as returned by the function acdFit).

x same as object, ie. an object of class 'acdFit'.

returnCoef on of "all", "distribution", or "model". Specifies whether all estimated parameters should be returned or only the distribution parameters or the model (for the conditional mean duration) parameters.

N the number of the predictions in predict.

additional arguments to print.

acf_acd

Autocorrelation function plots for ACD models

Description

plots the ACF (Auto Correlation Function) for the durations, diurnally adjusted durations, and residuals

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Arguments

a fitted model of class "acdFit", or a data.frame containing at least one the columns "durations", "adjDur", or "residuals". Can also be a vector of durations or residuals.

conf_level the confidence level of the confidence bands

max the largest lag to plot

max the largest lag to plot
min the smallest lag to plot
plotDur, plotAdjDur, plotResi

logical falgs. If FALSE, the respective ACF wont be plotted.

Value

returns a data.frame with the values of the sample autocorrelations for each lag and variable.

Author(s)

Markus Belfrage

Examples

```
data(adjDurData)
fitModel <- acdFit(adjDurData)
acf_acd(fitModel, conf_level = 0.95, max = 50, min = 1)
data(durData)
f <- acf_acd(durData)
f</pre>
```

BurrDist

The Burr Distribution

Description

Density, distribution function, quantile function, random generation and calculation of the expected value for the Burr distribution with parameters theta, kappa and sig2.

```
dburr(x, theta = 1, kappa = 1.2, sig2 = 0.3, forceExpectation = F)
pburr(x, theta = 1, kappa = 1.2, sig2 = .3, forceExpectation = F)
qburr(p, theta = 1, kappa = 1.2, sig2 = .3, forceExpectation = F)
rburr(n = 1, theta = 1, kappa = 1.2, sig2 = .3, forceExpectation = F)
burrExpectation(theta = 1, kappa = 1.2, sig2 = .3)
```

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Arguments

x vector of quantiles.

p vector of probabilities.

n number of observations...

theta, kappa, sig2

parameters, see 'Details'.

forceExpectation

logical; if TRUE, the expectation of the distribution is forced to be 1 by letting theta be a function of the other parameters.

Details

The PDF for the Burr distribution is (as in e.g. Grammig and Maurer, 2000):

$$f(x) = \frac{\theta \kappa x^{\kappa - 1}}{\left(1 + \sigma^2 x^{\kappa}\right)^{\frac{1}{\sigma^2} + 1}}$$

Value

dburr gives the density (PDF), qburr the quantile function (inverted CDF), rburr generates random deviates, and burrExpectation returns the expected value of the distribution, given the parameters.

Author(s)

Markus Belfrage

References

Grammig, J., and Maurer, K.-O. (2000) *Non-monotonic hazard functions and the autoregressive conditional duration model*. Econometrics Journal 3: 16-38.

computeDurations

Durations computation

Description

Computes durations from a data.frame containing the time stamps of transactions. Trade durations, price durations and volume durations can be computed (if the appropriate data columns are given).

```
computeDurations(transactions, open = "10:00:00", close = "18:25:00",
rm0dur = TRUE, type = "trade", priceDiff = .1, cumVol = 10000)
```

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Arguments

transactions a data.frame with, at least, transaction time in a column named 'time' (see De-

tails)

open the opening time of the exchange. Transactions done outside the trading hours

will be ignored.

close the closing time of the exchange.

rm0dur if TRUE zero-durations will be removed and transactions done on the same sec-

ond will be aggregated, e.g. price will then be the volume weighted avrage price

of the aggregated transactions.

type the type of durations to be computed. Either "trade", "price", or "volume".

priceDiff only if type = "price". Price durtions are (here) defind as the duration until the

price has changed by at least 'priceDiff' in absolute value.

cumVol only if type = "cumVol". Volume durtions are (here) defind as the duration until

the cumulative traded volume since the last duration has surpassed 'cumVol'.

Details

The data.frame must include a column named 'time' with the time of each transaction, in a time format recognizable by POSIXIt or strings in format "yyyy-mm-dd hh:mm:ss". If the column 'price' or 'volume' is included its also possible to compute price- and volume durations (see arguments priceDiff and cumVol)

Value

a data.frame with columns:

time the calander time of the start of each duration spell.

price the volume weighted avrage price of the shares traded during the spell of the

duration.

volume the volume (total shares traded) during the duration spell.

