

# Package ‘BayesChange’

April 28, 2025

**Title** Bayesian Methods for Change Points Analysis

**Version** 2.1.0

## Description

Perform change points detection on univariate and multivariate time series according to the methods presented by Asael Fabian Martínez and Ramsés H. Mena (2014) <[doi:10.1214/14-BA878](https://doi.org/10.1214/14-BA878)> and Corradin, Danese and Ongaro (2022) <[doi:10.1016/j.ijar.2021.12.019](https://doi.org/10.1016/j.ijar.2021.12.019)>. It also clusters different types of time dependent data with common change points, see ``Model-based clustering of time-dependent observations with common structural changes'' (Corradin,Danese,KhudaBukhsh and Ongaro, 2024) <[doi:10.48550/arXiv.2410.09552](https://doi.org/10.48550/arXiv.2410.09552)> for details.

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ClustCpObj	<i>ClustCpObj class constructor</i>
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### Description

A constructor for the ClustCpObj class. The class ClustCpObj contains...

### Usage

```
ClustCpObj(
  data = NULL,
  n_iterations = NULL,
  n_burnin = NULL,
  clust = NULL,
  orders = NULL,
  time = NULL,
  lkl = NULL,
  norm_vec = NULL,
  I0_MCMC = NULL,
  I0_MCMC_01 = NULL,
  kernel_ts = NULL,
  kernel_epi = NULL,
  univariate_ts = NULL
)
```

## Arguments

data	a vector or a matrix containing the values of the time series;
n_iterations	number of iterations of the MCMC algorithm;
n_burnin	number of MCMC iterations to exclude in the posterior estimate;
clust	a matrix with the clustering of each iteration.
orders	a matrix where each row corresponds to the output order of the corresponding iteration;
time	computational time in seconds;
lk1	a vector with the likelihood of the final clustering.
norm_vec	a vector with the estimated normalization constant.
I0_MCMC	traceplot for $I_0$ .
I0_MCMC_01	a 0/1 vector, the $n$ -th element is equal to 1 if the proposed $I_0$ was accepted, 0 otherwise.
kernel_ts	if TRUE data are time series.
kernel_epi	if TRUE data are survival functions.
univariate_ts	TRUE/FALSE if time series is univariate or not;

clust\_cp

*Clustering time dependent observations with common change points.*

## Description

The `clust_cp` function cluster observations with common change points. Data can be time series or survival functions.

## Usage

```
clust_cp(
  data,
  n_iterations,
  n_burnin = 0,
  params = list(),
  alpha_SM = 1,
  B = 1000,
  L = 1,
  q = 0.5,
  kernel,
  print_progress = TRUE,
  user_seed = 1234
)
```

## Arguments

<code>data</code>	a matrix or an array If a matrix the algorithm for univariate time series is used, where each row is a time series. If an array, the algorithm is run for multivariate time series. Each slice of the array is a matrix where the rows are the dimensions of the time series.
<code>n_iterations</code>	number of MCMC iterations.
<code>n_burnin</code>	number of iterations that must be excluded when computing the posterior estimate.
<code>params</code>	a list of parameters: If the time series is univariate the following must be specified: <ul style="list-style-type: none"> <li>• a,b,c parameters of the integrated likelihood.</li> <li>• phi correlation parameter in the likelihood.</li> </ul> If the time series is multivariate the following must be specified: <ul style="list-style-type: none"> <li>• k_0,nu_0,S_0,m_0 parameters of the integrated likelihood.</li> <li>• phi correlation parameter in the likelihood.</li> </ul> If data are survival functions: <ul style="list-style-type: none"> <li>• M number of Monte Carlo iterations when computing the likelihood of the survival function.</li> <li>• xi recovery rate fixed constant for each population at each time.</li> <li>• a0,b0 parameters for the computation of the integrated likelihood of the survival functions.</li> <li>• I0_var variance for the Metropolis-Hastings estimation of the proportion of infected at time 0.</li> <li>• p prior average number of change points for each order.</li> </ul>
<code>alpha_SM</code>	$\alpha$ for the split-merge main algorithm.
<code>B</code>	number of orders for the normalization constant.
<code>L</code>	number of split-merge steps for the proposal step.
<code>q</code>	probability of a split in the split-merge proposal and acceleration step.
<code>kernel</code>	can be "ts" if data are time series or "epi" if data are survival functions.
<code>print_progress</code>	If TRUE (default) print the progress bar.
<code>user_seed</code>	seed for random distribution generation.

## Value

A `ClustCpObj` class object containing

- `$data` vector or matrix with the data.
- `$n_iterations` number of iterations.
- `$n_burnin` number of burn-in iterations.
- `$clust` a matrix where each row corresponds to the output cluster of the corresponding iteration.

