

Package ‘mvnnormalTest’

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Description A simple informative powerful test (mvnTest()) for multivariate normality proposed by Zhou and Shao (2014) <doi:10.1080/02664763.2013.839637>, which combines kurtosis with Shapiro-Wilk test that is easy for biomedical researchers to understand and easy to implement in all dimensions. This package also contains some other multivariate normality tests including Fattorini's FA test (faTest()), Mardia's skewness and kurtosis test (mardia()), Henze-Zirkler's test (mhz()), Bowman and Shenton's test (msk()), Royston's H test (msw()), and Villaseñor-Alva and Gonzalez-Estrada's test (msw()). Empirical power calculation functions for these tests are also provided. In addition, this package includes some functions to generate several types of multivariate distributions mentioned in Zhou and Shao (2014).

License GPL (>= 2)

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copulas	<i>Random Generation for the Copula Generated Distributions</i>
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Description

Generate univariate or multivariate random sample for the Copula Generated Distributions.

Usage

```
copulas(n, p, c = "clayton", param, invF, ...)
```

Arguments

n	number of rows (observations).
p	total number of columns (variables).
c	name of an Archimedean copula, choosing from "clayton" (default), "frank", or "gumbel".
param	number (numeric) specifying the copula parameter.
invF	inverse function (quantile function, e.g. qnorm).
...	optional arguments passed to invF.

Value

univariate ($p = 1$) or multivariate ($p > 1$) random sample.

References

Yan, J. (2007). Enjoy the joy of copulas: with a package copula. *Journal of Statistical Software*, 21(4), 1-21.

Examples

```
set.seed(12345)

## Generate 5X2 random sample matrix from Clayton(0.5, qnorm) ##
copulas(n=50, p=2, c="clayton", param=0.5, invF=qnorm)

## Power calculation against bivariate (p=2) Clayton(0.5, qnorm) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

# Zhou-Shao's test #
power.mvnTest(a=0.05, n=50, p=2, B=100, FUN=copulas, c="clayton", param=0.5, invF=qnorm)
```

faTest

Rotational Robust Shapiro-Wilk Type (SWT) Test for Multivariate Normality (FA Test of Fattorini)

Description

It computes FA Test proposed by Fattorini (1986). This test would be more rotationally robust than other SWT tests such as Royston (1982) H test and the test proposed by Villasenor-Alva and Gonzalez-Estrada (2009). The p -value of the test statistic is computed based on a simulated null distribution of the statistic.

Usage

```
faTest(X, B = 1000)
```

Arguments

X	an $n * p$ data matrix or data frame, where n is number of rows (observations) and p is number of columns (variables) and $n > p$.
B	number of Monte Carlo simulations for null distribution, default is 1000 (increase B to increase the precision of p -value).

Value

Returns a list with two objects:

`mv.test` results of the FA test for multivariate normality, i.e., test statistic, p -value, and multivariate normality summary (YES, if p -value>0.05).

`uv.shapiro` a dataframe with p rows detailing univariate Shapiro-Wilk tests. Columns in the dataframe contain test statistics W , p -value, and univariate normality summary (YES, if p -value>0.05).

References

Fattorini, L. (1986). Remarks on the use of Shapiro-Wilk statistic for testing multivariate normality. *Statistica*, 46(2), 209-217.

Lee, R., Qian, M., & Shao, Y. (2014). On rotational robustness of Shapiro-Wilk type tests for multivariate normality. *Open Journal of Statistics*, 4(11), 964.

Shapiro, S. S., & Wilk, M. B. (1965). An analysis of variance test for normality (complete samples). *Biometrika*, 52(3/4), 591-611.

Royston, J. P. (1982). An extension of Shapiro and Wilk's W test for normality to large samples. *Journal of the Royal Statistical Society: Series C (Applied Statistics)*, 31(2), 115-124.

Villasenor Alva, J. A., & Estrada, E. G. (2009). A generalization of Shapiro-Wilk's test for multivariate normality. *Communications in Statistics—Theory and Methods*, 38(11), 1870-1883.

Zhou, M., & Shao, Y. (2014). A powerful test for multivariate normality. *Journal of applied statistics*, 41(2), 351-363.