Ntrans number of transactions done during the spell.

durations the computed durations.

Author(s)

Markus Belfrage

```
## Not run:
#only the first 3 days of data:
data(transData)
durDataShort <- computeDurations(transData[1:56700, ])
head(durDataShort)
## End(Not run)</pre>
```

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DataFiles

Time Series Data Sets

Description

The data file transData is the base data used in all of the examples. It is a data.frame with rows representing a single transaction and has the columns 'time', 'price', giving the trade price, and 'volume', giving the number of shares traded for the transaction. The data set is based on real transactions but has been obfuscated by transforming the dates, price and volume, for proprietary reasons. It covers two weeks of nearly 100 000 transactions, recorded with 1 second precision.

The durData data.frame is simply the trade durations formed from transData using the function durData <- computeDurations(transData)

The adjDurData data object is in turn created by adjDurData <- diurnalAdj(durData, aggregation = "all") to add diurnally adjusted durations.

defaultSplineObj is an estimated cubic spline of the diurnal component using the sample data. It is used when simulating from sim_ACD() with the argument diurnalFactor set to TRUE, when no user splineObj is provided.

dgenf

The generalized F distribution

Description

Density and distribution function for the generalized F distribution. Warning: the distribution function pgenf and genfHazard are computed numerically, and may not be precise!

Usage

```
dgenf(x, kappa = 5, eta = 1.5, gamma = .8, lambda = 1, forceExpectation = F) pgenf(q, kappa = 5, eta = 1.5, gamma = .8, lambda = 1, forceExpectation = F) genfHazard(x, kappa = 5, eta = 1.5, gamma = .8, lambda = 1, forceExpectation = F)
```

Arguments

```
x, q vector of quantiles.
kappa, eta, gamma, lambda
parameters, see 'Details'.
forceExpectation
```

logical; if TRUE, the expectation of the distribution is forced to be 1 by letting theta be a function of the other parameters.

Details

The PDF for the generelized F distribution is:

$$f(\epsilon) = \frac{\gamma \epsilon^{\kappa \gamma - 1} [\eta + (\epsilon/\lambda)^{\gamma}]^{-\eta - \kappa} \eta^{\eta}}{\lambda^{\kappa \gamma} B(\kappa, \eta)},$$

where $B(\kappa, \eta) = \frac{\Gamma(\kappa)\Gamma(\eta)}{\Gamma(\kappa+\eta)}$ is the beta function.

Discreetly mixed Q-Weibull and exponential

Discreet mix of the Q-Weibull and the exponential distributions

Description

Density (PDF), distribution function (CDF), and hazard function for a discreetly mixed distribution of the Q-Weibull and the exponential distributions.

Usage

```
dmixqwe(x, pdist = .5, a = .8, qdist = 1.5, lambda = .8, b = 1, forceExpectation = F)

pmixqwe(q, pdist = .5, a = .8, qdist = 1.5, lambda = .8, b = 1, forceExpectation = F)

mixqweHazard(x, pdist = .5, a = .8, qdist = 1.5, lambda = .8, b = 1, forceExpectation = F)
```

Arguments

x, q vector of quantiles. pdist, a, qdist, lambda, b parameters, see 'Details'.

forceExpectation

logical; if TRUE, the expectation of the distribution is forced to be 1 by letting b be a function of the other parameters.

Details

The PDF for the mixed distribution is:

$$f(x) = p(2-q)\frac{a}{b^a}x^{a-1}\left[1-(1-q)\left(\frac{x}{b}\right)^a\right]^{\frac{1}{1-q}} + (1-p)\frac{1}{\lambda}exp(-\frac{x}{\lambda})$$

if forceExpectation = TRUE the b parameter is a function of the other parameters to force the expectation to be 1.

See Also

qWeibullDist for the Q-Weibull distribution and pmixqww for Q-Weibull mixed with the ordinary Weibull.

Discreetly mixed Q-Weibull and ordinary Weibull

Discreet mix of the q-Weibull and the ordinary Weibull distributions

Description

Density (PDF), distribution function (CDF), and hazard function for a discreetly mixed distribution of the Q-Weibull and the ordinary Weibull distributions.

