

# Package ‘LSVAR’

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**Type** Package

**Title** Estimation of Low Rank Plus Sparse Structured Vector  
Auto-Regressive (VAR) Model

**Version** 1.2

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**Description** Implementations of estimation algorithm of low rank plus sparse structured VAR model by using Fast Iterative Shrinkage-Thresholding Algorithm (FISTA). It relates to the algorithm in Sumanta, Li, and Michailidis (2019) <[doi:10.1109/TSP.2018.2887401](https://doi.org/10.1109/TSP.2018.2887401)>.

**License** GPL-2

**Encoding** UTF-8

**Imports** igraph, mvtnorm, pracma

**Suggests** rmarkdown, knitr

**VignetteBuilder** knitr

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**NeedsCompilation** no

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<b>f.func</b>	<i>Main loss function for quadratic loss</i>
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## Description

Main loss function

## Usage

```
f.func(x, A, b)
```

## Arguments

x	Model parameters
A	Design matrix with size of n by p
b	Correspond vector or matrix

## Value

Value of objective function

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<b>fista.LpS</b>	<i>A function to solve low rank plus sparse model estimation using FISTA algorithm</i>
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## Description

A function to solve low rank plus sparse model estimation

## Usage

```
fista.LpS(
  data,
  lambda,
  mu,
  alpha_L = 0.25,
  niter = 100,
  backtracking = TRUE,
  x.true = NULL
)
```

**Arguments**

<code>data</code>	A numeric dataset with size of n by p
<code>lambda</code>	A positive numeric value, indicating the tuning parameter for sparse component
<code>mu</code>	A positive numeric value, indicating the tuning parameter for low rank component
<code>alpha_L</code>	The constraint coefficient of low rank component, default is 0.25
<code>niter</code>	The maximum number of iterations required for FISTA
<code>backtracking</code>	A boolean argument, indicating that use backtracking in the FISTA
<code>x.true</code>	A p by p matrix, the true model parameter. Only available for simulation.

**Value**

A S3 object of class LSVAR, including

- est\_phi** estimated model parameter
- sparse.comp** Estimated sparse component
- lr.comp** Estimated low-rank component
- obj.val** Values of objective function
- rel.err** Relative errors compared with the true model parameters if available

**Examples**

```

n <- 300
p <- 20
try <- testVAR(n, p, struct = "LS", signal = 0.75, rank = 2,
                 singular_vals = c(1, 0.8))
data <- as.matrix(try$series)
lambda <- 0.1; mu <- 1
fit <- fista.LpS(data, lambda = lambda, mu = mu, x.true = try$model_param)
summary(fit, threshold = 0.2)

```

**Description**

Gradient function of quadratic loss

**Usage**

```
gradf.func(x, AtA, Atb)
```

**Arguments**

- |     |  |
|-----|--|
| x   | A vector, or matrix, indicating the model parameter                      |
| AtA | A p by p Gram matrix for corresponding design matrix A                   |
| Atb | An inner product for design matrix A and corresponding matrix (vector) b |

**Value**

Value of gradients

nuclear.pen	<i>Nuclear norm penalty for low-rank component</i>
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**Description**

Nuclear norm penalty for low-rank component

**Usage**

```
nuclear.pen(x, lambda)
```

**Arguments**

- |        |                  |
|--------|------------------|
| x      | Model parameter  |
| lambda | Tuning parameter |

**Value**

Value of nuclear norm penalty term

obj.func	<i>Objective function</i>
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**Description**

objective function, main loss function and penalties

**Usage**

```
obj.func(x.lr, x.sparse, A, b, lambda, mu)
```

**Arguments**

x.lr	low-rank component
x.sparse	sparse component
A	design matrix
b	correspond vector
lambda	a tuning parameter for sparse component
mu	a tuning parameter for low-rank component

**Value**

value of objective function

---

**plot\_network**

*plot sparse component for use igraph and network layout*

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**Description**

Plot a network to illustrate the estimated sparse component

**Usage**

```
plot_network(mat, threshold = 0.1)
```

**Arguments**

mat	a p by p matrix, indicating the sparse component
threshold	the threshold for presenting the edges in the network

**Value**

A network plot for the sparse component

**Examples**

```
set.seed(1)
est_mats <- matrix(rnorm(400, 0, 1), 20, 20)
plot_network(est_mats, threshold = 0.1)
```

`prox.nuclear.func`      *Proximal function with nuclear norm penalty updating*

## Description

Proximal function with nuclear norm

## Usage

```
prox.nuclear.func(w1, y, A, b, L, lambda, AtA, Atb)
```

## Arguments

w1	previously updated model parameter
y	updated model parameter
A	design matrix
b	correspond vector, or matrix
L	learning rate
lambda	tuning parameter for low-rank component
AtA	Gram matrix of design matrix A
Atb	inner product of design matrix A and correspond vector b