See Also

[power.faTest](#), [mvnTest](#), [msk](#), [mardia](#), [msw](#), [mhz](#)

Examples

```
set.seed(12345)

## Data from gamma distribution ##
X = matrix(rgamma(50*4, shape = 2), 50)
faTest(X, B=100)

## load the ubiquitous multivariate iris data ##
## (first 50 observations of columns 1:4) ##
iris.df = iris[1:50, 1:4]
faTest(iris.df, B=100)
```

Description

Generate univariate or multivariate random sample for distribution with independent marginals such that $D_1 \otimes D_2$. $D_1 \otimes D_2$ denotes the distribution having independent marginal distributions D_1 and D_2 . This function can generate multivariate random samples only from distribution D_1 or from both D_1 and D_2 .

Usage

```
IMMV(n, p, q = NULL, D1, D2 = NULL, D1.args = list(), D2.args = list())
```

Arguments

n	number of rows (observations).
p	total number of columns (variables).
q	number of columns from distribution D1 if generate multivariate samples from independent marginal distribution D_1 and D_2 . Default is NULL, i.e., generating samples only from one distribution.
D1	random generation function for 1st distribution (e.g., rnorm, rbeta).
D2	random generation function for 2nd distribution (e.g., rnorm, rbeta).
D1.args	a list of optional arguments passed to D1.
D2.args	a list of optional arguments passed to D2.

Value

Returns univariate ($p = 1$) or multivariate ($p > 1$) random sample matrix.

References

Zhou, M., & Shao, Y. (2014). A powerful test for multivariate normality. *Journal of applied statistics*, 41(2), 351-363.

Henze, N., & Zirkler, B. (1990). A class of invariant consistent tests for multivariate normality. *Communications in statistics-Theory and Methods*, 19(10), 3595-3617.

Examples

```
set.seed(12345)

## Generate 5X2 random sample matrix from IMMV(N(0,1),Beta(1,2)) ##
IMMV(n=5, p=2, q=1, D1=rbeta, D1.args=list(shape1=1,shape2=2), D2=rnorm)

## Power calculation against bivariate (p=2) IMMV(Gamma(5,1)) distribution ##
```

```
## at sample size n=50 at one-sided alpha = 0.05 ##

# Zhou-Shao's test #
power.mvnTest(a=0.05, n=50, p=2, B=100, FUN=IMMV, D1=rgamma, D1.args=list(shape=5, rate=1))

## Power calculation against bivariate (p=2) IMMV(N(0,1),Beta(1,2)) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

# Zhou-Shao's test #
power.mvnTest(a=0.05, n=50, p=2, B=100, FUN=IMMV, q=1, D1=rbeta, D1.args=list(shape1=1,shape2=2),
D2=rnorm)
```

mardia

Mardia Test (Skewness and Kurtosis) for Multivariate Normality

Description

It computes Mardia (1970)'s multivariate skewness and kurtosis statistics and their corresponding p -value. Both p -values of skewness and kurtosis statistics should be greater than 0.05 to conclude multivariate normality. The skewness statistic will be adjusted for sample size $n < 20$.

Usage

```
mardia(X, std = TRUE)
```

Arguments

<code>X</code>	an $n * p$ numeric matrix or data frame.
<code>std</code>	if TRUE, the data matrix or data frame will be standardized via normalizing the covariance matrix by n .

Value

Returns a list with two objects:

`mv.test` results of the Mardia test, i.e., test statistic, p -value, and multivariate normality summary (YES, if both skewness and kurtosis p -value>0.05).

`uv.shapiro` a dataframe with p rows detailing univariate Shapiro-Wilk tests. Columns in the dataframe contain test statistics W , p -value, and univariate normality summary (YES, if p -value>0.05).

References

Mardia, K. V. (1970). Measures of multivariate skewness and kurtosis with applications. *Biometrika*, 57(3), 519-530.

Shapiro, S. S., & Wilk, M. B. (1965). An analysis of variance test for normality (complete samples). *Biometrika*, 52(3/4), 591-611.

Doornik, J. A., & Hansen, H. (2008). An omnibus test for univariate and multivariate normality. *Oxford Bulletin of Economics and Statistics*, 70, 927-939.

Zhou, M., & Shao, Y. (2014). A powerful test for multivariate normality. *Journal of applied statistics*, 41(2), 351-363.