Usage

```
dmixqww(x, pdist = .5, a = 1.2, qdist = 1.5, theta = .8, gamma = 1, b = 1,
  forceExpectation = F)

pmixqww(q, pdist = .5, a = 1.2, qdist = 1.5, theta = .8, gamma = 1, b = 1,
  forceExpectation = F)

mixqwwHazard(x, pdist = .5, a = 1.2, qdist = 1.5, theta = .8, gamma = 1, b = 1,
  forceExpectation = F)
```

Arguments

x, q vector of quantiles.
pdist, a, qdist, theta, gamma, b
parameters, see 'Details'.

forceExpectation

logical; if TRUE, the expectation of the distribution is forced to be 1 by letting b be a function of the other parameters.

Details

The PDF for the mixed distribution is:

$$f(x) = p(2-q)\frac{a}{b^a}x^{a-1} \left[1 - (1-q)\left(\frac{x}{b}\right)^a \right]^{\frac{1}{1-q}} + (1-p)\theta \gamma x^{-\theta x^{\gamma}}$$

if forceExpectation = TRUE the b parameter is a function of the other parameters to force the expectation to be 1.

See Also

qWeibullDist for the Q-Weibull distribution and pmixqwe for Q-Weibull mixed with the exponential distribution.

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Dirunal adjustment for durations

Description

Performs a diurnal adjustment of the durations, i.e. removes a daily seasonal component. Four different methods of diurnal adjustment are available, namely "cubicSpline", "supsmu" (Friedman's SuperSmoother), "smoothSpline" (smoothed version of the cubic spline), or "FFF" (Flexible Fourier Form).

Usage

```
diurnalAdj(dur, method = "cubicSpline", nodes = c(seq(600, 1105, 60), 1105),
aggregation = "all", span = "cv", spar = 0, Q = 4, returnSplineFnc = FALSE)
```

Arguments

dur a data.frame containing the columns durations, containing durations, and time,

containing the time stamps.

method the method used. One of "cubicSpline", "supsmu", "smoothSpline", or "FFF".

nodes only for method = "cubicSpline" or method = "smoothSpline". A vector of

nodes to use for the spline function, in the unit minutes after midnight. The first and last element of the vector must be the start and end of the trading day. The nodes given are actually the limits of intervalls, of wich the midpoints will be

set as the nodes using the means of the intervals.

aggregation what type of aggregation to use. Either "weekdays", "all", or "none". If for

example "weekdays" is chosen, all Mondays will have the same daily seasonal

component, and so on.

span argument passed to supsmu if method = "supsmu" were chosen. Affects the

smoothness of the curve, see supsmu.

spar argument passed to smooth.spline if method = "smooth.spline" were chosen.

Affects the smoothness of the curve, see smooth.spline.

Q number of trigonometric function pairs for method = "FFF".

returnSplineFnc

if TRUE instead or returning the adjusted durations a list of spline objects will be returned, containing the coefficients of the spline function. Only available for

method = "cubicSpline".

Value

```
if returnSplineFnc = FALSE (default)
```

the input data.frame 'dur' with an added column of the diurnally adjusted durations called 'adjDur'.

if returnSplineFnc = TRUE

a list of spline objects containing the coefficients of the spline function.

Author(s)

Markus Belfrage

Examples

```
data(durData)
diurnalAdj(durData, aggregation = "none", method = "supsmu")

## Not run:
head(durData)
f <- diurnalAdj(durData, aggregation = "weekdays", method = "FFF", Q = 3)
head(f)

f <- diurnalAdj(durData, aggregation = "all", returnSplineFnc = TRUE)
f

## End(Not run)</pre>
```

Finite mixture of inverse Gaussian Distributions

Finite mixture of inverse Gaussian Distribution

Description

Density (PDF), distribution function (CDF), and hazard function for Finite mixture of inverse Gaussian Distributions.

Usage

```
dmixinvgauss(x, theta = .2, lambda = .1, gamma = .05, forceExpectation = F)
pmixinvgauss(q, theta = .2, lambda = .1, gamma = .05, forceExpectation = F)
mixinvgaussHazard(x, theta = .2, lambda = .1, gamma = .05, forceExpectation = F)
```

Arguments

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Details

The finite mixture of inverse Gaussian distributions was used by Gomes-Deniz and Perez-Rodrigues (2013) for ACD-models. Its PDF is:

$$f(x) = \frac{\gamma + x}{\gamma + \theta} \sqrt{\frac{\lambda}{2\pi x^3}} \exp\left[-\frac{\lambda(x - \theta)^2}{2x\theta^2}\right].$$

If forceExpectation = TRUE the distribution is transformed by dividing the random variable with its expectation and using the change of variable function.

