Package 'ghypernet'

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Type Package

Title Fit and Simulate Generalised Hypergeometric Ensembles of Graphs

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Description Provides functions for model fitting and selection of generalised hypergeometric ensembles of random graphs (gHypEG). To learn how to use it, check the vignettes for a quick tutorial.

Please reference its use as Casiraghi, G., Nanumyan, V. (2019) <doi:10.5281/zenodo.2555300>

together with those relevant references from the one listed below.

The package is based on the research developed at the Chair of Systems Design, ETH Zurich.

Casiraghi, G., Nanumyan, V., Scholtes, I., Schweitzer, F. (2016) <arXiv:1607.02441>.

Casiraghi, G., Nanumyan, V., Scholtes, I., Schweitzer, F. (2017) <doi:10.1007/978-3-319-67256-4_11>.

Casiraghi, G., (2017) <arXiv:1702.02048>

Brandenberger, L., Casir-

aghi, G., Nanumyan, V., Schweitzer, F. (2019) <doi:10.1145/3341161.3342926> Casiraghi, G. (2019) <doi:10.1007/s41109-019-0241-1>. Casiraghi, G., Nanumyan, V. (2021) <doi:10.1038/s41598-021-92519-y>.

Casiraghi, G. (2021) <doi:10.1088/2632-072X/ac0493>.

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adj2el

Maps adjacency matrix to edgelist

Description

Maps adjacency matrix to edgelist

Usage

```
adj2el(adj, directed = TRUE)
```

Arguments

adj	matrix, the adjacency matrix
directed	boolean, is the graph directed?

Value

a dataframe containing the edgelist

Examples

data(contacts.adj)
el <- adj2el(contacts.adj)</pre>

adj_karate

Description

Weighted adjacency matrix reporting interactions among 34 nodes.

Usage

adj_karate

Format

a 34x34 matrix

Source

package 'igraphdata'

as.ghype

Map list to ghype object

Description

Manually map a list to a ghype object

Usage

```
as.ghype(object, ...)
## S3 method for class 'list'
as.ghype(object, ...)
## S3 method for class 'nrm'
as.ghype(object, ...)
```

Arguments

object	list object to map to ghype.
	additional arguments to be passed to logl function.

Value

an object of class "ghype"

bccm

Methods (by class)

- list: Map list to ghype
- nrm: Map list to ghype

Examples

bccm

Fitting bccm models

Description

bccm is used to fit a block-constrained configuration model.

Usage

```
bccm(
  adj,
  labels,
  directed = NULL,
  selfloops = NULL,
  directedBlocks = FALSE,
  homophily = FALSE,
  inBlockOnly = FALSE,
  xi = NULL,
  regular = FALSE,
  ...
)
## S3 method for class 'bccm'
```

```
print(x, suppressCall = FALSE, ...)
```

Arguments

adj	the adjacency matrix of the graph.
labels	vector or list. contains the vertex labels to generate the blocks in the bccm. In the case of bipartite graphs should be a list of two vectors, the first one with row labels and the second one with column labels.
directed	a boolean argument specifying whether the graph is directed or not.
selfloops	boolean argument specifying whether the model should incorporate selfloops.

directedBlocks	boolean argument specifying whether the model should incorporate directed blocks. Default to FALSE.
homophily	boolean argument specifying whether the model should fit only homophily blocks. Default to FALSE.
inBlockOnly	boolean argument specifying whether the model should fit only blocks over the diagonal. Default to FALSE.
xi	an optional matrix defining the combinatorial matrix of the model.
regular	optional boolean, fit regular gnp model? if not specified chosen through lr.test.
	optional arguments to print or plot methods.
x	object of class 'bccm'
suppressCall	logical, indicating whether to print the call that generated x

Value

bccm returns an object of class 'bccm' and 'ghype'. 'bccm' objects expand 'ghype' objects incorporating the parameter estimates.

Methods (by generic)

• print: Print method for elements of class 'bccm'.

See Also

bccm

Examples

```
data("vertexlabels","adj_karate")
blockmodel <- bccm(adj = adj_karate, labels = vertexlabels, directed = FALSE, selfloops = FALSE)
data('adj_karate')
data('vertexlabels')
bcc.model <- bccm(adj_karate, labels=vertexlabels, directed=FALSE, selfloops=FALSE)
print(bcc.model)</pre>
```

BootstrapProperty BootstrapProperty computes igraph analytics function on ensemble

Description

BootstrapProperty computes igraph analytics function on ensemble

BootstrapProperty

Usage

```
BootstrapProperty(
  graph,
  property,
  directed,
  selfloops,
  nsamples = 1000,
  xi = NULL,
  omega = NULL,
  model = NULL,
  m = NULL,
  seed = NULL,
  ...
)
```

Arguments

graph	igraph graph
property	igraph function that can be applied to a graph
directed	boolean
selfloops	boolean
nsamples	number of samples from ensemble. defaults to 1000
xi	matrix, default null
omega	matrix, default null
model	ghype model from which to extract xi and omega, default to null
m	int, number of edges to sample from model
seed	seed
	other parameters to pass to 'property'

Value

vector of length nsamples

Examples

```
library(igraph)
data('adj_karate')
result <- BootstrapProperty(adj_karate, page_rank, FALSE, FALSE, nsamples=10)</pre>
```

```
checkGraphtype
```

Description

Returns TRUE if the supplied object graph is an adjacency matrix. Returns FALSE if the provided object is an edgelist. The function checks whether the edgelist conforms to our standards (sender, target, edgecount).

Usage

checkGraphtype(graph)

Arguments

graph A graph adjacency matrix or an edgelist.

Value

TRUE or FALSE. Returns TRUE if the provided object graph is an adjacency matrix.

coef.nrm

Extraction method for coefficients of models of class 'nrm'.

Description

Extraction method for coefficients of models of class 'nrm'.