See Also

[mvnTest](#), [faTest](#), [msw](#), [msk](#), [mhz](#), [mvn](#)

Examples

```
set.seed(12345)

## Data from gamma distribution
X = matrix(rgamma(50*4, shape = 2), 50)
mardia(X)

## Data from normal distribution
X = matrix(rnorm(50*4, mean = 2, sd = 1), 50)
mardia(X)

## load the ubiquitous multivariate iris data ##
## (first 50 observations of columns 1:4) ##
iris.df = iris[1:50, 1:4]
mardia(iris.df)
```

mhz

Henze-Zirkler Test for Multivariate Normality

Description

It computes a multivariate normality test based on a non-negative functional distance which was proposed by Henze and Zirkler (1990). Under the null hypothesis the test statistic is approximately log-normally distributed.

Usage

```
mhz(X)
```

Arguments

X an $n * p$ numeric matrix or data frame.

Value

Returns a list with two objects:

- `mv.test` results of the Henze-Zirkler test, i.e., test statistic, p -value, and multivariate normality summary (YES, if p -value>0.05).
- `uv.shapiro` a dataframe with p rows detailing univariate Shapiro-Wilk tests. Columns in the dataframe contain test statistics W , p -value, and univariate normality summary (YES, if p -value>0.05).

References

- Henze, N., & Zirkler, B. (1990). A class of invariant consistent tests for multivariate normality. *Communications in statistics-Theory and Methods*, 19(10), 3595-3617.
- Shapiro, S. S., & Wilk, M. B. (1965). An analysis of variance test for normality (complete samples). *Biometrika*, 52(3/4), 591-611.
- Zhou, M., & Shao, Y. (2014). A powerful test for multivariate normality. *Journal of applied statistics*, 41(2), 351-363.

See Also

[power.mhz](#), [mvnTest](#), [faTest](#), [msw](#), [msk](#), [mardia](#), [mvn](#)

Examples

```
set.seed(12345)

## Data from gamma distribution
X = matrix(rgamma(50*4, shape = 2), 50)
mhz(X)

## Data from normal distribution
X = matrix(rnorm(50*4, mean = 2, sd = 1), 50)
mhz(X)

## load the ubiquitous multivariate iris data ##
## (first 50 observations of columns 1:4) ##
iris.df = iris[1:50, 1:4]
mhz(iris.df)
```

msk

Bowman and Shenton Test for Multivariate Normality

Description

It computes Bowman and Shenton (1975)'s test statistic (MSK) and its corresponding p -value for multivariate normality. The statistic is calculated based on a combination of multivariate skewness (MS) and kurtosis (MK) such that $MSK = MS + |MK|^2$. For formulas of MS and MK, please refer to Mardia (1970). The corresponding p -value of the statistic is computed based on a simulated null distribution of MSK. The skewness statistic (MS) will be adjusted for sample size $n < 20$.

Usage

```
msk(X, B = 1000)
```

Arguments

X an $n * p$ numeric matrix or data frame.

B number of Monte Carlo simulations for null distribution, default is 1000 (increase B to increase the precision of p-value).

Value

Returns a list with two objects:

mv.test results of the Bowman and Shenton test, i.e., test statistic, p -value, and multivariate normality summary (YES, if p -value>0.05).

uv.shapiro a dataframe with p rows detailing univariate Shapiro-Wilk tests. Columns in the dataframe contain test statistics W , p -value, and univariate normality summary (YES, if p -value>0.05).

References

- Bowman, K. O., & Shenton, L. R. (1975). Omnibus test contours for departures from normality based on $\sqrt{b_1}$ and b_2 . *Biometrika*, 62(2), 243-250.
- Shapiro, S. S., & Wilk, M. B. (1965). An analysis of variance test for normality (complete samples). *Biometrika*, 52(3/4), 591-611.
- Mardia, K. V. (1970). Measures of multivariate skewness and kurtosis with applications. *Biometrika*, 57(3), 519-530.
- Doornik, J. A., & Hansen, H. (2008). An omnibus test for univariate and multivariate normality. *Oxford Bulletin of Economics and Statistics*, 70, 927-939.
- Zhou, M., & Shao, Y. (2014). A powerful test for multivariate normality. *Journal of applied statistics*, 41(2), 351-363.

See Also

[power.msk](#), [mvnTest](#), [faTest](#), [msw](#), [mardia](#), [mhz](#), [mvn](#)

Examples

```
set.seed(12345)

## Data from gamma distribution
X = matrix(rgamma(50*4, shape = 2), 50)
msk(X, B=100)

## load the ubiquitous multivariate iris data ##
## (first 50 observations of columns 1:4) ##
iris.df = iris[1:50, 1:4]
msk(iris.df, B=100)
```

msw

*Shapiro-Wilk Type (SWT) Tests for Multivariate Normality***Description**

The SWT-based tests for multivariate normality including Royston's H test and the test proposed by Villaseñor-Alva and Gonzalez-Estrada (2009).