References

Gomez-Deniz, E. and Perez-Rodriguez, J.V. (2016) *Mixture Inverse Gaussian for Unobserved Heterogeneity in the Autoregressive Conditional Duration Model*. Communications in Statistics - Theory and Methods, http://dx.doi.org/10.1080/03610926.2016.1200094

GeneralizedGammaDist The generalized Gamma distribution

Description

Density (PDF), distribution function (CDF), quantile function (inverted CDF), random generation and hazard function for the generelized Gamma distribution with parameters gamma, kappa and lambda.

Usage

```
dgengamma(x, gamma = 0.3, kappa = 1.2, lambda = 0.3, forceExpectation = F)
pgengamma(x, gamma = .3, kappa = 3, lambda = .3, forceExpectation = F)
qgengamma(p, gamma = .3, kappa = 3, lambda = .3, forceExpectation = F)
rgengamma(n = 1, gamma = .3, kappa = 3, lambda = .3, forceExpectation = F)
gengammaHazard(x, gamma = .3, kappa = 3, lambda = .3, forceExpectation = F)
```

Arguments

x vector of quantiles.

p vector of probabilities.

n number of observations..

gamma, kappa, lambda

parameters, see 'Details'.

forceExpectation

logical; if TRUE, the expectation of the distribution is forced to be 1 by letting theta be a function of the other parameters.

plotDescTrans 19

Details

The PDF for the generelized Gamma distribution is:

$$f(x) = \frac{\gamma x^{\kappa \gamma - 1}}{\lambda^{\kappa \gamma} \Gamma(\kappa)} \exp\left\{-\left(\frac{x}{\lambda}\right)^{\gamma}\right\}$$

Value

dgengamma gives the density (PDF), pgengamma gives the distribution function (CDF), qgengamma gives the quantile function (inverted CDF), rgenGamma generates random deviates, and genGammaHazard gives the hazard function.

Author(s)

Markus Belfrage

Description

Plots (1) the price over time, (2) volume traded over time for a given interval, and (3) number of transactions over time for a given interval.

Usage

```
plotDescTrans(trans, windowunit = "hours", window = 1)
```

Arguments

trans a data.frame with the column 'time', 'price', and 'volume'. Currently only

works if all of those are available.

windowunit the unit of the time interval. One of "secs", "mins", "hours", or "days".

window a positive integer giving the length of the interval.

```
## Not run:
data(transData)
plotDescTrans(transData, windowunit = "hours", window = 1)
## End(Not run)
```

20 plotHazard

Description

Estimates and plots the hazard function from an estimatated ACD model.

Usage

```
plotHazard(fitModel, breaks = 20, implied = TRUE, xstop)
```

Arguments

fitModel an estimated model of class acdFit. Can also be a numerical vector.

breaks the number of quantiles used to estimate the hazard.

implied a logical flag. If TRUE then the implied hazard function using the distribution

parameter estimates will be plotted together with the nonparametric estimate of

the error term hazard function.

where to stop plotting the implied hazard.

Details

This estimator of the hazard function is based on the one used by Engle and Russell (1998). It is modified slightly to decrease its bias and inconsistency. However, the estimator is still not fully consistent when using a fixed number of breaks (quantiles).

Author(s)

Markus Belfrage

References

Engle, R.F and Russell, J.R. (1998) Autoregressive Conditional Duration: A New Model for Irregularly Spaced Transaction Data. *Econometrica*, 66(5): 1127-1162.

```
## Not run:
data(adjDurData)
fitModelWei <- acdFit(adjDurData, dist = "wei")
plotHazard(fitModelWei)
## End(Not run)</pre>
```

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plotHistAcd

Mean duration plot

Description

Plots the mean duration over time at chosen interval length

Usage

```
plotHistAcd(durations, windowunit = "mins", window = 1)
```

Arguments

durations a data.frame containing the durations and their time stamps.

windowunit the unit of the time interval. One of "secs", "mins", "hours", or "days".

window a positive integer giving the length of the interval.

Author(s)

Markus Belfrage

Examples

```
data(durData)
plotHistAcd(durData, windowunit = "days", window = 1)
## Not run:
plotHistAcd(durData, windowunit = "mins", window = 30)
## End(Not run)
```

plotLL

Plots the response surface of the log likelihood of a fitted model.