- \$orders a multidimensional array where each slice is a matrix and represent an iteration. The row of each matrix correspond the order associated to the corresponding cluster.
- \$time computational time.
- \$lkl a matrix where each row is the likelihood of each observation computed at the corresponding iteration.
- \$norm\_vec a vector containing the normalization constant computed at the beginning of the algorithm.
- I0\_MCMC traceplot for  $I_0$ .
- I0\_MCMC\_01 a 0/1 vector, the  $n$ -th element is equal to 1 if the proposed  $I_0$  was accepted, 0 otherwise.
- \$kernel\_ts if TRUE data are time series.
- \$kernel\_epsi if TRUE data are survival function.
- \$univariate\_ts TRUE if data is an univariate time series, FALSE if it is a multivariate time series.

## References

Corradin, R., Danese, L., KhudaBukhsh, W. R., & Ongaro, A. (2024). *Model-based clustering of time-dependent observations with common structural changes*. arXiv preprint arXiv:2410.09552.

## Examples

```
## Univariate time series

data_mat <- matrix(NA, nrow = 5, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_mat[4,] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
data_mat[5,] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))

out <- clust_cp(data = data_mat, n_iterations = 5000, n_burnin = 1000,
                 L = 1, params = list(phi = 0.5), B = 1000, kernel = "ts")

print(out)

## Multivariate time series

data_array <- array(data = NA, dim = c(3,100,5))

data_array[1,,1] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_array[2,,1] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_array[3,,1] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))

data_array[1,,2] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_array[2,,2] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
```

```

data_array[3,,2] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))

data_array[1,,3] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_array[2,,3] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_array[3,,3] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))

data_array[1,,4] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
data_array[2,,4] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
data_array[3,,4] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))

data_array[1,,5] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))
data_array[2,,5] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))
data_array[3,,5] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))

out <- clust_cp(data = data_array, n_iterations = 3000, n_burnin = 1000,
                  params = list(phi = 0.5, k_0 = 0.25,
                                nu_0 = 5, S_0 = diag(0.1,3,3),
                                m_0 = rep(0,3)), B = 1000, kernel = "ts")

print(out)

## Epidemiological data


data_mat <- matrix(NA, nrow = 5, ncol = 50)

betas <- list(c(rep(0.45, 25),rep(0.14,25)),
               c(rep(0.55, 25),rep(0.11,25)),
               c(rep(0.50, 25),rep(0.12,25)),
               c(rep(0.52, 10),rep(0.15,40)),
               c(rep(0.53, 10),rep(0.13,40)))

inf_times <- list()

for(i in 1:5){

  inf_times[[i]] <- sim_epi_data(10000, 10, 50, betas[[i]], 1/8)

  vec <- rep(0,50)
  names(vec) <- as.character(1:50)

  for(j in 1:50){
    if(as.character(j) %in% names(table(floor(inf_times[[i]])))){
      vec[j] = table(floor(inf_times[[i]]))[which(names(table(floor(inf_times[[i]]))) == j)]
    }
  }
  data_mat[i,] <- vec
}

out <- clust_cp(data = data_mat, n_iterations = 100, n_burnin = 10,
                  params = list(M = 100, xi = 1/8), B = 1000, kernel = "epi")

```

```
clust_cp.epi
```

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```
print(out)
```

---

```
clust_cp.epi
```

*Clustering Epidemiological survival functions with common changes  
in time*

---

## Description

Clustering Epidemiological survival functions with common changes in time

## Usage

```
clust_cp.epi(  
  data,  
  n_iterations,  
  M,  
  B,  
  L,  
  xi = 1/8,  
  alpha_SM = 1,  
  q = 0.1,  
  a0 = 4,  
  b0 = 10,  
  I0_var = 0.01,  
  avg_blk = 0.003,  
  print_progress = TRUE,  
  user_seed = 1234L  
)
```

## Arguments

data	a matrix where each entry is the number of infected for a population (row) at a specific discrete time (column).
n_iterations	Second value
M	number of Monte Carlo iterations when computing the likelihood of the survival function.
B	number of orders for the normalisation constant.
L	number of split-merge steps for the proposal step.
xi	recovery rate fixed constant for each population at each time.
alpha_SM	$\alpha$ parameter for the main split-merge algorithm.
q	probability of performing a split when updating the single order for the proposal procedure.

a0, b0	parameters for the computation of the integrated likelihood of the survival functions.
I0_var	variance for the Metropolis-Hastings estimation of the proportion of infected at time 0.
avg_blk	average number of change points for the random generated orders.
print_progress	If TRUE (default) print the progress bar.
user_seed	seed for random distribution generation.

### Value

Function *clust\_cp.epi* returns a list containing the following components:

- \$clust a matrix where each row corresponds to the output cluster of the corresponding iteration.
- \$orders a multidimensional matrix where each slice is a matrix with the orders associated to the output cluster of that iteration.
- time computational time in seconds.
- \$llik a matrix containing the log-likelihood of each population at each iteration.
- \$rho traceplot for the proportion of infected individuals at time 0.

### Examples