Usage

```
msw(X)
```

Arguments

X an $n * p$ numeric matrix or data frame, the number of n must be between 3 and 5000, $n > p$.

Value

Returns a list with two objects:

mv.test a result table of multivariate normality tests, including the name of the test, test statistic, p -value, and multivariate normality summary (Yes, if p -value > 0.05). Note that the test results of Royston will not be reported if $n > 2000$ or $n < 3$ and the test results of Villaseñor-Alva and Gonzalez-Estrada (VAGE) will not be reported if $n > 5000$ or $n < 12$.

uv.shapiro a dataframe with p rows detailing univariate Shapiro-Wilk tests. Columns in the dataframe contain test statistics W , p -value, and univariate normality summary (YES, if p -value > 0.05). If the number of variable is $p = 1$, only univariate Shapiro-wilk's test result will be produced.

References

Shapiro, S. S., & Wilk, M. B. (1965). An analysis of variance test for normality (complete samples). *Biometrika*, 52(3/4), 591-611.

Royston, J. P. (1982). An extension of Shapiro and Wilk's W test for normality to large samples. *Journal of the Royal Statistical Society: Series C (Applied Statistics)*, 31(2), 115-124.

Villaseñor Alva, J. A., & Estrada, E. G. (2009). A generalization of Shapiro-Wilk's test for multivariate normality. *Communications in Statistics—Theory and Methods*, 38(11), 1870-1883.

Lee, R., Qian, M., & Shao, Y. (2014). On rotational robustness of Shapiro-Wilk type tests for multivariate normality. *Open Journal of Statistics*, 4(11), 964.

See Also

[power.mswR](#), [power.mswV](#), [mvnTest](#), [faTest](#), [msk](#), [mardia](#), [mhz](#), [mvn](#), [shapiro.test](#)

Examples

```

set.seed(12345)

## Data from gamma distribution
X = matrix(rgamma(50*4, shape = 2), 50)
msw(X)

## Data from normal distribution
X = matrix(rnorm(50*4, mean = 2, sd = 1), 50)
msw(X)

## load the ubiquitous multivariate iris data ##
## (first 50 observations of columns 1:4) ##
iris.df = iris[1:50, 1:4]
msw(iris.df)

```

MVNMIX

*Random Generation for the Normal Mixture Distribution***Description**

Generate univariate or multivariate random sample for the normal mixture distribution with density $\lambda N(0, \Sigma_1) + (1 - \lambda)N(bl, \Sigma_2)$, where l is the column vector with all elements being 1, $\Sigma_i = (1 - \rho_i)I + \rho_i ll^T$ for $i = 1, 2$. ρ has to satisfy $\rho > -1/(p - 1)$ in order to make the covariance matrix meaningful.

Usage

```
MVNMIX(n, p, lambda, mu2, rho1 = 0, rho2 = 0)
```

Arguments

n	number of rows (observations).
p	total number of columns (variables).
lambda	weight parameter to allocate the proportions of the mixture, $0 < \lambda < 1$.
mu2	is bl of $N(bl, \Sigma_2)$.
rho1	parameter in Σ_1 .
rho2	parameter in Σ_2 .

Value

Returns univariate ($p = 1$) or multivariate ($p > 1$) random sample matrix.

References

Zhou, M., & Shao, Y. (2014). A powerful test for multivariate normality. *Journal of applied statistics*, 41(2), 351-363.

Examples

```
set.seed(12345)

## Generate 5X2 random sample matrix from MVNMIX(0.5,4,0,0) ##
MVNMIX(n=5, p=2, lambda=0.5, mu2=4, rho1=0, rho2=0)

## Power calculation against bivariate (p=2) MVNMIX(0.5,4,0,0) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

# Zhou-Shao's test #
power.mvnTest(a=0.05, n=50, p=2, B=100, FUN=MVNMIX, lambda=0.5, mu2=4, rho1=0, rho2=0)
```

mvnTest

A Powerful Test for Multivariate Normality (Zhou-Shao's Test)

Description

A simple and powerful test for multivariate normality with a combination of multivariate kurtosis (MK) and Shapiro-Wilk which was proposed by Zhou and Shao (2014). The p -value of the test statistic (T_n) is computed based on a simulated null distribution of T_n . Details see Zhou and Shao (2014).