Description

Plots the log likelihood for a fitted model against either one or two of the parameters at a time. This can help to find issues with for example poor identification of a model.

22 plotLL

Arguments

fitModel a fitted model of class acdFit.

parameter1 the first parameter for the log likelihood to be plotted against. Either the index

of the parameter as an integer, or the name of the parameter.

parameter 2 the second parameter for the log likelihood to be plotted against. Either the

index of the parameter as an integer, or the name of the parameter. If left empty,

a plot with only the parameter1 will be drawn.

param1sequence, param2sequence

the sequence of points from which the log likelihood is computed. If left empty, the log likelihood will be computed at 21 points spanning between MLE-3*SD and MLE+3*SD in the one dimensional case, and the 11x11 points for the same

range in the two dimensional case.

startpoint a vector of size equal to the number of parameters in the model. If this is sup-

plied, the log likelihood will be evaluated at this point instead of the point of the

MLE (for the parameters not in parameter1 and parameter2).

length.out (optional) overrides the default number of points (for each dimension) where the

log likelihood is computed.

returnOutput a logical flag. If set to TRUE, the values of the response surface will be returned.

See 'value' below.

Value

Only if returnOutput = TRUE

1. For the one dimensional case: a data.frame with the columns 'logLikelihood', and 'param1sequence' for all the values of the parameter1 witch the log likelihood was evaluated at

2. For the two dimensional case: a list with the following items:

para1 a vector with the sequence of the parameter1 values.
para2 a vector with the sequence of the parameter2 values.

z a matrix with the log likelihood values. The element at the ith row and jth

column is evaluated at the ith para1 value and jth para2 value.

Author(s)

Markus Belfrage

Not run:

```
data(adjDurData)
#Indicates identification issues with the generelized gamma distibution:
#(Try a diffrent 'startPara' in acdFit() to get slightly a better fit)
fit <- acdFit(durations = adjDurData[1:3000, ], dist = "gengamma")
seq1 <- seq(500, 1000, 50)</pre>
```

plotRollMeanAcd 23

plotRollMeanAcd

Plots rolling means of durations

Description

Plots rolling means of durations

Usage

```
plotRollMeanAcd(durations, window = 500)
```

Arguments

durations a data.frame containing the column 'time' and 'durations'.

window the length of the rolling window.

Examples

```
data(durData)
plotRollMeanAcd(durData, window = 500)
```

plotScatterAcd

Scatter plot for ACD models

Description

Function to help scatter plot different variables of a fitted ACD model and superimposes a smoothed conditional mean using ggplot2. Can be used to investigate the possible need for non-linear models and issues with the diurnal adjustment.

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Arguments

fitModel	a fitted model of class "acdFit"
X	the variable used on the x-axis. One of "muHats", "residuals", "durations", "adjDur", "dayTime", "time", or "index".
У	the variable used on the y-axis. One of "muHats", "residuals", "durations", "adjDur", "dayTime", "time", or "index".
xlag	number of lags used for the variable shown on the x-axis.
ylag	number of lags used for the variable shown on the y-axis.
colour	a possible third variable to be represented with a colour scale. One of "muHats", "residuals", "durations", "adjDur", "dayTime", or "time".
xlim	a vector of the limits of the x-axis to possibly zoom in on a certain region.
ylim	a vector of the limits of the y-axis to possibly zoom in on a certain region.
alpha	alpha parameter passed to ggplot2. For large data sets many data points will overlap. The alpha parameter can make the points transparent, making it easier to distinguish the density of different region. Takes the value between 1 (opaque) and 0 (completely transparent).
smoothMethod	value passed as smooth argument to ggplot2. See stat_smooth.

Author(s)

Markus Belfrage

Examples

```
## Not run:
data(adjDurData)
# The mean residuals are too small for small values of the estimated conditional
# mean, suggesting a need for a different conditional mean model specification:
fitModel <- acdFit(adjDurData)
plotScatterAcd(fitModel, x = "muHats", y = "residuals")
## End(Not run)</pre>
```

qqplotAcd

Quantile-Quantile plot of the residuals

Description

Plots a QQ-plot of the residuals and the theoretical quantiles implied by the model estimates.

```
qqplotAcd(fitModel, xlim = NULL, ylim = NULL)
```

qWeibullDist 25

Arguments

fitModel a fitted ACD model, i.e. an object of class "acdFit" xlim an optional vector of limits for the x-axis ylim an optional vector of limits for the y-axis

Examples

```
data(adjDurData)
fitModelExp <- acdFit(adjDurData, dist = "exp")
qqplotAcd(fitModelExp)</pre>
```

qWeibullDist

The q-Weibull distribution

Description

Density (PDF), distribution function (CDF), quantile function (inverted CDF), random generation, exepcted value, and hazard function for the q-Weibull distribution.