```

data_mat <- matrix(NA, nrow = 5, ncol = 50)

betas <- list(c(rep(0.45, 25),rep(0.14,25)),
               c(rep(0.55, 25),rep(0.11,25)),
               c(rep(0.50, 25),rep(0.12,25)),
               c(rep(0.52, 10),rep(0.15,40)),
               c(rep(0.53, 10),rep(0.13,40)))

inf_times <- list()

for(i in 1:5){

  inf_times[[i]] <- sim_epidata(10000, 10, 50, betas[[i]], 1/8)

  vec <- rep(0,50)
  names(vec) <- as.character(1:50)

  for(j in 1:50){
    if(as.character(j) %in% names(table(floor(inf_times[[i]])))){
      vec[j] = table(floor(inf_times[[i]]))[which(names(table(floor(inf_times[[i]]))) == j)]
    }
  }
  data_mat[i,] <- vec
}

out <- clust_cp.epi(data = data_mat, n_iterations = 3000, M = 250, B = 1000, L = 1)

```

---

clust\_cp\_multi*Clustering multivariate times series with common changes in time*

---

**Description**

Clustering multivariate times series with common changes in time

**Usage**

```
clust_cp_multi(
  data,
  n_iterations,
  B,
  L,
  phi,
  k_0,
  nu_0,
  S_0,
  m_0,
  q = 0.5,
  alpha_SM = 0.1,
  print_progress = TRUE,
  user_seed = 1234L
)
```

**Arguments**

data	a multidimensional matrix where each element is a matrix whose rows are the observations and columns the dimensions.
n_iterations	number of MCMC iterations.
B	number of orders for the normalisation constant.
L	number of split-merge steps for the proposal step.
phi, k_0, nu_0, S_0, m_0	parameters of the integrated likelihood.
q	probability of a split in the split-merge proposal and acceleration step.
alpha_SM	$\alpha$ for the main split-merge algorithm.
print_progress	If TRUE (default) print the progress bar.
user_seed	seed for random distribution generation.

**Value**

Function `clust_cp_multi` returns a list containing the following components:

- \$clust a matrix where each row corresponds to the output cluster of the corresponding iteration.

- \$orders a multidimensional array where each slice is a matrix and represent an iteration. The row of each matrix correspond the order associated to the corresponding cluster.
- time computational time in seconds.
- \$norm\_vec a vector containing the normalisation constant computed at the beginning of the algorithm.

### Examples

```

data_array <- array(data = NA, dim = c(3,100,5))

data_array[1,,1] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_array[2,,1] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_array[3,,1] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))

data_array[1,,2] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_array[2,,2] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_array[3,,2] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))

data_array[1,,3] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_array[2,,3] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_array[3,,3] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))

data_array[1,,4] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
data_array[2,,4] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
data_array[3,,4] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))

data_array[1,,5] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))
data_array[2,,5] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))
data_array[3,,5] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))

out <- clust_cp_multi(data = data_array, n_iterations = 3000, B = 1000, L = 1,
                      phi = 0.1, k_0 = 0.25, nu_0 = 5, S_0 = diag(0.1,3,3), m_0 = rep(0,3))

```

### Description

Clustering univariate times series with common changes in time

### Usage

```

clust_cp_uni(
  data,
  n_iterations,
  B,
  L,
  phi,

```

```

  a = 1,
  b = 1,
  c = 1,
  q = 0.5,
  alpha_SM = 0.1,
  print_progress = TRUE,
  user_seed = 1234L
)

```

## Arguments

data	a matrix where each row is an observation and each column corresponds to a discrete time.
n_iterations	number of MCMC iterations.
B	number of orders for the normalisation constant.
L	number of split-merge steps for the proposal step.
phi, a, b, c	parameters of the integrated likelihood.
q	probability of a split in the split-merge proposal and acceleration step.
alpha_SM	$\alpha$ for the main split-merge algorithm.
print_progress	If TRUE (default) print the progress bar.
user_seed	seed for random distribution generation.

## Value

Function `clust_cp_uni` returns a list containing the following components:

- `$clust` a matrix where each row corresponds to the output cluster of the corresponding iteration.
- `$orders` a multidimensional array where each slice is a matrix and represent an iteration. The row of each matrix correspond the order associated to the corresponding cluster.
- `$time` computational time in seconds.
- `$norm_vec` a vector containing the normalisation constant computed at the beginning of the algorithm.

## Examples

```

data_mat <- matrix(NA, nrow = 5, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_mat[4,] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
data_mat[5,] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))

out <- clust_cp_uni(data = data_mat, n_iterations = 5000, B = 1000, L = 1, phi = 0.5)

```

---

DetectCpObj	<i>DetectCpObj class constructor</i>
-------------	--------------------------------------

---

## Description

A constructor for the DetectCpObj class. The class DetectCpObj contains...

## Usage