Usage

S3 method for class 'nrm'
coef(object, ...)

Arguments

object	object of class 'nrm'.
	optional arguments to print methods.

Value

coefficients of nrm model.

Author(s)

Giona Casiraghi

compute_xi

See Also

nrm

compute_xi

Auxiliary function. Computes combinatorial matrix.

Description

Combinatorial matrix computed according to soft configuration model or 'regular' gnp model.

Usage

compute_xi(adj, directed, selfloops, regular = FALSE)
ComputeXi(adj, directed, selfloops, regular = FALSE)

Arguments

adj	adjacency matrix
directed	boolean, whether the model is for a directed network
selfloops	boolean, whether the model contains selfloops
regular	boolean. Is the combinatorial matrix computed for configuration model or for regular gnp model? default FALSE.

Value

combinatorial matrix

Examples

```
data('adj_karate')
xi = compute_xi(adj_karate, directed = FALSE, selfloops = FALSE)
```

conf.test

Description

Likelihood ratio test for gnp vs configuration model.

Usage

```
conf.test(
  graph,
  directed,
  selfloops,
  nempirical = NULL,
  parallel = NULL,
  seed = NULL
)
```

Arguments

graph	adjacency matrix or igraph graph
directed	a boolean argument specifying whether object is directed or not.
selfloops	a boolean argument specifying whether the model should incorporate selfloops.
nempirical	optional, number of graphs to sample from null distribution for empirical distribution.
parallel	optional, number of cores to use or boolean for parallel computation. If passed TRUE uses all cores-1, else uses the number of cores passed. If none passed performed not in parallel.
seed	optional integer

Value

p-value of test.

Examples

```
data("adj_karate")
conf.test(graph = adj_karate, directed = FALSE, selfloops = FALSE, seed=123)
```

contacts.adj

Description

contacts.adj: contains the adjacency matrix of 327 x 327 highschool students.

Usage

data(highschool.predictors)

Format

327x327 adjacency matrix

Source

http://www.sociopatterns.org

References

Casiraghi, G. Multiplex Network Regression: How do relations drive interactions? 15 (2017).

Mastrandrea, R., Fournet, J. & Barrat, A. Contact patterns in a high school: A comparison between data collected using wearable sensors, contact diaries and friendship surveys. PLoS One 10, 1–26 (2015).

cospons_mat

Swiss MPs network adjacency matrix

Description

cospons_mat: contains the adjacency matrix of 163 x 163 MPs.

Usage

data(cospons_mat)

Format

163x163 adjacency matrix

coxsnellR2

Description

Computes Cox and Snell pseudo R-squared for nrm models.

Usage

```
coxsnellR2(mod0, mod1, m)
```

Arguments

mod0	nrm null model
mod1	nrm alternative model
m	number of edges

Value

Cox and Snell pseudo R-squared

Author(s)

GC

CreateIgGraphs Convert a list of adjacency matrices to a list of igraph graphs.

Description

Convert a list of adjacency matrices to a list of igraph graphs.

Usage

```
CreateIgGraphs(adjlist, directed, selfloops, weighted = NULL)
```

Arguments

adjlist	a list of adjacency matrices
directed	a boolean argument specifying whether object is directed or not.
selfloops	a boolean argument specifying whether the model should incorporate selfloops.
weighted	boolean, generate weighted graphs?

create_predictors

Value

list of igraph graphs.

Examples

```
data('adj_karate')
adj_list <- list(adj_karate)
glist <- CreateIgGraphs(adj_list, FALSE, FALSE)</pre>
```

create_predictors Create a nrmpredictor object from passed argument

Description

Create a nrmpredictor object from passed argument

Usage

```
create_predictors(predictors, ...)
createPredictors(predictors, ...)
```

Arguments

predictors	the dataframe or list of predictors for to apply nrm model selection
	additional parameters passed to the different methods (currently disabled)

Value

nested list of nrmpredictor class

Examples

```
data('highschool.predictors')
predictors <- create_predictors(highschool.predictors)</pre>
```

create_predictors.list

Description

Create a nrmpredictor object from list

Usage

```
## S3 method for class 'list'
create_predictors(predictors, ...)
```

Arguments

predictors	the dataframe or list of predictors for to apply nrm model selection
	additional parameters used to creating the predictor object (currently disabled)

Value

nested list of nrmpredictor class

Examples

```
data('highschool.predictors')
predictors <- create_predictors(highschool.predictors)</pre>
```

dt

Swiss MPs attribute data frame.

Description

dt: contains different attributes of the 163 MPs, such as their names, their party affiliation (variable: *party*), their parliamentary group affiliation (variable: *parlGroup*), the Canton (or state) they represent (variable: *canton*), their gender (variable: *gender*) and date of birth (variable: *birthdate*).

Usage

data(dt)

Format

163x8 data.frame

dtcommittee

Description

dtcommittee: a list of committees each MP was part of during their stay in parliament

Usage

data(dtcommittee)

Format

163x2 data.frame

el2adj

Maps edgelist to adjacency matrix

Description

Maps edgelist to adjacency matrix

Usage

el2adj(el, nodes = NULL)

Arguments

el	dataframe containing a (weighted) edgelist. Column 1 is the sender, column 2 is the receiver, column 3 the number of edges.
nodes	optional vector containing all node names in case disconnected nodes should be included.

Value

the (weighted) adjacency matrix corresponding the edgelist passed

extract.nrm.cluster

Extract details from statistical models for table construction. The function has methods for a range of statistical models.

Description

Extract details from statistical models for table construction. The function has methods for a range of statistical models.

Usage

extract.nrm.cluster(model, ...)

Arguments

model	A statistical model object.	
	Custom parameters, which are handed over to subroutines. The arguments are	
	usually passed to the summary function, but in some cases to other functions.	

Value

The function returns a texreg object.