Usage

```
mvnTest(X, B = 1000, pct = c(0.01, 0.99))
```

Arguments

X	an $n * p$ data matrix or data frame, where n is number of rows (observations) and p is number of columns (variables) and $n > p$.
B	number of Monte Carlo simulations for null distribution, default is 1000 (increase B to increase the precision of p -value).
pct	percentiles of MK to get c_1 and c_2 described in the reference paper, default is (0.01, 0.99).

Value

Returns a list with two objects:

- `mv.test` results of the Zhou-Shao's test for multivariate normality, i.e., test statistic T_n , p -value (under H_0 , i.e. multivariate normal, that T_n is at least as extreme as the observed value), and multivariate normality summary (YES, if p -value>0.05).
- `uv.shapiro` a dataframe with p rows detailing univariate Shapiro-Wilk tests. Columns in the dataframe contain test statistics W , p -value, and univariate normality summary (YES, if p -value>0.05).

References

Zhou, M., & Shao, Y. (2014). A powerful test for multivariate normality. *Journal of applied statistics*, 41(2), 351-363.

Shapiro, S. S., & Wilk, M. B. (1965). An analysis of variance test for normality (complete samples). *Biometrika*, 52(3/4), 591-611.

See Also

[power.mvnTest](#), [msk](#), [mardia](#), [msw](#), [faTest](#), [mhz](#)

Examples

```
set.seed(12345)

## Data from gamma distribution ##
X = matrix(rgamma(50*4, shape = 2), 50)
mvnTest(X, B=100)

## load the ubiquitous multivariate iris data ##
## (first 50 observations of columns 1:4) ##
iris.df = iris[1:50, 1:4]
mvnTest(iris.df, B=100)
```

power.faTest

Power Calculation using the Fattorini's FA Test Statistic

Description

Empirical power calculation using the Fattorini's FA Test Statistic.

Usage

```
power.faTest(a, n, p, B = 1000, FUN, ...)
```

Arguments

a	significance level (α).
n	number of rows (observations).
p	number of columns (variables), $n > p$.
B	number of Monte Carlo simulations, default is 1000 (can increase B to increase the precision).
FUN	self-defined function for generate multivariate distribution. See example.
...	optional arguments passed to FUN.

Value

Returns a numeric value of the estimated empirical power (value between 0 and 1).

References

Fattorini, L. (1986). Remarks on the use of Shapiro-Wilk statistic for testing multivariate normality. *Statistica*, 46(2), 209-217.

Examples

```
set.seed(12345)

## Power calculation against bivariate (p=2) independent Beta(1, 1) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

power.faTest(a = 0.05, n = 50, p = 2, B = 100, FUN=IMMV, D1=runif)
```

power.mhz

Power Calculation using the Henze-Zirkler Test Statistic

Description

Empirical power calculation using the Henze-Zirkler Test Statistic.

Usage

```
power.mhz(a, n, p, B = 1000, FUN, ...)
```

Arguments

a	significance level (α).
n	number of rows (observations).
p	number of columns (variables), $n > p$.
B	number of Monte Carlo simulations, default is 1000 (can increase B to increase the precision).
FUN	self-defined function for generate multivariate distribution. See example.
...	optional arguments passed to FUN.

Value

Returns a numeric value of the estimated empirical power (value between 0 and 1).

References

Henze, N., & Zirkler, B. (1990). A class of invariant consistent tests for multivariate normality. *Communications in statistics-Theory and Methods*, 19(10), 3595-3617.

Examples

```
set.seed(12345)

## Power calculation against bivariate (p=2) independent Beta(1, 1) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

power.mhz(a = 0.05, n = 50, p = 2, B = 100, FUN=IMMV, D1=runif)
```

power.msk

*Power Calculation using the Bowman and Shenton Test Statistic***Description**

Empirical power calculation using Bowman and Shenton Test Statistic.

Usage

```
power.msk(a, n, p, B = 1000, FUN, ...)
```

Arguments

a	significance level (α).
n	number of rows (observations).
p	number of columns (variables), $n > p$.
B	number of Monte Carlo simulations, default is 1000 (can increase B to increase the precision).
FUN	self-defined function for generate multivariate distribution. See example.
...	optional arguments passed to FUN.