```
DetectCpObj(
  data = NULL,
  n_iterations = NULL,
  n_burnin = NULL,
  orders = NULL,
  time = NULL,
  phi_MCMC = NULL,
  phi_MCMC_01 = NULL,
  sigma_MCMC = NULL,
  sigma_MCMC_01 = NULL,
  theta_MCMC = NULL,
  I0_MCMC = NULL,
  I0_MCMC_01 = NULL,
  kernel_ts = NULL,
  kernel_epsi = NULL,
  univariate_ts = NULL
)
```

## Arguments

<code>data</code>	a vector or a matrix containing the values of the time series;
<code>n_iterations</code>	number of iterations of the MCMC algorithm;
<code>n_burnin</code>	number of MCMC iterations to exclude in the posterior estimate;
<code>orders</code>	a matrix where each row corresponds to the output order of the corresponding iteration;
<code>time</code>	computational time in seconds;
<code>phi_MCMC</code>	traceplot for $\gamma$ .
<code>phi_MCMC_01</code>	a 0/1 vector, the $n$ -th element is equal to 1 if the proposed $\phi$ was accepted, 0 otherwise.
<code>sigma_MCMC</code>	traceplot for $\sigma$ .
<code>sigma_MCMC_01</code>	a 0/1 vector, the $n$ -th element is equal to 1 if the proposed $\sigma$ was accepted, 0 otherwise.
<code>theta_MCMC</code>	traceplot for $\theta$ .
<code>I0_MCMC</code>	traceplot for $I_0$ .

I0_MCMC_01	a 0/1 vector, the $n$ -th element is equal to 1 if the proposed $I_0$ was accepted, 0 otherwise.
kernel_ts	if TRUE data are time series.
kernel_epi	if TRUE data are survival functions.
univariate_ts	TRUE/FALSE if time series is univariate or not.

detect\_cp

*Detect change points on time series.*

## Description

The detect\_cp function detect change points on univariate and multivariate time series.

## Usage

```
detect_cp(
  data,
  n_iterations,
  n_burnin = 0,
  q = 0.5,
  params = list(),
  kernel,
  print_progress = TRUE,
  user_seed = 1234
)
```

## Arguments

**data** a vector or a matrix. If a vector the algorithm for univariate time series is used. If a matrix, where rows are the observations and columns are the times, then the algorithm for multivariate time series is used.

**n\_iterations** number of MCMC iterations.

**n\_burnin** number of iterations that must be excluded when computing the posterior estimate.

**q** probability of performing a split at each iteration.

**params** a list of parameters:

If data is an univariate time series the following must be specified:

- a, b, c parameters of the Normal-Gamma prior for  $\mu$  and  $\lambda$ .
- prior\_var\_phi variance for the proposal in the  $N(0, \sigma_\phi^2)$  posterior estimate of  $\theta$ .
- par\_theta\_c parameter of the shifted Gamma prior of  $\theta$ .
- par\_theta\_d parameter of the shifted Gamma prior of  $\theta$ .

If the time series is multivariate the following must be specified:

- $m_0, k_0, nu_0, S_0$  parameters for the Normal-Inverse-Wishart prior for  $(\mu, \lambda)$ .
- $prior\_var\_phi$  variance for the proposal in the  $N(0, \sigma_\phi^2)$  posterior estimate of  $\theta$ .
- $par\_theta_c$  parameter of the shifted Gamma prior of  $\theta$ .
- $par\_theta_d$  parameter of the shifted Gamma prior of  $\theta$ .

If data are survival functions:

- $M$  number of Monte Carlo iterations when computing the likelihood of the survival function.
- $xi$  recovery rate fixed constant for each population at each time.
- $a0, b0$  parameters for the computation of the integrated likelihood of the survival functions.
- $I0\_var$  variance for the Metropolis-Hastings estimation of the proportion of infected at time 0.
- $p$  prior average number of change points for each order.

**kernel** can be "ts" if data are time series or "epi" if data are survival functions.

**print\_progress** If TRUE (default) print the progress bar.

**user\_seed** seed for random distribution generation.

### Value

A DetectCpObj class object containing

- **\$data** vector or matrix with the data.
- **\$n\_iterations** number of iterations.
- **\$n\_burnin** number of burn-in iterations.
- **\$orders** matrix where each entries is the assignment of the realization to a block. Rows are the iterations and columns the times.
- **\$time** computational time.
- **\$gammaMCMC** traceplot for  $\gamma$ .
- **\$phi\_MCMC\_01** a 0/1 vector, the  $n$ -th element is equal to 1 if the proposed  $\gamma$  was accepted, 0 otherwise.
- **\$sigma\_MCMC** traceplot for  $\sigma$ .
- **\$sigma\_MCMC\_01** a 0/1 vector, the  $n$ -th element is equal to 1 if the proposed  $\sigma$  was accepted, 0 otherwise.
- **\$theta\_MCMC** traceplot for  $\theta$ .
- **I0\_MCMC** traceplot for  $I_0$ .
- **I0\_MCMC\_01** a 0/1 vector, the  $n$ -th element is equal to 1 if the proposed  $I_0$  was accepted, 0 otherwise.
- **kernel\_ts** if TRUE data are time series.
- **kernel\_epi** if TRUE data are survival functions.
- **\$univariate\_ts** TRUE if data is an univariate time series, FALSE if it is a multivariate time series.

## References

- Martínez, A. F., & Mena, R. H. (2014). On a Nonparametric Change Point Detection Model in Markovian Regimes. *Bayesian Analysis*, 9(4), 823–858. doi:10.1214/14BA878
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## Examples