Author(s)

L. Brandenberger, G. Casiraghi

FitOmega

Fit propensity matrix for full model

Description

(auxiliary function)

Usage

```
FitOmega(adj, xi, directed, selfloops)
```

Arguments

adj	adjacency matrix
xi	combinatorial matrix
directed	boolean
selfloops	boolean

get_zero_dummy

Value

propensity matrix

Examples

```
data(adj_karate)
xi <- compute_xi(adj_karate, FALSE, FALSE)
FitOmega(adj_karate, xi, FALSE, FALSE)</pre>
```

get_zero_dummy

Create a dummy variable to encode zero values of another variable.

Description

Use this to substitute zero-values in your nrm values. Zero values in the predictors are recognized in the gHypEG regression as structural zeroes. To ensure this does not happen, please recode your zero-values in all your predictors, ideally using a dummy variable fitting an optimal value for the zeroes. This function takes a predictor that needs to be recoded and returns a list containing two matrices. The first one contains the original predictor recoded such that all zero values are 1 (and thus do not impact the model). The second one consist of a matrix with 1 where the original predictor was different from 0, and 'zero_values' where the original predictor was 0. If 'zero_values' is not specified, it is fixed to e to simplify the interpretation of the results.

Usage

get_zero_dummy(dat, name = NULL, zero_values = NULL)

Arguments

dat	matrix, the predictor for which the zero values should be recoded.
name	optional character, the name of the predictor to create a named list
zero_values	optional numeric, the value to assign to the zero values of 'dat' in the dummy variable. It defaults to e to simplify the interpretation of the results.

Value

a possibly named list of two matrices. The first one is the recoded version of 'dat' where all zeroes are changed to 1. The second is the dummy variable such that dummy[dat==0] <- zero_values and 1 otherwise.

See Also

reciprocity_stat or sharedPartner_stat

ghype

Description

ghype is used to fit gHypEG models when the propensity matrix is known. It can be used to estimate a null model (soft configuration model), or the benchmark 'full-model', where the propensity matrix is fitted such that the expected graph from the fitted model is the one passed to the function.

Usage

```
ghype(
  graph,
  directed,
  selfloops,
  xi = NULL,
  omega = NULL,
  unbiased = FALSE,
  regular = FALSE,
  . . .
)
## S3 method for class 'matrix'
ghype(
  graph,
  directed,
  selfloops,
  xi = NULL,
  omega = NULL,
  unbiased = FALSE,
  regular = FALSE,
  . . .
)
## Default S3 method:
ghype(
  graph,
 directed,
  selfloops,
  xi = NULL,
  omega = NULL,
  unbiased = FALSE,
  regular = FALSE,
)
## S3 method for class 'igraph'
```

ghype

```
ghype(
  graph,
  directed,
  selfloops,
  xi = NULL,
  omega = NULL,
  unbiased = FALSE,
  regular = FALSE,
  ...
)
## S3 method for class 'ghype'
print(x, suppressCall = FALSE, ...)
```

Arguments

graph	either an adjacency matrix or an igraph graph.
directed	a boolean argument specifying whether graph is directed or not.
selfloops	a boolean argument specifying whether the model should incorporate selfloops.
xi	an optional matrix defining the combinatorial matrix of the model.
omega	an optional matrix defining the propensity matrix of the model.
unbiased	a boolean argument specifying whether to model the hypergeometric ensemble (no propensity), defaults to FALSE.
regular	a boolean argument specifying whether to model the 'gnp' ensemble (no xi), defaults to FALSE.
	further arguments passed to or from other methods.
х	ghype model
suppressCall	boolean, suppress print of the call

Value

ghype return an object of class "ghype".

Methods (by class)

- matrix: Fitting ghype models from an adjacency matrix
- default: Generating a ghype model from given xi and omega
- igraph: Fitting ghype models from an igraph graph
- ghype: Print method for ghype object.

Examples

```
data("adj_karate")
fullmodel <- ghype(graph = adj_karate, directed = FALSE, selfloops = FALSE, unbiased = FALSE)</pre>
```

data('adj_karate')

```
model <- scm(adj_karate, FALSE, FALSE)
print(model)</pre>
```

gof.test

Perform a goodness-of-fit test

Description

Perform a goodness-of-fit test

Usage

```
gof.test(
  model,
  Beta = TRUE,
  nempirical = NULL,
  parallel = NULL,
  returnBeta = FALSE,
  seed = NULL
)
```

Arguments

model	ghype model to test	
Beta	boolean, whether to use empirical Beta distribution approximation. Default TRUE	
nempirical	optional scalar, number of replicates for empirical beta distribution.	
parallel	optional, number of cores to use or boolean for parallel computation. If passed TRUE uses all cores-1, else uses the number of cores passed. If none passed performed not in parallel.	
returnBeta	boolean, return estimated parameters of Beta distribution? Default FALSE.	
seed	scalar, seed for the empirical distribution.	

Value

p-value of test. If returnBeta=TRUE returns the p-value together with the parameters of the beta distribution.

Examples

```
data("adj_karate")
confmodel <- scm(graph = adj_karate, directed = FALSE, selfloops = FALSE)
gof.test(model = confmodel, seed = 123)</pre>
```

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highschool.multiplex Highschool contact network multiplex representation

Description

highschool.multiplex: list containing the adjacency matrix of 327 x 327 highschool students, and the adjacency matrices corresponding to the 5 predictors used in Casiraghi2017.

Usage

```
data(highschool.multiplex)
```

Format

6x327x327 list of adjacency matrices

Source

http://www.sociopatterns.org

References

Casiraghi, G. Multiplex Network Regression: How do relations drive interactions? 15 (2017).

Mastrandrea, R., Fournet, J. & Barrat, A. Contact patterns in a high school: A comparison between data collected using wearable sensors, contact diaries and friendship surveys. PLoS One 10, 1–26 (2015).

highschool.predictors Highschool contact network predictors

Description

highschool.predictors: list containing the adjacency matrices corresponding to the 5 predictors used in Casiraghi2017.