Value

Returns a numeric value of the estimated empirical power (value between 0 and 1).

References

Bowman, K. O., & Shenton, L. R. (1975). Omnibus test contours for departures from normality based on $\sqrt{b_1}$ and b_2 . *Biometrika*, 62(2), 243-250.

Examples

```
set.seed(12345)

## Power calculation against bivariate (p=2) independent Beta(1, 1) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

power.msk(a = 0.05, n = 50, p = 2, B = 100, FUN=IMMV, D1=runif)
```

power.mswR

*Power Calculation using the SWT-based Royston Test Statistic***Description**

Empirical power calculation using Royston test statistic.

Usage

```
power.mswR(a, n, p, B = 1000, FUN, ...)
```

Arguments

a	significance level (α).
n	number of rows (observations).
p	number of columns (variables), $n > p$.
B	number of Monte Carlo simulations, default is 1000 (can increase B to increase the precision).
FUN	self-defined function for generate multivariate distribution. See example.
...	optional arguments passed to FUN.

Value

Returns a numeric value of the estimated empirical power (value between 0 and 1).

References

Royston, J. P. (1982). An extension of Shapiro and Wilk's W test for normality to large samples. *Journal of the Royal Statistical Society: Series C (Applied Statistics)*, 31(2), 115-124.

Examples

```
set.seed(12345)

## Power calculation against bivariate (p=2) independent Beta(1, 1) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

power.mswR(a = 0.05, n = 50, p = 2, B = 100, FUN=IMMV, D1=runif)
```

power.mswV	<i>Power Calculation using the SWT-based Villasenor-Alva and Gonzalez-Estrada (VAGE) Test Statistic</i>
------------	---

Description

Empirical power calculation using VAGE test statistic.

Usage

```
power.mswV(a, n, p, B = 1000, FUN, ...)
```

Arguments

a	significance level (α).
n	number of rows (observations).
p	number of columns (variables), $n > p$.
B	number of Monte Carlo simulations, default is 1000 (can increase B to increase the precision).
FUN	self-defined function for generate multivariate distribution. See example.
...	optional arguments passed to FUN.

Value

Returns a numeric value of the estimated empirical power (value between 0 and 1).

References

Villasenor Alva, J. A., & Estrada, E. G. (2009). A generalization of Shapiro–Wilk’s test for multivariate normality. *Communications in Statistics—Theory and Methods*, 38(11), 1870-1883.

Examples

```
set.seed(12345)

## Power calculation against bivariate (p=2) independent Beta(1, 1) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

power.mswV(a = 0.05, n = 50, p = 2, B = 100, FUN=IMMV, D1=runif)
```

power.mvnTest	<i>Power Calculation using the Zhou-Shao's Multivariate Normality Test Statistic (T_n)</i>
---------------	---

Description

Empirical power calculation using the Zhou-Shao's multivariate normality test Statistic T_n .

Usage

```
power.mvnTest(a, n, p, B = 1000, pct = c(0.01, 0.99), FUN, ...)
```

Arguments

a	significance level (α).
n	number of rows (observations).
p	number of columns (variables), $n > p$.
B	number of Monte Carlo simulations, default is 1000 (can increase B to increase the precision).
pct	percentiles of MK to get c1 and c2 described in the reference paper, default is (0.01, 0.99).
FUN	self-defined function for generate multivariate distribution. See example.
...	optional arguments passed to FUN.

Value

Returns a numeric value of the estimated empirical power (value between 0 and 1).

References

Zhou, M., & Shao, Y. (2014). A powerful test for multivariate normality. *Journal of applied statistics*, 41(2), 351-363.

Examples

```
set.seed(12345)

## Power calculation against bivariate (p=2) independent Beta(1, 1) distribution ##
## at sample size n=50 for  $T_n$  at one-sided alpha = 0.05 ##

power.mvnTest(a = 0.05, n = 50, p = 2, B = 100, pct = c(0.01, 0.99), FUN=IMMV, D1=runif)
```

power.usw

*Power Calculation using the Univariate Shapiro-Wilk Test Statistic***Description**

Empirical power calculation using univariate Shapiro-Wilk test statistic.