Usage

```
dqweibull(x, a = .8, qdist = 1.2, b = 1, forceExpectation = F)
pqweibull(q, a = .8, qdist = 1.2, b = 1, forceExpectation = F)
qqweibull(p, a = .8, qdist = 1.2, b = 1, forceExpectation = F)
rqweibull(n = 1, a = .8, qdist = 1.2, b = 1, forceExpectation = F)
qweibullExpectation(a = .8, qdist = 1.2, b = 1)
qweibullHazard(x, a = .8, qdist = 1.2, b = 1, forceExpectation = F)
```

Arguments

x, q vector of quantiles.
p vector of probabilities.
n number of observations.
a, qdist, b parameters, see 'Details'.
forceExpectation

logical; if TRUE, the expectation of the distribution is forced to be 1 by letting b be a function of the other parameters.

Details

The PDF for the q-Weibull distribution is:

$$f(\epsilon) = (2 - q) \frac{a}{b^a} \epsilon^{a-1} \left[1 - (1 - q) \left(\frac{\epsilon}{b} \right)^a \right]^{\frac{1}{1 - q}}$$

The distribution was used for ACD models by Vuorenmaa (2009).

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References

Vuorenmaa, T. (2009) A q-Weibull Autoregressive Conditional Duration Model with an Application to NYSE and HSE data. Available at SSRN: http://ssrn.com/abstract=1952550.

resiDensityAcd

Residual Density Histogram

Description

Plots a density histogram of the residuals and superimposes the density implied by the model estimates.

Usage

```
resiDensityAcd(fitModel, xlim = NULL, binwidth = .1, density = FALSE)
```

Arguments

fitModel a fitted ACD model, i.e. an object of class "acdFit"

xlim an optional vector of limits for the x-axis

binwidth the width of the bins of the density histogram.

density if TRUE a kernel density estimate will be added

Author(s)

Markus Belfrage

```
## Not run:
data(adjDurData)
fitModelBurr <- acdFit(adjDurData, dist = "burr")
resiDensityAcd(fitModelBurr)
## End(Not run)</pre>
```

sim_ACD 27

sim_ACD	ACD simulation		
---------	----------------	--	--

Description

Simulates a sample from a specified ACD model and error term distribution dist. The error terms can also be sampled from residuals.

Usage

```
sim_ACD(N = 1000, model = "ACD", dist = "exponential", param = NULL, order = NULL,
    Nburn = 50, startX = c(1), startMu = c(1), errors = NULL, sampleErrors = TRUE,
    roundToSec = FALSE, rm0 = FALSE, bp = NULL)
```

Arguments

Value

a numerical vector of simulated ACD durations

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Author(s)

Markus Belfrage

Examples

```
x <- sim\_ACD() #simulates 1000 observations from an ACD(1,1) with exp. errors as default acdFit(x)
```

standardizeResi

Residual standardization

Description

Standardizes residuals from a fitted ACD model of class 'acdFit' by a probability integral transformation (taking the CDF, using the estimated distribution parameters, of the residuals) or by returning the Cox-Snell residuals.

Usage

```
standardizeResi(fitModel, transformation = "probIntegral")
```

Arguments

fitModel a fitted ACD model of class 'acdFit'.

transformation type of transformation done, either "probIntegral", or "cox-snell".

Details

The probability integral transformation is done by taking the CDF of the residuals from the model estimation, using the estimated distribution parameters. Under correct specification the probability integral transformed residuals should be iid. uniform(0, 1).

The Cox-Snell residuals is the computed by taking the integrated hazard of the residuals from the model estimation, using the estimated distribution parameters. Under correct specification the probability integral transformed residuals should be iid. unit exponentially distributed.

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testRmACD

LM test of no Remaining ACD (Meitz and Terasvirta, 2006)

Description

Tests if there is any remaining ACD structure in the residuals (currently only works for model = "ACD").