Usage

data(highschool.predictors)

Format

5x327x327 list of adjacency matrices

Source

http://www.sociopatterns.org

References

Casiraghi, G. Multiplex Network Regression: How do relations drive interactions? 15 (2017).

Mastrandrea, R., Fournet, J. & Barrat, A. Contact patterns in a high school: A comparison between data collected using wearable sensors, contact diaries and friendship surveys. PLoS One 10, 1–26 (2015).

homophily_stat Calculate homophily in multi-edge graphs.

Description

The function calculates homophily matrices. If you supply a categorical variable (factor, character), the function returns attribute matches for dyads from the same group. If you supply a continuous variable (numeric, integers), the function returns absolute difference effects for each dyad in the graph.

Usage

```
homophily_stat(
  variable = variable,
  type = "categorical",
  nodes = nodes,
  these.categories.only = NULL,
  zero_values = NULL
)
```

Arguments

variable	A attribute variable. Can be categorical (attribute matches) or continuous (absolute difference effects).
type	set to categorical. Can be set to absdiff instead. If set to categorical, the homophily statistic calculates matches between dyads from the same group (analogous to dummy variables measuring attribute match between two nodes $(=10)$ and attribute mismatch $(=1)$). If set to absdiff it calculates the difference in values from variable for each dyad in the graph.
nodes	optional character/factor vector. If an edgelist is provided, you have to provide a list of unique identifiers of your nodes in the graph. This is because in the edgelist, isolates are usually not recorded. If you do not specify isolates in your nodes object, they are excluded from the analysis (falsifies data).
these.categorie	
	optional vector specifying the categories to be used, if only a subset of fac- tor(variable) is needed.
zero_values	optional numeric value. Use this to substitute zero-values in your homophily change statistic matrix. Zero values in the predictors are recognized in the gHypEG regression as structural zeroes. To ensure this does not happen, please recode your zero-values in all your predictors, ideally using a dummy variable fitting an optimal value for the zeroes. Only useful with absdiff type.

isNetwork

Value

Homophily change statistic matrix.

Author(s)

LB, GC

See Also

reciprocity_stat or sharedPartner_stat

Examples

```
homop_stat <- homophily_stat(variable = vertexlabels, nodes = rownames(adj_karate))
nrm(w=list('homophily'= homop_stat), adj_karate, directed = FALSE, selfloops = FALSE)</pre>
```

isNetwork

Test null model vs full ghype.

Description

isNetwork tests a graph for the SCM vs the full ghype model.

Usage

```
isNetwork(
  graph,
  directed,
  selfloops,
  Beta = TRUE,
  nempirical = NULL,
  parallel = FALSE,
  returnBeta = FALSE,
  seed = NULL
)
```

Arguments

graph	adjacency matrix or igraph graph
directed	a boolean argument specifying whether object is directed or not.
selfloops	a boolean argument specifying whether the model should incorporate selfloops.
Beta	boolean, use Beta test? default TRUE
nempirical	optional, number of graphs to sample from null distribution for empirical distri- bution.

parallel	optional, number of cores to use or boolean for parallel computation. If passed TRUE uses all cores-1, else uses the number of cores passed. If none passed performed not in parallel.
returnBeta	boolean, return estimated parameters of Beta distribution? Default FALSE.
seed	optional integer, seed for empirical lr.test

Value

p-value of test.

Examples

```
data("adj_karate")
isNetwork(graph = adj_karate, directed = FALSE, selfloops = FALSE, seed=123)
```

JnBlock

Fisher Information matrix for estimators in block models.

Description

Fisher Information matrix for estimators in block models.

Usage

```
JnBlock(omegaBlocks, xiBlocks, mBlocks, m)
```

Arguments

omegaBlocks	the block parameters (vector)
xiBlocks	the xi-block (vector)
mBlocks	the adj-block (vector)
m	the number of edges (scalar)

Value

Fisher Information matrix

linkSignificance Estimate statistical deviations from ghype model

Description

linkSignificance allows to estimate the statistical deviations of an observed graph from a ghype model.

Usage

```
linkSignificance(
  graph,
 model,
  under = FALSE,
  log.p = FALSE,
 binomial.approximation = FALSE,
 give_pvals = FALSE
)
link_significance(
 graph,
 model,
 under = FALSE,
 log.p = FALSE,
 binomial.approximation = FALSE,
  give_pvals = FALSE
)
```

Arguments

graph	an adjacency matrix or a igraph object.
model	a ghype model
under	boolean, estimate under-represented deviations? Default FALSE.
log.p	boolean, return log values of probabilities
<pre>binomial.approx</pre>	imation
	boolean, force binomial? default FALSE
give_pvals	boolean, return p-values for both under and over significance?

Value

matrix of probabilities with same size as adjacency matrix.

Examples

```
data("adj_karate")
fullmodel <- ghype(graph = adj_karate, directed = FALSE, selfloops = FALSE)
link_significance(graph = adj_karate, model = fullmodel, under=FALSE)</pre>
```

logl

General method to compute log-likelihood for ghype models.

Description

General method to compute log-likelihood for ghype models.

Usage

```
logl(
 object,
 xi = NULL,
  omega = NULL,
  directed = NULL,
  selfloops = NULL,
  adj = NULL,
 multinomial = NULL,
  . . .
)
## S3 method for class 'ghype'
logl(
 object,
 xi = NULL,
  omega = NULL,
 directed = NULL,
  selfloops = NULL,
  adj = NULL,
 multinomial = NULL,
  . . .
)
## S3 method for class 'matrix'
logl(
 object,
  xi = NULL,
  omega = NULL,
  directed = NULL,
  selfloops = NULL,
  adj = NULL,
 multinomial = NULL,
```

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) ...