```
## Univariate time series

data_vec <- as.numeric(c(rnorm(50,0,0.1), rnorm(50,1,0.25)))

out <- detect_cp(data = data_vec, n_iterations = 2500, n_burnin = 500,
                  params = list(a = 1, b = 1, c = 0.1), kernel = "ts")

print(out)

## Multivariate time series

data_mat <- matrix(NA, nrow = 3, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))

out <- detect_cp(data = data_mat, n_iterations = 2500, n_burnin = 500,
                  params = list(m_0 = rep(0,3), k_0 = 0.25, nu_0 = 4,
                                S_0 = diag(1,3,3)), kernel = "ts")

print(out)

## Survival functions

data_mat <- matrix(NA, nrow = 1, ncol = 100)

betas <- c(rep(0.45, 25),rep(0.14,75))

inf_times <- sim_epi_data(10000, 10, 100, betas, 1/8)

inf_times_vec <- rep(0,100)
names(inf_times_vec) <- as.character(1:100)

for(j in 1:100){
  if(as.character(j) %in% names(table(floor(inf_times)))){
    inf_times_vec[j] = table(floor(inf_times))[which(names(table(floor(inf_times))) == j)]
  }
}
```

```

data_mat[1,] <- inf_times_vec

out <- detect_cp(data = data_mat, n_iterations = 500, n_burnin = 100,
                   params = list(M = 250, xi = 1/8, a0 = 40, b0 = 10), kernel = "epi")

print(out)

```

**detect\_cp.epi***Detect Change Points on a survival function***Description**

Detect Change Points on a survival function

**Usage**

```

detect_cp.epi(
  data,
  n_iterations,
  q,
  M,
  xi,
  a0,
  b0,
  I0_var = 0.01,
  print_progress = TRUE,
  user_seed = 1234L
)

```

**Arguments**

<b>data</b>	a matrix where each row is a component of the time series and the columns correspond to the times.
<b>n_iterations</b>	number of MCMC iterations.
<b>q</b>	probability of performing a split at each iteration.
<b>M</b>	number of Monte Carlo iterations when computing the likelihood of the survival function.
<b>xi</b>	recovery rate fixed constant for each population at each time.
<b>a0, b0</b>	parameters for the computation of the integrated likelihood of the survival functions.
<b>I0_var</b>	variance for the Metropolis-Hastings estimation of the proportion of infected at time 0.
<b>print_progress</b>	If TRUE (default) print the progress bar.
<b>user_seed</b>	seed for random distribution generation.

**Value**

Function `detect_cp_epi` returns a list containing the following components:

- `$orders` a matrix where each row corresponds to the output order of the corresponding iteration.
- time computational time in seconds.
- `$I0_MCMC` traceplot for  $I_0$ .
- `$I0_MCMC_01` a 0/1 vector, the  $n$ -th element is equal to 1 if the proposed  $I_0$  was accepted, 0 otherwise.

**Examples**

```
data_mat <- matrix(NA, nrow = 1, ncol = 100)

betas <- c(rep(0.45, 25), rep(0.14, 75))

inf_times <- sim_epidata(10000, 10, 100, betas, 1/8)

inf_times_vec <- rep(0, 100)
names(inf_times_vec) <- as.character(1:100)

for(j in 1:100){
  if(as.character(j) %in% names(table(floor(inf_times)))){
    inf_times_vec[j] =
    table(floor(inf_times))[which(names(table(floor(inf_times))) == j)]}
}

data_mat[1,] <- inf_times_vec

out <- detect_cp_epi(data = data_mat, n_iterations = 250, q = 0.5,
                      xi = 1/8, a0 = 40, b0 = 10, M = 250)
```

**Description**

Detect Change Points on multivariate time series

**Usage**

