## Package 'drape'

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Title Doubly Robust Average Partial Effects

Version 0.0.2

**Description** Doubly robust average partial effect estimation. This implementation contains methods for adding additional smoothness to plug-in regression procedures and for estimating score functions using smoothing splines. Details of the method can be found in Harvey Klyne and Rajen D. Shah (2023) <doi:10.48550/arXiv.2308.09207>.

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## Index

basis_poly	Estimate the score function of the d'th covariate using a polynomial
	basis.

## Description

Computes the score function estimate when rho(X) is assumed to lie within the span of the polynomial basis of X.

## Usage

basis\_poly(X, d, degree = 2, lambda = NULL)

## Arguments

Х	matrix of covariates.
d	integer index of covariate of interest.
degree	maximum degree of polynomial terms.
lambda	optional scalar penalty, if "NULL" chosen via cross-validation.

#### Value

list containing the estimated score function "rho", which takes matrix input and yields a vector of score estimates.

#### compare

#### Examples

```
set.seed(0)
X <- matrix(stats::rnorm(200), ncol=4)
bs <- basis_poly(X=X, d=1, degree=2)
bs$rho(X)</pre>
```

compare	Generate simulation data and evaluate estimators, with sample split-
	ting.

#### Description

Generate simulation data and evaluate estimators, with sample splitting.

#### Usage

compare(n, ex\_setting, f\_setting, nfold = 5)

#### Arguments

n	integer number of samples. For "401k" ex_setting this is ignored and the whole data set is used.
ex_setting	string "normal", "mixture2", "mixture3", "logistic", "t4", "401k".
f_setting	string "plm", "additive", "interaction".
nfold	integer number of cross-validation folds.

#### Value

list containing estimates, standard error estimates, and sample theta (for debugging).

compare_evaluate	Evaluate estimators by training nuisance functions on training set and
	evaluating them on test set.

## Description

Evaluate estimators by training nuisance functions on training set and evaluating them on test set.

#### Usage

```
compare_evaluate(train, test, ex_setting, f_setting, regression, sm_bw_out)
```

#### Arguments

train	list containing vector of responses y and matrix of predictors $X = (x,z)$ .
test	list containing vector of responses y and matrix of predictors $X = (x,z)$ .
ex_setting	string "normal", "mixture2", "mixture3", "logistic", "t4", "401k".
f_setting	string "plm", "additive", "interaction".
regression	Optional fitted regression.
sm_bw_out	Output of cv_resmooth.

## Value

list containing f, df, and score estimates evaluated on the test set.

Generate simulation data and evaluate OLS estimator.

## Description

Generate simulation data and evaluate OLS estimator.

#### Usage

compare\_lm(n, ex\_setting, f\_setting)

## Arguments

n	integer number of samples. For "401k" ex_setting this is ignored and the whole data set is used.
ex_setting	string "normal", "mixture2", "mixture3", "logistic", "t4", "401k".
f_setting	string "plm", "additive", "interaction".

#### Value

list containing estimate, standard error estimate, and sample theta (for debugging).

compare\_partially\_linear

Generate simulation data and evaluate partially linear estimator.

#### Description

Generate simulation data and evaluate partially linear estimator.

#### Usage

compare\_partially\_linear(n, ex\_setting, f\_setting)

#### Arguments

n	integer number of samples. For "401k" ex_setting this is ignored and the whole
	data set is used.
ex_setting	string "normal", "mixture2", "mixture3", "logistic", "t4", "401k".
f_setting	string "plm", "additive", "interaction".

## Value

list containing estimate, standard error estimate, and sample theta (for debugging).

compare\_rothenhausler Generate simulation data and evaluate Rothenhausler estimator.

## Description

Generate simulation data and evaluate Rothenhausler estimator.

#### Usage

```
compare_rothenhausler(n, ex_setting, f_setting)
```

#### Arguments

n	integer number of samples. For "401k" ex_setting this is ignored and the whole
	data set is used.
ex_setting	string "normal", "mixture2", "mixture3", "logistic", "t4", "401k".
f_setting	string "plm", "additive", "interaction".

#### Value

list containing estimate, standard error estimate, and sample theta (for debugging).

cv\_resmooth

#### Description

Picks the largest resmoothing bandwidth achieving a cross-validation score within some specified tolerance of the original regression.