Arguments

object	either an adjacency matrix or ghype model If a ghype model is passed, then 'xi', 'omega', 'directed', 'selfloops' are ignored If an adjacency matrix is passed, then 'adj' is ignored
xi	matrix, combinatorial matrix to build ghype model, considered only if object is an adjacency matrix
omega	matrix, propensity matrix to build ghype model, considered only if object is an adjacency matrix
directed	boolean, is ghype model directed? considered only if object is an adjacency matrix
selfloops	boolean, has ghype model selfloops? considered only if object is an adjacency matrix
adj	optional matrix, adjacency matrix of which to compute log-likelihood, consid- ered only if object is ghype model If adj is not passed, and object is a ghype model, the log-likelihood is computed for the original adjacency matrix stored in object.
multinomial	optional boolean. Force multinomial approximation? If not chosen, multinomial chosen for large graphs.
	additional parameters passed to and from internal methods

Value

loglikelihood value

Methods (by class)

- ghype: Computes log-likelihood for ghype models from model object
- matrix: Computes log-likelihood for ghype models from adjacency.

Examples

```
data('adj_karate')
model <- scm(adj_karate, FALSE, FALSE)
logl(object = model)
new_adj <- adj_karate
new_adj[3,4] <- 10
logl(object=model, adj=new_adj)</pre>
```

logLik.ghype

Description

Extract Log-Likelihood

Usage

S3 method for class 'ghype'
logLik(object, ...)

Arguments

object	ghype model.
	additional arguments passed to and from internal methods.

Value

Returns an object of class logLik. This is a number with at least one attribute, "df" (degrees of freedom), giving the number of (estimated) parameters in the model.

loglratio	Compute log-likelihood ratio for ghype models.	
-----------	--	--

Description

Compute log-likelihood ratio for ghype models.

Usage

loglratio(mod0, mod1)

Arguments

mod0	ghype, null model
mod1	ghype, alternative model

Value

scalar, log-likelihood ratio

lr.test

Examples

```
data('adj_karate')
sc.model <- scm(adj_karate, FALSE, FALSE)
full.model <- ghype(adj_karate, FALSE, FALSE)
loglratio(sc.model,full.model)</pre>
```

lr.test

Perform likelihood ratio test between two ghype models.

Description

lr.test allows to test between two nested ghype models whether there is enough evidence for the alternative (more complex) model compared to the null model.

Usage

```
lr.test(
   nullmodel,
   altmodel,
   df = NULL,
   Beta = TRUE,
   seed = NULL,
   nempirical = NULL,
   parallel = FALSE,
   returnBeta = FALSE,
   method = NULL
)
```

Arguments

nullmodel	ghype object. The null model
altmodel	ghype object. The alternative model
df	optional scalar. the number of degrees of freedom.
Beta	boolean, whether to use empirical Beta distribution approximation. Default TRUE
seed	scalar, seed for the empirical distribution.
nempirical	optional scalar, number of replicates for empirical beta distribution.
parallel	optional, number of cores to use or boolean for parallel computation. If passed TRUE uses all cores-1, else uses the number of cores passed. If none passed performed not in parallel.
returnBeta	boolean, return estimated parameters of Beta distribution? Default FALSE.
method	string, for internal use

Value

p-value of test. If returnBeta=TRUE returns the p-value together with the parameters of the beta distribution.

Examples

```
data("adj_karate")
regularmodel <- regularm(graph = adj_karate, directed = FALSE, selfloops = FALSE)
confmodel <- scm(graph = adj_karate, directed = FALSE, selfloops = FALSE)
lr.test(nullmodel = regularmodel, altmodel = confmodel, seed = 123)</pre>
```

mat2vec.ix Auxiliary function, gives mask for matrix for directed, undirected	mat2vec.ix	Auxiliary function	, gives mask for matrix	for directed	, undirected etc
---	------------	--------------------	-------------------------	--------------	------------------

Description

Auxiliary function, gives mask for matrix for directed, undirected etc.

Usage

mat2vec.ix(mat, directed, selfloops)

Arguments

mat	matrix
directed	a boolean argument specifying whether object is directed or not.
selfloops	a boolean argument specifying whether the model should incorporate selfloops.

Value

a boolean matrix that can be used to mask adjacency matrices.

Examples

```
data('adj_karate')
mat2vec.ix(adj_karate, FALSE, FALSE)
```

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mcfaddenR2

Description

Pass either the models or the model parameters as arguments

Usage

```
mcfaddenR2(
  adj = NULL,
  xi = NULL,
  omega0 = NULL,
  omega1 = NULL,
  directed,
  selfloops,
  mod0 = NULL,
  mod1 = NULL,
  nparam
)
```

Arguments

adj	optimal adjacency matrix
xi	optional xi matrix
omega0	optional propensity matrix of null model
omega1	optional propensity matrix of alternative model
directed	boolean, is the model directed?
selfloops	boolean, are there selfloops?
mod0	nrm null model
mod1	nrm alternative model
nparam	integer, number of parameters

Value

Mc Fadden pseudo R-squared.

nr.ci

Description

Internal function to compute confidence intervals for estimated parameters of nrm model

Usage

nr.ci(nr.m, w, adj, pval)

Arguments

nr.m	nrm model from which getting coefficients
W	list of predictors
adj	adjacency matrix
pval	numeric. confidence level

Value

matrix reporting values of predictors and confidence bounds

nr.significance	Computes the significance of more complex model against a simpler
	model by means of a likelihood ratio test.

Description

Computes the significance of more complex model against a simpler model by means of a likelihood ratio test.

Usage

```
nr.significance(mod0 = NULL, mod1, adj = NULL)
```

Arguments

mod0	null nrm model (optional). defaults to the scm model.
mod1	alternative nrm model, the model to test
adj	adjacency matrix for which performing the test. (optional) defaults to the matrix used for mod1.