## Value

Value of proximal function with nuclear norm penalty

`prox.sparse.func`      *Proximal function with l1-norm penalty updating*

## Description

Proximal function with l1-norm

## Usage

```
prox.sparse.func(w1, y, A, b, L, lambda, AtA, Atb)
```

**Arguments**

w1	previously updated model parameter
y	updated model parameter
A	design matrix
b	correspond vector, or matrix
L	learning rate
lambda	tuning parameter for sparse component
AtA	Gram matrix of design matrix A
Atb	inner product of design matrix A and correspond vector b

**Value**

Value of proximal function with l1-norm penalty

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*Q.func*

*An auxiliary function in FISTA algorithm*

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**Description**

Auxiliary function for FISTA implementation

**Usage**

*Q.func(x, y, A, b, L, AtA, Atb)*

**Arguments**

x	Model parameter for previous update
y	Model parameter for updating
A	An n by p design matrix
b	A correspond vector, or matrix with size of n by 1 or n by p
L	Learning rate
AtA	Gram matrix for design matrix A
Atb	Inner product for design matrix A and correspond vector b

**Value**

Value of function Q

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**shrinkage***Shrinkage function for sparse soft-thresholding*

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**Description**

Shrinkage function for sparse soft-thresholding

**Usage**

```
shrinkage(y, tau)
```

**Arguments**

y	A matrix, or a vector for thresholding
tau	A positive number, threshold

**Value**

A thresholded matrix, or vector

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**shrinkage.lr***Shrinkage function for low-rank soft-thresholding*

---

**Description**

Shrinkage function for low-rank soft-thresholding

**Usage**

```
shrinkage.lr(y, tau)
```

**Arguments**

y	A matrix, or a vector for thresholding
tau	A positive number, threshold

**Value**

A thresholded matrix, or vector

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sparse.pen	<i>L1-norm penalty for sparse component</i>
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**Description**

L1-norm penalty for sparse component

**Usage**

```
sparse.pen(x, lambda)
```

**Arguments**

x	Model parameter
lambda	Tuning parameter

**Value**

Value of 11-norm penalty term

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summary.LSVAR	<i>Summary of LSVAR S3 class</i>
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**Description**

summary function for S3 class for the fitting result

**Usage**

```
## S3 method for class 'LSVAR'  
summary(object, threshold = 0.2, ...)
```

**Arguments**

object	the S3 class object of LSVAR
threshold	the threshold for sparse component visualization
...	not in use

**Value**

A series of summary for the S3 result

## Examples

```
n <- 300
p <- 20
try <- testVAR(n, p, struct = "LS", signal = 0.75, rank = 2,
               singular_vals = c(1, 0.8))
data <- as.matrix(try$series)
lambda <- 0.1; mu <- 1
fit <- fista.LpS(data, lambda = lambda, mu = mu, x.true = try$model_param)
summary(fit, threshold = 0.2)
```

**testVAR**

*Function to generate a VAR process*

## Description

A function to generate synthetic time series process based on the given structure

## Usage

```
testVAR(
  n,
  p,
  struct = c("sparse", "low rank", "LS")[1],
  sp_density = 0.1,
  signal = NULL,
  rank = NULL,
  singular_vals,
  spectral_radius = 0.9,
  sigma = NULL,
  skip = 50,
  seed = 1
)
```

## Arguments

<b>n</b>	the length of time series
<b>p</b>	the number of multivariate time series
<b>struct</b>	a character string indicating the structure of the transition matrix, here are three options: sparse, low rank and LS (low rank plus sparse)
<b>sp_density</b>	a numeric value, indicating the sparsity density of sparse components, default is 0.1
<b>signal</b>	a numeric value, indicating the magnitude of transition matrix
<b>rank</b>	a positive integer, the rank for low rank component
<b>singular_vals</b>	a numeric vector, indicating the singular values for the low rank component, the length of singular value must equal to the rank

spectral_radius	a numeric value, controlling the stability of the process, default is 0.9
sigma	a numeric matrix, indicating the covariance matrix of noise term
skip	a numeric value, indicating the number of skipped time points in the beginning of the process
seed	an integer, indicating the seed for random seed.

### Value

A list object, including

- series** the generated time series
- noise** the noise term
- model\_param** true transition matrix

### Examples

```
n <- 300; p <- 15
signal <- 0.75
rank <- 3
singular_vals <- c(1, 0.75, 0.5)
try <- testVAR(n, p, struct = "LS", signal = signal, rank = rank,
               singular_vals = singular_vals)
data <- as.matrix(try$series)
```

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