#### Usage

```
cv_resmooth(
    X,
    y,
    d = 1,
    regression,
    tol = 2,
    prefit = FALSE,
    foldid = NULL,
    bw = exp(seq(-5, 2, 0.2))/(2 * sqrt(3)) * stats::sd(X[, d]),
    nfolds = 5L,
    n_points = 101,
    sd_trim = 5
)
```

## Arguments

Х	matrix of covariates.
У	vector of responses.
d	integer index of covariate to be smoothed along.
regression	If prefit = FALSE this is a function which takes input data of the form $(X,y)$ , and returns a prediction function. This prediction function itself accepts matrix input same width as X, and returns a vector of y-predictions, and optionally a vector of derivative predictions. If prefit = TRUE then this is a list of length nfolds with each entry containing a component "fit" consisting of a prediction function taking matrix input and returning a vector.
tol	vector of tolerances controlling the degree of permissible cross-validation error increase. Larger values lead to a larger amount of smoothing being selected.
prefit	boolean signifying if the regressions are already fit to the training data for each fold.
foldid	optional vector with components in 1:nfolds indicating the folds in which each observation fell. Overwrites nfolds.
bw	vector of bandwidths for the Gaussian resmoothing kernel.
nfolds	integer number of cross-validation folds.
n_points	integer number of gridpoints to be used for convolution.
sd_trim	float number of standard deviations at which to trim the Gaussian distribution.

#### cv\_spline\_score

#### Value

list. Vector "bw" of bandwidths used. Vectors "cv" of cross-validation scores and numeric "cv\_unsm" for the cross-validation without any smoothing. Vector "bw\_opt\_inds" for the indices of the selected bandwidths under various tolerances. Vector "bw\_opt" for the corresponding bandwidths.

#### Examples

```
X <- matrix(stats::rnorm(200), ncol=2)
y <- X[,1] + sin(X[,2]) + 0.5 * stats::rnorm(nrow(X))
reg <- function(X,y){
    df <- data.frame(y,X)
    colnames(df) <- c("y", "X1", "X2")
    lm1 <- stats::lm(y~X1+sin(X2), data=df)
    fit <- function(newX){
        newdf = data.frame(newX)
        colnames(newdf) <- c("X1", "X2")
        return(as.vector(stats::predict(lm1, newdata=newdf))))
    return(list("fit"=fit))
}
cv_resmooth(X=X, y=y, d=2, regression=reg, tol = c(0.5, 1, 2))</pre>
```

cv\_spline\_score *K*-fold cross-validation for spline\_score.

#### Description

K-fold cross-validation for spline\_score.

#### Usage

```
cv_spline_score(x, df = 2:15, nfolds = 5L, tol = 0.001, nmax = NULL)
```

#### Arguments

х	vector of datapoints
df	vector of smoothing parameters for the non-parametric score estimator, corre- sponding to the effective degrees of freedom for a smoothing spline.
nfolds	integer number of cross-validation folds.
tol	numeric tolerance, minimum distance between neighbouring points, to avoid singularities.
nmax	if specified, overrides tol as maximal number of unique points.

#### Value

list of 5 elements: df vector, cv vector of corresponding cross-validation scores, se vector of standard error estimates, df\_min cross-validation minimiser, df\_1se largest smoothing parameter within CV score within one standard error of df\_min.

#### Examples

```
set.seed(0)
x <- stats::rt(100, df=4)
cv_spline_score(x)
x <- stats::rlogis(500)
cvspl <- cv_spline_score(x)
cvspl$df_min</pre>
```

*Estimate the doubly-robust average partial effect estimate of X on Y, in the presence of Z.* 

## Description

Estimate the doubly-robust average partial effect estimate of X on Y, in the presence of Z.

#### Usage

```
drape(
    y,
    x,
    z,
    response_regression,
    predictor_regression,
    resmooth_bw = NULL,
    spline_df = NULL,
    nfolds = 5L,
    foldid = NULL,
    verbose = FALSE
)
```

#### Arguments

У	vector of responses.	
x	vector of the predictor of interest.	
z	matrix of additional predictors.	
response_regres	sion	
	function which takes input data of the form $(X,y)$ , where X=cbind $(x,z)$ , and returns a prediction function f:X -> y and optionally a similar derivative estimation function (in this case no resmoothing is done).	
predictor_regression		
	function which takes input data of the form (z,x), and returns a prediction function m:z -> x.	
resmooth_bw	optional numeric to be used as resmoothing bandwidth, otherwise chosen via cross-validation. Only used if response_regression doesn't predict derivatives.	