Value

p-value of the lr test mod0 vs mod1

nrm

Description

nrm is used to fit multi-edge network regression models.

Usage

```
nrm(
 w,
  adj,
 xi = NULL,
 pval = 0.01,
 directed = TRUE,
  selfloops = TRUE,
 regular = FALSE,
  . . .
)
## Default S3 method:
nrm(
 w,
  adj,
 xi = NULL,
 pval = 0.01,
 directed = FALSE,
  selfloops = FALSE,
  regular = FALSE,
  ci = TRUE,
  significance = FALSE,
 null = FALSE,
 init = NULL,
  . . .
)
## S3 method for class 'nrm'
print(x, suppressCall = FALSE, ...)
```

Arguments

W	an object of class 'list' containing the predictors layers (explanatory vari- ables/covariates) of the multiplex, passed as adjacency matrices. The entries of the list can be named.
adj	matrix. The adjacency matrix of the response network (dependent variable).
xi	optional matrix. Passes a non-standard Ξ matrix.

pval	the significance level used to compute confidence intervals of the parameters. Per default, set to 0.01.
directed	logical. If TRUE the response variable is considered the adjacency matrix of directed graph. If FALSE only the upper triangular of adj is considered. Default set to FALSE.
selfloops	logical. Whether selfloops are allowed. Default set to FALSE.
regular	logical. Whether the gHypEG regression should be performed with correction of combinatorial effects (TRUE) or without (FALSE).
	optional arguments to print or plot methods.
ci	logical. Whether to compute confidences for the parameters. Defaults to TRUE.
significance	logical. Whether to test the model significance against the null by means of lr-test.
null	logical. Is this a null model? Used for internal routines.
init	numeric. Vector of initial values used for numerical MLE. If only a single value is passed, this is repeated to match the number of predictors in w.
x	object of class 'nrm'
suppressCall	logical, indicating whether to print the call that generated x

Value

nrm returns an object of class 'nrm'.

The function summary is used to obtain and print a summary and analysis of the results. The generic accessory functions coefficients, etc, extract various useful features of the value returned by nrm.

An object of class 'nrm' is a list containing at least the following components:

coef	a named vector of coefficients.
confint	a named matrix with confidence intervals and standard deviation for each coef- ficient.
omega	the estimated propensity matrix.
xi	the matrix of possibilities.
loglikelihood	log-likelihood of the estimated model.
AIC	AIC of the estimated model.
R2	Mc Fadden pseudo R-squared
csR2	Cox and Snells pseudo R-squared
significance	the p-value of the likelihood-ratio test for the estimated model against the null.

Methods (by class)

- default: Default method for nrm
- nrm: Print method for elements of class 'nrm'.

nrmChoose

Author(s)

Giona Casiraghi

Giona Casiraghi

References

Casiraghi, Giona. 'Multiplex Network Regression: How do relations drive interactions?.' arXiv preprint arXiv:1702.02048 (2017).

See Also

nrm

Examples

For a complete example see the vignette

```
data('highschool.predictors')
```

```
highschool.m <- nrm(w=highschool.predictors[1], adj=contacts.adj, directed=FALSE,
    selfloops=FALSE)
```

highschool.m

data('highschool.predictors')

```
highschool.m <- nrm(w=highschool.predictors, adj=contacts.adj, directed=FALSE,
    selfloops=FALSE)
```

highschool.m

nrmChoose	Selects the best set of predictors among the given sets by means of
	AIC.

Description

Computes all the models defined by a list of groups of predictors Returns the best model according to AIC and id of the corresponding predictors in the list The different models are computed in parallel

nrmChoose

Usage

```
nrmChoose(
  adj,
  w.list,
  xi = NULL,
  directed,
  selfloops,
  pval = 0.05,
  init = NULL,
  ncores = NULL
)
nrm_choose(
  adj,
  w.list,
  xi = NULL,
  directed,
  selfloops,
  pval = 0.05,
  init = NULL,
  ncores = NULL
)
```

Arguments

adj	adjacency matrix
w.list	nrmPredictor object. Nested list of predictors to be selected.
xi	Xi matrix (optional). defaults to scm Xi matrix.
directed	logical. Is the network directed?
selfloops	logical. Does the network contain selfloops?
pval	numeric. the significance at which computing confidence intervals. defaults to 0.05
init	initial values for the MLE numerical maximisation. (See nrm.)
ncores	Number of cores for parallelisation of selection process. (optional) Defaults to number of available cores - 1.

Value

list containing the best model according to AIC and id of the corresponding predictors in the list

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nrmSelection

Description

Perform AIC forward selection for nrm.

Usage

```
nrmSelection(
  adj,
 predictors,
 directed,
  selfloops,
 pval = 0.05,
 xi = NULL,
 init = NULL,
 ncores = NULL,
  . . .
)
nrm_selection(
  adj,
  predictors,
  directed,
  selfloops,
  pval = 0.05,
 xi = NULL,
  init = NULL,
 ncores = NULL,
  . . .
)
## Default S3 method:
nrm_selection(
  adj,
 predictors,
 directed,
  selfloops,
  pval = 0.05,
 xi = NULL,
  init = NULL,
  ncores = NULL,
  . . .
)
## S3 method for class 'nrmpredictor'
```

```
nrm_selection(
    adj,
    predictors,
    directed,
    selfloops,
    pval = 0.05,
    xi = NULL,
    init = NULL,
    ...
)
## S3 method for class 'nrm_selection'
```

```
print(x, ...)
```

Arguments

adj	the adjacency matrix of the response network
predictors	list containing the set of predictors as sublists.
directed	logical, is the response network directed?
selfloops	logical, do the response network allows selfloops?
pval	the significance at which computing confidence intervals.
xi	optional, the possibility matrix Ξ .
init	optional, initial values passed to the solver to estimate the MLE.
ncores	optional, number of cores over which parallelise the task.
	optional arguments to print or plot methods.
х	object of class 'nrm_selection'.