Usage

```
power.usw(a, n, p = 1, B = 1000, FUN, ...)
```

Arguments

a	significance level (α).
n	number of rows (observations).
p	p=1 for univariate.
B	number of Monte Carlo simulations, default is 1000 (can increase B to increase the precision).
FUN	self-defined function for generate multivariate distribution. See example.
...	optional arguments passed to FUN.

Value

Returns a numeric value of the estimated empirical power (value between 0 and 1).

References

Shapiro, S. S., & Wilk, M. B. (1965). An analysis of variance test for normality (complete samples). *Biometrika*, 52(3/4), 591-611.

Examples

```
set.seed(12345)

## Power calculation against univariate (p=1) independent Beta(1, 1) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

power.usw(a = 0.05, n = 50, p = 1, B = 100, FUN=IMMV, D1=runif)
```

PSII	<i>Random Generation for the Spherically Symmetric Pearson Type II Distribution</i>
------	---

Description

Generate univariate or multivariate random sample for the spherically symmetric Pearson type II distribution.

Usage

PSII(n, p, s)

Arguments

n	number of rows (observations).
p	number of columns (variables).
s	shape parameter, $s > -1$.

Value

Returns univariate ($p = 1$) or multivariate ($p > 1$) random sample matrix.

References

Kotz, S. (1975). Multivariate distributions at a cross road. In A Modern Course on Statistical Distributions in Scientific Work (pp. 247-270). Springer, Dordrecht.

Henze, N., & Zirkler, B. (1990). A class of invariant consistent tests for multivariate normality. *Communications in statistics-Theory and Methods*, 19(10), 3595-3617.

Examples

```
set.seed(12345)

## Generate 5X2 random sample matrix from PSII(s=1) ##
PSII(n=5, p=2, s=1)

## Power calculation against bivariate (p=2) PSII(s=1) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

# Zhou-Shao's test #
power.mvnTest(a = 0.05, n = 50, p = 2, B = 100, FUN = PSII, s = 1)
```

PSVII	<i>Random Generation for the Spherically Symmetric Pearson Type VII Distribution</i>
-------	--

Description

Generate univariate or multivariate random sample for the spherically symmetric Pearson type VII distribution.

Usage

```
PSVII(n, p, s)
```

Arguments

n	number of rows (observations).
p	number of columns (variables).
s	shape parameter, $s > p/2$.

Value

Returns univariate ($p = 1$) or multivariate ($p > 1$) random sample matrix.

References

Kotz, S. (1975). Multivariate distributions at a cross road. In *A Modern Course on Statistical Distributions in Scientific Work* (pp. 247-270). Springer, Dordrecht.

Henze, N., & Zirkler, B. (1990). A class of invariant consistent tests for multivariate normality. *Communications in statistics-Theory and Methods*, 19(10), 3595-3617.

Examples

```
set.seed(12345)

## Generate 5X2 random sample matrix from PSVII(s=3) ##
PSVII(n=5, p=2, s=3)

## Power calculation against bivariate (p=2) PSVII(s=3) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

# Zhou-Shao's test #
power.mvnTest(a = 0.05, n = 50, p = 2, B = 100, FUN = PSVII, s = 3)
```

SPH

*Random Generation for General Spherically Symmetric Distributions***Description**

Generate univariate or multivariate random sample for general spherically symmetric distributions.

Usage

```
SPH(n, p, D, ...)
```

Arguments

n	number of rows (observations).
p	number of columns (variables).
D	random generation functions for some distributions (e.g., rgamma, rbeta).
...	optional arguments passed to D.

Value

Returns univariate ($p = 1$) or multivariate ($p > 1$) random sample matrix.

References

Chmielewski, M. A. (1981). Elliptically symmetric distributions: A review and bibliography. *International Statistical Review/Revue Internationale de Statistique*, 67-74.

Henze, N., & Zirkler, B. (1990). A class of invariant consistent tests for multivariate normality. *Communications in statistics-Theory and Methods*, 19(10), 3595-3617.

Examples

```
set.seed(12345)

## Generate 5X2 random sample matrix from SPH(Beta(1,1)) ##
SPH(n=5, p=2, D=rbeta, shape1=1, shape2=1)

## Power calculation against bivariate (p=2) SPH(Beta(1,1)) distribution ##
## at sample size n=50 at one-sided alpha = 0.05 ##

# Zhou-Shao's test #
power.mvnTest(a=0.05, n=50, p=2, B=100, FUN=SPH, D=rbeta, shape1=1, shape2=1)
```

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