```
detect_cp_multi(
  data,
  n_iterations,
  q,
  k_0,
```

```

nu_0,
S_0,
m_0,
par_theta_c = 1,
par_theta_d = 1,
prior_var_phi = 0.1,
print_progress = TRUE,
user_seed = 1234L
)

```

## Arguments

- data** a matrix where each row is a component of the time series and the columns correposond to the times.  
**n\_iterations** number of MCMC iterations.  
**q** probability of performing a split at each iteration.  
**k\_0, nu\_0, S\_0, m\_0** parameters for the Normal-Inverse-Wishart prior for  $(\mu, \lambda)$ .  
**par\_theta\_c, par\_theta\_d** parameters for the shifted Gamma prior for  $\theta$ .  
**prior\_var\_phi** parameters for the correlation coefficient in the likelihood.  
**print\_progress** If TRUE (default) print the progress bar.  
**user\_seed** seed for random distribution generation.

## Value

Function detect\_cp\_multi returns a list containing the following components:

- \$orders a matrix where each row corresponds to the output order of the corresponding iteration.
- time computational time in seconds.
- \$phi\_MCMC traceplot for  $\gamma$ .
- \$phi\_MCMC\_01 a 0/1 vector, the  $n$ -th element is equal to 1 if the proposed  $\phi$  was accepted, 0 otherwise.
- \$sigma\_MCMC traceplot for  $\sigma$ .
- \$sigma\_MCMC\_01 a 0/1 vector, the  $n$ -th element is equal to 1 if the proposed  $\sigma$  was accepted, 0 otherwise.
- \$theta\_MCMC traceplot for  $\theta$ .

## Examples

```

data_mat <- matrix(NA, nrow = 3, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))

```

```
out <- detect_cp_multi(data = data_mat,
                        n_iterations = 2500,
                        q = 0.25, k_0 = 0.25, nu_0 = 4, S_0 = diag(1,3,3), m_0 = rep(0,3),
                        par_theta_c = 2, par_theta_d = 0.2, prior_var_phi = 0.1)
```

**detect\_cp\_uni***Detect Change Points on an univariate time series.***Description**

Detect Change Points on an univariate time series.

**Usage**

```
detect_cp_uni(
  data,
  n_iterations,
  q,
  a = 1,
  b = 1,
  c = 0.1,
  prior_var_phi = 0.1,
  par_theta_c = 1,
  par_theta_d = 1,
  print_progress = TRUE,
  user_seed = 1234L
)
```

**Arguments**

<b>data</b>	vector of observations.
<b>n_iterations</b>	number of MCMC iteration.
<b>q</b>	probability of performing a split at each iterations.
<b>a, b, c</b>	parameters of the Normal-Gamma prior for $\mu$ and $\lambda$ .
<b>prior_var_phi</b>	parameters for the correlation coefficient in the likelihood.
<b>par_theta_c, par_theta_d</b>	parameters of the shifted Gamma prior for $\theta$ .
<b>print_progress</b>	If TRUE (default) print the progress bar.
<b>user_seed</b>	seed for random distribution generation.

**Value**

Function `detect_cp_uni` returns a list containing the following components:

- `$orders` a matrix where each row corresponds to the output order of the corresponding iteration.
- time computational time in seconds.
- `$sigma_MCMC` traceplot for  $\sigma$ .
- `$sigma_MCMC_01` a 0/1 vector, the  $n$ -th element is equal to 1 if the proposed  $\sigma$  was accepted, 0 otherwise.
- `$theta_MCMC` traceplot for  $\theta$ .

**Examples**

```
data_vec <- as.numeric(c(rnorm(50,0,0.1), rnorm(50,1,0.25)))

out <- detect_cp_uni(data = data_vec,
                      n_iterations = 2500,
                      q = 0.25)
```

**plot.ClustCpObj** *Plot estimated partition*

**Description**

The `plot` method plots the estimates partition through the salso algorithm, for a `ClustCpObj` class object.

**Usage**

```
## S3 method for class 'ClustCpObj'
plot(
  x,
  y = NULL,
  loss = "VI",
  maxNClusters = 0,
  nRuns = 16,
  maxZealousAttempts = 10,
  ...
)
```

### Arguments

x	an object of class ClustCpObj.
y	parameter of the generic method.
loss	The loss function used to estimate the final partition, it can be "VI", "binder", "omARI", "NVI", "ID", "NID".
maxNClusters	maximum number of clusters in salso procedure.
nRuns	number of runs in salso procedure.
maxZealousAttempts	maximum number of zealous attempts in salso procedure.
...	parameter of the generic method.

### Value

The function returns a ggplot object representing the time series or the survival functions colored according to the final partition.

### Examples

```
## Time series

data_mat <- matrix(NA, nrow = 5, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_mat[4,] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
data_mat[5,] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))

out <- clust_cp(data = data_mat, n_iterations = 5000, n_burnin = 1000,
                  params = list(L = 1, B = 1000, phi = 0.5), kernel = "ts")

plot(out)

## Survival functions

data_mat <- matrix(NA, nrow = 5, ncol = 50)

betas <- list(c(rep(0.45, 25),rep(0.14,25)),
               c(rep(0.55, 25),rep(0.11,25)),
               c(rep(0.50, 25),rep(0.12,25)),
               c(rep(0.52, 10),rep(0.15,40)),
               c(rep(0.53, 10),rep(0.13,40)))

inf_times <- list()

for(i in 1:5){
  inf_times[[i]] <- sim_epi_data(10000, 10, 50, betas[[i]], 1/8)
```