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#### fit\_lasso\_poly

spline_df	optional double, a smoothing parameter for the unconditional spline score esti- mator, corresponding to the effective degrees of freedom for a smoothing spline. If NULL, chosen via cross-validation.
nfolds	integer, number of sample-splits. If set to one, then all data is used for both training and evaluation.
foldid	optional vector with components in 1:nfolds indicating the folds in which each observation fell. Overwrites nfolds.
verbose	boolean controlling level of information outputted.

#### Value

list containing the average partial effect estimate and the corresponding standard error estimate. If verbose=TRUE, additionally contains variables used in computations.

#### Examples

```
set.seed(0)
data <- simulate_data(200, "normal", "plm")</pre>
response_regression <- function(X,y){</pre>
    df <- data.frame(y,X)</pre>
    colnames(df) <- c("y", paste0("X", 1:10))</pre>
    lm1 <- stats::lm(y~X1+sin(X2), data=df)</pre>
    fit <- function(newX){</pre>
        newdf <- data.frame(newX)</pre>
        colnames(newdf) <- paste0("X", 1:10)</pre>
        return(as.vector(stats::predict(lm1, newdata=newdf)))}
    return(list("fit"=fit))
}
predictor_regression <- function(z,x){</pre>
    df <- data.frame(x,z)</pre>
    colnames(df) <- c("x", paste0("Z", 1:9))</pre>
    lm1 <- stats::lm(x~Z1+Z2, data=df)</pre>
    fit <- function(newz){</pre>
        newdf <- data.frame(newz)</pre>
        colnames(newdf) <- paste0("Z", 1:9)</pre>
         return(as.vector(stats::predict(lm1, newdata=newdf)))}
    return(list("fit"=fit))
}
drape(data$y, data$x, data$z, response_regression, predictor_regression, nfolds=2)
```

fit\_lasso\_poly Fit a lasso regression using quadratic polynomial basis, with interactions.

#### Description

Compute regression function and derivative estimates based on polynomial basis lasso with penalty parameter chosen by cross validation (CV).

#### Usage

fit\_lasso\_poly(X, y, degree, lambda = NULL)

#### Arguments

Х	matrix of covariates.
У	vector of responses.
degree	maximum degree of polynomial terms.
lambda	optional scalar tuning parameter, if "NULL" chosen via cross-validation.

#### Value

List containing: A function "fit" which takes matrix input of the same width as X, and returns a vector of y-predictions. A scalar "lambda" the tuning parameter.

fit_xgboos	t
------------	---

Fit pre-tuned XGBoost regression for use in simulations.

#### Description

Fit pre-tuned XGBoost regression for use in simulations.

#### Usage

fit\_xgboost(X, y, params, derivative = FALSE)

#### Arguments

Х	matrix of covariates.
У	vector of responses.
params	XGBoost hyperparameters.
derivative	logical determining if numerical difference derivative estimate (wrt the first pre- dictor) should also be returned.

#### Value

list containing a function "fit" which takes matrix input of the same width as X, and returns a vector of predictions. Optionally the list also contains a function "deriv\_fit" for numerical difference derivative estimates.

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 $MC\_sums$ 

#### Description

Compute sums of a Monte Carlo vector for use in resmoothing.

#### Usage

MC\_sums(a, n, nMC, nbw)

#### Arguments

а	vector of length (n x nMC x nbw).
n	integer.
nMC	integer.
nbw	integer.

#### Value

list with nbw elements. The j'th element of which is a vector of length n, the i'th element being the sum of the  $(((j-1)n + (i-1)) \times nMC + 1)$  to  $(((j-1)n + i) \times nMC)$  elements of a inclusive.

mixture_score	Population score function for the symmetric mixture two Gaussian
	random variables.

#### Description

Population score function for the symmetric mixture two Gaussian random variables.

#### Usage

```
mixture_score(x, sd)
```

#### Arguments

Х	vector of observations.
sd	standard deviation of each Gaussian.