Value

A nrm object

Methods (by class)

- default: Default method for the nrm stepwise selection.
- nrmpredictor: Method for the nrm stepwise selection when nrmpredictors are passed.
- nrm_selection: Print method for elements of class 'nrm_selection'.

Author(s)

Giona Casiraghi Giona Casiraghi

See Also

nrm
nrm_selection

onlinesim_mat

Examples

```
data('highschool.predictors')
models <- nrm_selection(adj=contacts.adj,predictors=create_predictors(highschool.predictors),
    ncores=1,directed=FALSE,selfloops=FALSE)
texreg::screenreg(models$models, digits=3)</pre>
```

onlinesim_mat Swiss MPs committee similarity matrix.

Description

onlinesim_mat: a similarity matrix of how similar two MPs are in their online social media presence (shared supportees).

Usage

data(onlinesim_mat)

Format

163x163 similarity matrix

predict.nrm

Method to predict the expected values of a nrm model

Description

Method to predict the expected values of a nrm model

Usage

```
## S3 method for class 'nrm'
predict(object, m = NULL, adj = NULL, null = FALSE, multinomial = NULL, ...)
```

object	nrm object from which to predict
m	integer, the number of edges to be used
adj	optional matrix, the adjacency matrix from which to get the number of edges
null	optional boolean, is it a null model? default FALSE
multinomial	logical. Optional argument. Whether to use multinomial approximation. If left blank it is selected automatically based on network size.
	other arguments

Value

numeric, predicted values from nrm model. (If model is undirected, only upper.tri of adjacency matrix is returned.)

Examples

```
data('highschool.predictors')
highschool.m <- nrm(w=highschool.predictors[1], adj=contacts.adj, directed=FALSE, selfloops=FALSE)
predict(highschool.m, contacts.adj)</pre>
```

```
data('highschool.predictors')
highschool.m <- nrm(w=highschool.predictors, adj=contacts.adj, directed=FALSE, selfloops=FALSE)
predict(highschool.m, contacts.adj)</pre>
```

<pre>reciprocity_stat</pre>	Calculate	weighted	reciprocity	change	statistics	for	multi-edge
	graphs.						

Description

The function takes either an edgelist or an adjacency matrix and returns an adjacency matrix with the reciprocity change statistic. This reciprocity matrix can then be used as a predictor in the gHypEG regression.

Usage

```
reciprocity_stat(graph, nodes = NULL, zero_values = NULL)
```

Arguments

graph	A graph adjacency matrix or an edgelist. The edgelist needs to have 3 columns: a sender vector, a target vector and an edgecount vector.
nodes	optional character/factor vector. If an edgelist is provided, you have to provide a list of unique identifiers of your nodes in the graph. This is because in the edgelist, isolates are usually not recorded. If you do not specify isolates in your nodes object, they are excluded from the analysis (falsifies data).
zero_values	optional numeric value. Use this to substitute zero-values in your reciprocity change statistic matrix. Zero values in the predictors are recognized in the gHy- pEG regression as structural zeros. To ensure this does not happen, please recode your zero-values in all your predictors, ideally using a dummy variable fitting an optimal value for the zeroes.

Value

Reciprocity change statistic matrix.

regularm

Author(s)

LB, GC

See Also

sharedPartner_stat or homophily_stat

Examples

```
recip_stat <- reciprocity_stat(adj_karate)
recip_stat_dummy <- get_zero_dummy(recip_stat, name = 'reciprocity')
nrm(w=recip_stat_dummy, adj_karate, directed = FALSE, selfloops = FALSE)</pre>
```

regularm

Fit the gnm model

Description

regularm is wrapper for ghype that allows to specify a gnm regular model. i.e. where all entries of the combinatorial matrix Xi are the same.

Usage

```
regularm(graph, directed = NULL, selfloops = NULL, ...)
```

Arguments

graph	either an adjacency matrix or an igraph graph
directed	optional boolean, if not specified detected from graph
selfloops	optional boolean, if not specified detected from graph
	additional parameters passed to the ghype function

Value

ghype object

Examples

```
data("adj_karate")
regularmodel <- regularm(graph = adj_karate, directed = FALSE, selfloops = FALSE)</pre>
```

residuals.nrm

Description

Method to compute residuals of nrm models

Usage

```
## S3 method for class 'nrm'
residuals(object, adj, RMSLE = FALSE, null = FALSE, ...)
```

Arguments

object	nrm object
adj	adjacency against which to compute residuals
RMSLE	logical, return log residuals? default FALSE
null	logical. use null model?
	additional parameters to be passed to and from internal functions.

Value

numeric vector, residuals of nrm model fit against the original data

Examples

```
data('highschool.predictors')
highschool.m <- nrm(w=highschool.predictors[1], adj=contacts.adj, directed=FALSE, selfloops=FALSE)
residuals(highschool.m, contacts.adj)</pre>
```

rgł	уре
-----	-----

Generate random realisations from ghype model.

Description

Generate random realisations from ghype model.

Usage

```
rghype(nsamples, model, m = NULL, multinomial = NULL, seed = NULL)
```

RMSE

Arguments

nsamples	scalar number of realisations
model	ghype model
m	optional scalar, number of edges to draw
multinomial	optional boolean, draw from multinomial?
seed	optional scalar, seed for random sampling.

Value

list of adjacency matrices.