Usage

```
testRmACD(fitModel, pStar = 2, robust = TRUE)
```

Arguments

fitModel a fitted ACD model, i.e. an object of class "acdFit".

pStar the number of alpha parameters in the alternative hypothesis. See p* under

'Details'.

robust if TRUE the LM statistic will be calculated using the "robust" version, making its

asymptotic behavior unaffected by possible misspecification of the error term

distribution (Meitz and Terasvirta, 2006).

Details

For the model

$$x_i = \mu_i \phi_i \epsilon_i,$$

$$\mu_i = \omega + \sum_{j=1}^p \alpha_j x_{i-j} + \sum_{j=1}^q \beta_j \mu_{i-j},$$

$$\phi_i = 1 + \sum_{j=1}^{p*} \frac{x_{i-j}}{\mu_{i-j}},$$

the function tests the null hypothesis

$$H_0: \phi_i = 1.$$

Value

a list of:

chi2 the value of the LM statistic.
pv the pvalue of the test statistic.

Author(s)

Markus Belfrage

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References

Meitz, M. and Terasvirta, T. (2006). Evaluating models of autoregressive conditional duration. Journal of Business and Economic Statistics 24: 104-124.

See Also

```
testTVACD, testSTACD.
```

Examples

```
data(adjDurData)
fitModel3000obs <- acdFit(adjDurData[1:3000,])
testRmACD(fitModel3000obs, pStar = 2, robust = TRUE)</pre>
```

testSTACD

LM test against Smooth Transition ACD models (Meitz and Terasvirta, 2006)

Description

Tests if the alpha parameters and the constant should be varying with the value of the lagged durations, according to a logistic transition function (currently only works for model = "ACD").

Usage

```
testSTACD(fitModel, K = 2, robust = TRUE)
```

Arguments

fitModel a fitted ACD model, i.e. an object of class "acdFit".

K the order of the logistic transition function used for the alternative hypothesis.

robust if TRUE the LM statistic will be calculated using the "robust" version, making its

asymptotic behavior unaffected by possible misspecification of the error term

distribution (Meitz and Terasvirta, 2006).

Value

a list of:

chi2 the value of the LM statistic.

pv the pvalue of the test statistic.

References

Meitz, M. and Terasvirta, T. (2006) Evaluating models of autoregressive conditional duration. Journal of Business and Economic Statistics 24: 104-124.

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See Also

```
testRmACD, testTVACD.
```

Examples

```
data(adjDurData)
fitModel3000obs <- acdFit(adjDurData[1:3000,])
testSTACD(fitModel3000obs, K = 2, robust = TRUE)</pre>
```

testTVACD

LM test against Time-Varying ACD models (Meitz and Terasvirta, 2006)

Description

Tests if the parameters are time-varying (currently only works for model = "ACD").

Usage

```
testTVACD(fitModel, K = 2, type = "total", robust = TRUE)
```

Arguments

fitModel a fitted ACD model, i.e. an object of class "acdFit".

K the order of the logistic transition function used for the alternative hypothesis.

type either "total" or "intraday". If "total", the possible time varying parameters under

the alternative varies over the total time of the sample, whereas for "intraday",

the time variable is time of the day. See 'Details'

robust if TRUE the LM statistic will be calculated using the "robust" version, making its

asymptotic behavior unaffected by possible misspecification of the error term

distribution (Meitz and Terasvirta, 2006).

Details

This function tests the fitted standard ACD model against the TVACD model of Meitz and Terasvirta (2006). The TVACD model lets the ACD parameters vary over time by a logistic transition function.

In one specification, the time variable is total time, and a test rejecting the null in favor of this alternative specification would indicate that the ACD parameters are changing over time over the total sample.

The other specification lets the parameters be intraday varying, by letting the transition variable be the time of the day. Failing this test could indicate that the diurnal adjustment was inadequate at removing any diurnal component.

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Value

a list of:

chi2 the value of the LM statistic.

pv the pvalue of the test statistic.

Author(s)

Markus Belfrage

References

Meitz, M. and Terasvirta, T. (2006). *Evaluating models of autoregressive conditional duration*. Journal of Business and Economic Statistics 24: 104-124.

See Also

```
test Rm ACD, \, test ST ACD. \,
```

```
data(adjDurData)
fitModel5000obs <- acdFit(adjDurData[1:5000,])
testTVACD(fitModel5000obs, K = 2, type = "total", robust = TRUE)
testTVACD(fitModel5000obs, K = 2, type = "intraday", robust = TRUE)</pre>
```

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