#### Value

vector of length n

new\_X

Generate a matrix of covariates for use in resmoothing, in which the d'th column of X is translated successively by the Kronecker product of bw and MC\_variates.

#### Description

Generate a matrix of covariates for use in resmoothing, in which the d'th column of X is translated successively by the Kronecker product of bw and MC\_variates.

#### Usage

new\_X(X, d, MC\_variates, bw)

#### Arguments

Х	matrix of covariates.
d	integer index of covariate to be smoothed along.
MC_variates	vector of standard Gaussian rvs.
bw	vector of bandwidths for the Gaussian kernel.

#### Value

matrix with ncol(X) columns and (nrow(X)length(MC\_variates) length(bw)) rows.

ng_pseudo_response	Generate pseudo responses as in Ng 1994 to enable univariate score
	estimation by standard smoothing spline regression.

#### Description

Pseudo responses should be regarded as a computational tool, not as an estimate of the score itself.

#### Usage

ng\_pseudo\_response(x, w = rep(1, length(x)))

#### Arguments

х	vector of covariates.
W	vector of weights.

#### Value

A vector of score estimates.

#### partially\_linear

#### Examples

```
x <- seq(-3,3, length.out=50)
ng_pseudo_response(x)</pre>
```

partially_linear	Fit a doubly-robust partially linear regression using the DoubleML
	package and pre-tuned XGBoost regressions, for use in simulations.

#### Description

Fit a doubly-robust partially linear regression using the DoubleML package and pre-tuned XGBoost regressions, for use in simulations.

#### Usage

partially\_linear(X, y, g\_params, m\_params)

#### Arguments

Х	matrix of covariates.
У	vector of responses.
g_params	XGBoost hyperparameters for partially linear regression of y on X.
m_params	XGBoost hyperparameters for predictor regression of the first column of X on
	the others.

#### Value

List containing the linear parameter estimate and the corresponding standard error estimate.

resmooth	re	smo	otl	h
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Resmooth the predictions of a fitted model

#### Description

Smooth the predictions of a fitted model by convolving them with a Gaussian kernel along the d'th covariate.

#### Usage

```
resmooth(
   fit,
   X,
   d = 1,
   bw = exp(seq(-1, 1))/(2 * sqrt(3)) * stats::sd(X[, d]),
   n_points = 101,
   sd_trim = 5
)
```

rmixture

#### Arguments

fit a <sub>l</sub>	prediction function taking matrix input and returning a vector.
X ma	atrix of covariates.
d int	teger index of covariate to be smoothed along.
bw ve	ctor of bandwidths for the Gaussian kernel.
n_points inf	teger number of gridpoints to be used for convolution.
sd_trim flo	bat number of standard deviations at which to trim the Gaussian distribution.

#### Value

List with the following elements. A list "pred" of the same length as "bw". Each element is a vector of predictions which are smooth with respect to the dth column of X, with smoothness corresponding to the respective element of "bw". A similar list "deriv" of corresponding vectors of first derivatives. Vectors "gridpoints" and "prob\_weights" of equally spaced gridpoints and corresponding normal density weights. Vector "bw" of bandwidths used.

#### Examples

```
# Single bandwidth
X <- matrix(seq(-2,2,by=0.05))
fit <- function(Y){1*(rowMeans(Y)<0)}
sm <- resmooth(fit=fit, X=X, d=1, bw=0.2)
sm$pred[[1]]
# Multiple bandwidths simultaneously
X <- matrix(stats::rnorm(200), ncol=2)
y <- X[,1] + sin(X[,2]) + 0.5 * stats::rnorm(nrow(X))
df <- data.frame(y,X)
lm1 <- stats::lm(y~X1+sin(X2), data=df)
fit <- function(Y){as.vector(stats::predict(lm1, newdata=data.frame(Y)))}
resmooth(fit=fit, X=X, d=2)</pre>
```

rmixture

Symmetric mixture two Gaussian random variables.

#### Description

The resulting distribution is mean zero, variance one.  $X \sim N(-sqrt(1-sd^2), sd^2)$  wp 0.5,  $N(sqrt(1-sd^2), sd^2)$ , wp 0.5.

#### Usage

rmixture(n, sd)

#### Arguments

n	number of observations.
sd	standard deviation of each Gaussian.