Examples

```
data('adj_karate')
model <- scm(adj_karate, FALSE, FALSE)
rghype(1, model)</pre>
```

```
RMSE
```

Computes the Root Mean Squared Error

Description

Computes the Root Mean Squared Error

Usage

RMSE(model, adj, null = FALSE)

Arguments

model	nrm model estimate
adj	original adjacency matrix
null	logical, whether to compute using null model

Value

numeric, root mean squared error of residuals of nrm model fit

Examples

```
data('highschool.predictors')
highschool.m <- nrm(w=highschool.predictors[1], adj=contacts.adj, directed=FALSE, selfloops=FALSE)
RMSE(highschool.m, contacts.adj)</pre>
```

RMSLE

Description

Computes the Root Mean Squared Logged Error

Usage

RMSLE(model, adj, null = FALSE)

Arguments

model	nrm model estimate
adj	original adjacency matrix
null	logical, whether to compute using null model

Value

numeric, root mean squared logged error of residuals of nrm model fit

Examples

```
data('highschool.predictors')
highschool.m <- nrm(w=highschool.predictors[1], adj=contacts.adj, directed=FALSE, selfloops=FALSE)
RMSLE(highschool.m, contacts.adj)</pre>
```

scm

Fit the Soft-Configuration Model

Description

scm is wrapper for ghype that allows to specify a soft-configuration model.

Usage

scm(graph, directed = NULL, selfloops = NULL, ...)

graph	either an adjacency matrix or an igraph graph
directed	optional boolean, if not specified detected from graph
selfloops	optional boolean, if not specified detected from graph
	additional parameters passed to the ghype function

sharedPartner_stat

Value

ghype object

Examples

```
data("adj_karate")
confmodel <- scm(graph = adj_karate, directed = FALSE, selfloops = FALSE)</pre>
```

sharedPartner_stat Calculate (un-)weighted shared partner change statistics for multiedge graphs.

Description

The function calculates the change statistic for shared partners for each dyad in the graph. Shared partner statistics count for each dyad involving nodes i and j in the graph, how many nodes k these two nodes have in common (or share). The shared partner \$k\$ counts are weighted by their interactions with the focal nodes \$i\$ and \$j\$. This is necessary in dense multi-edge graphs to ensure that meaningful triadic closure is detected. The statistic can be calculated in 3 different forms: undirected, incoming shared partners (where shared partner k: k->i and k->j) and outgoing shared partners (where shared partner k: k->i and k->j).

Usage

```
sharedPartner_stat(
  graph,
  directed,
  weighted = TRUE,
  triad.type = "undirected",
  nodes = NULL,
  zero_values = NULL
)
```

graph	A graph adjacency matrix or an edgelist. The edgelist needs to have 3 columns: a sender vector, a target vector and an edgecount vector.
directed	boolean. Is the graph directed?
weighted	set to TRUE.
triad.type	set to undirected. Can be set to incoming or outgoing instead. This then corresponds to directed triadic closure in the multi-edge graph.
nodes	optional character/factor vector. If an edgelist is provided, you have to provide a list of unique identifiers of your nodes in the graph. This is because in the edgelist, isolates are usually not recorded. If you do not specify isolates in your nodes object, they are excluded from the analysis (falsifies data).

zero_values	optional numeric value. Use this to substitute zero-values in your shared part-
	ner change statistic matrix. Zero values in the predictors are recognized in the
	gHypEG regression as structural zeros. To ensure this does not happen, please
	recode your zero-values in all your predictors, ideally using a dummy variable
	fitting an optimal value for the zeroes.

Value

Shared partner change statistic matrix.

Author(s)

LB, GC, GV

See Also

reciprocity_stat or homophily_stat

Examples

```
tri_stat <- sharedPartner_stat(adj_karate, directed = FALSE)
tri_stat_dummy <- get_zero_dummy(tri_stat, name = 'shared_partners')
nrm(w=tri_stat_dummy, adj_karate, directed = FALSE, selfloops = FALSE)</pre>
```

summary.nrm Summary method for elements of class 'nrm'.

Description

Currently it provides the same output as 'print.nrm'

Usage

```
## S3 method for class 'nrm'
summary(object, ...)
```

S3 method for class 'summary.nrm'
print(x, ...)

Arguments

object	an object of class 'nrm', usually, a result of a call to nrm.
	further arguments passed to or from other methods.
х	object of class 'summary.nrm' returned by [summary.nrm()].

Value

The function summary.nrm computes and returns a list of summary statistics of the fitted nrm model given in object.

summary.nrm_selection Summary method for elements of class 'nrm_selection'.

Description

Summary method for elements of class 'nrm_selection'.

Usage

```
## S3 method for class 'nrm_selection'
summary(object, ...)
## S3 method for class 'summary.nrm_selection'
print(x, ...)
```

Arguments

object	an object of class 'nrm_selection', usually, a result of a call to nrm_selection.
	further arguments passed to or from other methods.
x	object of class 'summary.nrm_selection' returned by [summary.nrmselection()].

Value

The function summary.nrm_selection computes and returns a list of summary statistics of the fitted nrm_selection model given in object.

vec2mat Auxiliary function, produces matrix from vector	
---	--

Description

The number of elements of vec are the number of non-zero elements in the adjacency matrix. It performs the opposite operation of 'mat2vec.ix'.

Usage

```
vec2mat(vec, directed, selfloops, n)
```

vec	vector to be put in matrix form
directed	a boolean argument specifying whether object is directed or not.
selfloops	a boolean argument specifying whether the model should incorporate selfloops.
n	vector. if $length(n)==1$, n is the number of vertices. If $length(n)==3$ first element is number of vertices, second and third elements are number of vertices for row and column of bipartite matrix.

Value

matrix nxn generated from vector.

Examples

```
data('adj_karate')
ix <- mat2vec.ix(adj_karate, FALSE, FALSE)
vec <- adj_karate[ix]
vec2mat(vec, FALSE, FALSE, nrow(adj_karate))</pre>
```

vertexlabels Zachary's Karate Club vertex faction assignment

Description

Vector reporting the assignment of nodes to communities.

Usage

vertexlabels

Format

a 34-vector with the assignment of nodes to faction 1 or 2

Source

package 'igraphdata'

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