```

vec <- rep(0,50)
names(vec) <- as.character(1:50)
for(j in 1:50){
  if(as.character(j) %in% names(table(floor(inf_times[[i]])))){
    vec[j] = table(floor(inf_times[[i]]))[which(names(table(floor(inf_times[[i]]))) == j)]
  }
}
data_mat[i,] <- vec
}

out <- clust_cp(data = data_mat, n_iterations = 100, n_burnin = 10,
                 params = list(M = 100, L = 1, B = 100), kernel = "epi")

plot(out)

```

**plot.DetectCpObj**      *Plot estimated change points*

## Description

The `plot` method plots the estimates change points estimated through the salso algorithm, for a `DetectCpObj` class object.

## Usage

```

## S3 method for class 'DetectCpObj'
plot(
  x,
  y = NULL,
  plot_freq = FALSE,
  loss = "VI",
  maxNClusters = 0,
  nRuns = 16,
  maxZealousAttempts = 10,
  ...
)

```

## Arguments

- `x`            an object of class `DetectCpObj`.
- `y, ...`        parameters of the generic method.
- `plot_freq`     if TRUE also the histogram with the empirical frequency of each change point is plotted.
- `loss`           The loss function used to estimate the final partition, it can be "VI", "binder", "omARI", "NVI", "ID", "NID".

```

maxNClusters      maximum number of clusters in salso procedure.
nRuns            number of runs in salso procedure.
maxZealousAttempts
                  maximum number of zealous attempts in salso procedure.

```

### Value

The function returns a ggplot object representing the detected change points. If `plot_freq = TRUE` is plotted also an histogram with the frequency of times that a change point has been detected in the MCMC chain.

### Examples

```

data_mat <- matrix(NA, nrow = 3, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))

out <- detect_cp(data = data_mat, n_iterations = 2500, n_burnin = 500,
                   params = list(q = 0.25, k_0 = 0.25, nu_0 = 4, S_0 = diag(1,3,3),
                                 m_0 = rep(0,3), par_theta_c = 2, par_theta_d = 0.2,
                                 prior_var_phi = 0.1), kernel = "ts")
plot(out)

```

### posterior\_estimate.ClustCpObj

*Estimate the change points of the data*

### Description

The `posterior_estimate` method estimates the change points of the data making use of the salso algorithm, for a `DetectCPObj` class object.

### Usage

```

## S3 method for class 'ClustCpObj'
posterior_estimate(
  object,
  loss = "VI",
  maxNClusters = 0,
  nRuns = 16,
  maxZealousAttempts = 10,
  ...
)

```

## Arguments

<code>object</code>	an object of class <code>ClustCpObj</code> .
<code>loss</code>	The loss function used to estimate the final partition, it can be "VI", "binder", "omARI", "NVI", "ID", "NID".
<code>maxNCusters</code>	maximum number of clusters in salso procedure.
<code>nRuns</code>	number of runs in salso procedure.
<code>maxZealousAttempts</code>	maximum number of zealous attempts in salso procedure.
<code>...</code>	parameter of the generic method.

## Details

put details here

## Value

The function returns a vector with the cluster assignment of each observation.

## References

#' D. B. Dahl, D. J. Johnson, and P. Müller (2022), Search Algorithms and Loss Functions for Bayesian Clustering, *Journal of Computational and Graphical Statistics*, 31(4), 1189-1201, doi:[10.1080/10618600.2022.2069779](https://doi.org/10.1080/10618600.2022.2069779).

## Examples

```
data_mat <- matrix(NA, nrow = 5, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_mat[4,] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
data_mat[5,] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))

out <- clust_cp(data = data_mat, n_iterations = 5000, n_burnin = 1000,
                 params = list(L = 1, B = 1000, phi = 0.5), kernel = "ts")

posterior_estimate(out)
```

---

`posterior_estimate.DetectCpObj`  
*Estimate the change points of the data*

---

## Description

The `posterior_estimate` method estimates the change points of the data making use of the salso algorithm, for a `DetectCPObj` class object.

## Usage

```
## S3 method for class 'DetectCpObj'
posterior_estimate(
  object,
  loss = "VI",
  maxNClusters = 0,
  nRuns = 16,
  maxZealousAttempts = 10,
  ...
)
```

## Arguments

<code>object</code>	an object of class <code>DetectCPObj</code> .
<code>loss</code>	The loss function used to estimate the final partition, it can be "VI", "binder", "omARI", "NVI", "ID", "NID".
<code>maxNClusters</code>	maximum number of clusters in salso procedure.
<code>nRuns</code>	number of runs in salso procedure.
<code>maxZealousAttempts</code>	maximum number of zealous attempts in salso procedure.
<code>...</code>	parameter of the generic method.

## Details

put details here

## Value

The function returns a vector with the cluster assignment of each observation.

## References

D. B. Dahl, D. J. Johnson, and P. Müller (2022), Search Algorithms and Loss Functions for Bayesian Clustering, *Journal of Computational and Graphical Statistics*, 31(4), 1189-1201, [doi:10.1080/10618600.2022.2069779](https://doi.org/10.1080/10618600.2022.2069779).

## Examples