#### rothenhausler\_basis

#### Value

vector of length n

rothenhausler\_basis Generate the modified quadratic basis of Rothenhausler and Yu.

#### Description

Generate the modified quadratic basis of Rothenhausler and Yu.

#### Usage

rothenhausler\_basis(X)

## Arguments X

matrix of covariates.

#### Value

List containing the modified basis matrices for regression and derivative estimation.

rothenhausler_yu	Estimate the average partial effect of using the debiased lasso method
	of Rothenhausler and Yu, using pre-tuned lasso penalties, for use in
	simulations.

#### Description

Estimate the average partial effect of using the debiased lasso method of Rothenhausler and Yu, using pre-tuned lasso penalties, for use in simulations.

#### Usage

```
rothenhausler_yu(X, y, f_lambda, m_lambda)
```

#### Arguments

Х	matrix of covariates.
У	vector of responses.
f_lambda	lasso penalty for regression of y on X.
m_lambda	lasso penalty for predictor regression of the first column of X on the others.

#### Value

List containing the linear parameter estimate and the corresponding standard error estimate.

simulate\_data

#### Description

If ex\_setting = "401k" then 401k data set is used for (X,Z). Otherwise:

 $Z N_9(0, \Sigma),$ 

where  $\Sigma_{jj} = 1$ ,  $\Sigma_{jk} = 0.5$  for all j not equal to k.

X = m(Z) + s(Z) \* ex,

where m and s are step functions of  $z_1$  and  $z_3$  respectively.

$$Y = f(X, Z) + N(0, 1).$$

#### Usage

```
simulate_data(n, ex_setting, f_setting)
```

#### Arguments

n	integer number of samples. For "401k" ex_setting this is ignored and the whole data set is used.
ex_setting	string "normal", "mixture2", "mixture3", "logistic", "t4", "401k".
f_setting	string "plm", "additive", "interaction".

#### Value

list containing y, x, z. Additionally contains the population nuisance parameters evaluated on the data, and the sample version of the average partial effect.

## Examples

simulate\_data(100, "normal", "plm")

sort\_bin

#### Description

Sort and bin x within a specified tolerance, using hist().

#### Usage

sort\_bin(x, tol = 1e-05, nmax = NULL)

#### Arguments

х	vector of covariates.
tol	numeric tolerance, minimum distance between neighbouring points, to avoid singularities.
nmax	if specified, overrides tol as maximal number of unique points.

### Value

list with three elements. x\_sort is sorted and binned x, w is a vector of weights corresponding to the frequency of each bin, order is a vector specifying the ordering of x into the binned values sort\_x.

spline_score	Univariate score estimation via the smoothing spline method of Cox
	1985 and Ng 1994.

### Description

Univariate score estimation via the smoothing spline method of Cox 1985 and Ng 1994.

#### Usage

spline\_score(x, df = 5, tol = 0.001, nmax = NULL)

#### Arguments

х	vector of datapoints
df	vector of smoothing parameters for the non-parametric score estimator, corre- sponding to the effective degrees of freedom for a smoothing spline.
tol	numeric tolerance, minimum distance between neighbouring points, to avoid singularities.
nmax	if specified, overrides tol as maximal number of unique points.

#### Value

score function "rho" and derivative "drho", which take vector input and yield a vector of score estimates corresponding to each df (in a list if there are multiple df values). Also output the vector "df".

#### Examples

```
# Single bandwidth
x <- stats::rlogis(100)
spl <- spline_score(x, df=6)
spl$rho(x)
spl$drho(x)
# Multiple bandwidths simultaneously
x <- stats::rt(n=100, df=4)
spl <- spline_score(x, df=c(2,5,10))
spl$rho(x)</pre>
```

z_correlated_normal	Generate n copies of $Z^{\sim}N_p(0,\Sigma)$ , where $\Sigma_j = 1$ , $\Sigma_j k = corr$
	for all j not equal to k.

#### Description

Generate n copies of  $Z N_p(0, \Sigma)$ , where  $\Sigma_{jj} = 1, \Sigma_{jk} = \text{corr for all } j$  not equal to k.

#### Usage

z\_correlated\_normal(n, p, corr)

#### Arguments

n	integer number of samples.
р	integer number of dimensions.
corr	float correlation in (-1,1).

#### Value

n by p matrix.

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