```
data_vec <- as.numeric(c(rnorm(50,0,0.1), rnorm(50,1,0.25)))

out <- detect_cp(data = data_vec, n_iterations = 1000, n_burnin = 100,
                  params = list(q = 0.25, phi = 0.1, a = 1, b = 1, c = 0.1), kernel = "ts")

posterior_estimate(out)
```

**print.ClustCpObj**      *ClustCpObj print method*

## Description

The `ClustCpObj` method prints which algorithm was run.

## Usage

```
## S3 method for class 'ClustCpObj'
print(x, ...)
```

## Arguments

<code>x</code>	an object of class <code>ClustCpObj</code> .
...	parameter of the generic method.

## Examples

```
data_mat <- matrix(NA, nrow = 5, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_mat[4,] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
data_mat[5,] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))

out <- clust_cp(data = data_mat, n_iterations = 5000, n_burnin = 1000,
                  params = list(L = 1, B = 1000, phi = 0.5), kernel = "ts")

print(out)
```

<code>print.DetectCpObj</code>	<i>DetectCpObj print method</i>
--------------------------------	---------------------------------

## Description

The DetectCpObj method prints which algorithm was run.

## Usage

```
## S3 method for class 'DetectCpObj'
print(x, ...)
```

## Arguments

<code>x</code>	an object of class DetectCpObj.
<code>...</code>	parameter of the generic method.

## Examples

```
data_mat <- matrix(NA, nrow = 3, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))

out <- detect_cp(data = data_mat, n_iterations = 2500, n_burnin = 500,
                  params = list(q = 0.25, k_0 = 0.25, nu_0 = 4,
                                S_0 = diag(1,3,3), m_0 = rep(0,3),
                                par_theta_c = 2, par_theta_d = 0.2,
                                prior_var_phi = 0.1), kernel = "ts")
print(out)
```

<code>sim_epidata</code>	<i>Simulate epidemiological data</i>
--------------------------	--------------------------------------

## Description

Simulate epidemiological data

## Usage

```
sim_epidata(S0, I0, max_time, beta_vec, xi_0, user_seed = 1234L)
```

**Arguments**

<code>S0</code>	number of individuals in the population.
<code>I0</code>	number of infected individuals at time 0.
<code>max_time</code>	maximum observed time.
<code>beta_vec</code>	vector with the infection rate for each discrete time.
<code>xi_0</code>	the recovery rate of the population, must be in (0, 1).
<code>user_seed</code>	seed for random distribution generation.

**Value**

Function `sim.epi.data` returns a vector with the simulated infection times.

**Examples**

```
betas <- c(rep(0.45, 25), rep(0.14, 25))

inf_times <- as.numeric()

inf_times <- sim.epi.data(10000, 10, 50, betas, 1/8)
```

`summary.ClustCpObj`      *ClustCpObj summary method*

**Description**

The `ClustCpObj` method returns a summary of the algorithm.

**Usage**

```
## S3 method for class 'ClustCpObj'
summary(object, ...)
```

**Arguments**

<code>object</code>	an object of class <code>ClustCpObj</code> .
<code>...</code>	parameter of the generic method.

**Examples**

```
data_mat <- matrix(NA, nrow = 5, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))
data_mat[4,] <- as.numeric(c(rnorm(25,0,0.135), rnorm(75,1,0.225)))
```

```

data_mat[5,] <- as.numeric(c(rnorm(25,0,0.155), rnorm(75,1,0.280)))

out <- clust_cp(data = data_mat, n_iterations = 5000, n_burnin = 1000,
                  params = list(L = 1, B = 1000, phi = 0.5), kernel = "ts")

summary(out)

```

**summary.DetectCpObj**    *DetectCpObj summary method*

### Description

The DetectCpObj method returns a summary of the algorithm.

### Usage

```
## S3 method for class 'DetectCpObj'
summary(object, ...)
```

### Arguments

object	an object of class DetectCpObj;
...	parameter of the generic method.

### Examples

```

data_mat <- matrix(NA, nrow = 3, ncol = 100)

data_mat[1,] <- as.numeric(c(rnorm(50,0,0.100), rnorm(50,1,0.250)))
data_mat[2,] <- as.numeric(c(rnorm(50,0,0.125), rnorm(50,1,0.225)))
data_mat[3,] <- as.numeric(c(rnorm(50,0,0.175), rnorm(50,1,0.280)))

out <- detect_cp(data = data_mat, n_iterations = 2500, n_burnin = 500,
                  params = list(q = 0.25, k_0 = 0.25, nu_0 = 4,
                                S_0 = diag(1,3,3), m_0 = rep(0,3),
                                par_theta_c = 2, par_theta_d = 0.2,
                                prior_var_phi = 0.1), kernel = "ts")

summary(out)

```

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