Package 'nicheROVER'

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Title Niche Region and Niche Overlap Metrics for Multidimensional Ecological Niches

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Description Implementation of a probabilistic method to calcu-

late 'nicheROVER' (_niche__r_egion and niche _over_lap) metrics using multidimensional niche indicator data (e.g., stable isotopes, environmental variables, etc.). The niche region is defined as the joint probability density function of the multidimensional niche indicators at a user-defined probability alpha (e.g., 95%). Uncertainty is accounted for in a Bayesian framework, and the method can be extended to three or more indicator dimensions. It provides directional estimates of niche overlap, accounts for speciesspecific distributions in multivariate niche space, and produces unique and consistent bivariate projections of the multivariate niche region. The article by Swanson et al. (2015) <doi:10.1890/14-0235.1> provides a detailed description of the methodology. See the package vignette for a worked example using fish stable isotope data.

URL https://github.com/mlysy/nicheROVER

BugReports https://github.com/mlysy/nicheROVER/issues **Depends** R (>= 1.9.0) Imports graphics, stats, utils Suggests knitr, rmarkdown VignetteBuilder knitr License GPL-3 LazyData true **Encoding** UTF-8 RoxygenNote 7.2.3 NeedsCompilation no Author Martin Lysy [aut, cre], Ashley D. Stasko [aut], Heidi K. Swanson [aut] Maintainer Martin Lysy <mlysy@uwaterloo.ca> **Repository** CRAN Date/Publication 2023-10-13 16:10:02 UTC

R topics documented:

nicheROVER-package	2
ellipse	4
fish	5
niche.par.plot	5
niche.plot	7
niche.runif	9
niche.size	10
niiw.post	10
niw.coeffs	
niw.mom	14
niw.post	
overlap	
overlap.plot	
overlap.unif	
rniw	
rwish	23
	25

Index

nicheROVER-package

(Niche) (R)egion and Niche (Over)lap Metrics for Multidimensional Ecological Niches.

Description

This package uses a probabilistic method to calculate niche regions and pairwise niche overlap using multidimensional niche indicator data (e.g., stable isotopes, environmental variables, etc.). The niche region is defined as the joint probability density function of the multidimensional niche indicators at a user-defined probability alpha (e.g., 95%). Uncertainty is accounted for in a Bayesian framework, and the method can be extended to three or more indicator dimensions. It provides directional estimates of niche overlap, accounts for species-specific distributions in multivariate niche space, and produces unique and consistent bivariate projections of the multivariate niche region. See Swanson et al. (2014) for a detailed description and worked example below using fish stable isotope data.

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References

Swanson, H.K., Lysy, M., Stasko, A.D., Power, M., Johnson, J.D., and Reist, J.D. "A new probabilistic method for quantifying n-dimensional ecological niches and niche overlap." *Ecology: Statistical Reports* 96:2 (2015): 318-324. doi:10.1890/140235.1.

See Also

Useful links:

- https://github.com/mlysy/nicheROVER
- Report bugs at https://github.com/mlysy/nicheROVER/issues

```
# analysis for fish data
data(fish) # 4 fish, 3 isotopes
aggregate(fish[2:4], fish[1], mean) # isotope means per fish
# random draws from posterior distribution with default prior
nsamples <- 500
fish.par <- tapply(1:nrow(fish), fish$species,</pre>
                   function(ii) niw.post(nsamples = nsamples, X = fish[ii,2:4]))
# display p(mu | X) and p(Sigma | X) for each fish
clrs <- c("black", "red", "blue", "orange") # colors for each species</pre>
par(mar = c(4.2, 4.2, 2, 1)+.1)
niche.par.plot(fish.par, col = clrs)
legend(x = "topright", legend = names(fish.par), fill = clrs)
# 2-d projections of 10 niche regions
nsamples <- 10
fish.par <- tapply(1:nrow(fish), fish$species,</pre>
                   function(ii) niw.post(nsamples = nsamples, X = fish[ii,2:4]))
# format data for plotting function
fish.data <- tapply(1:nrow(fish), fish$species, function(ii) X = fish[ii,2:4])</pre>
niche.plot(niche.par = fish.par, niche.data = fish.data, pfrac = .05,
           iso.names = expression(delta^{15}*N, delta^{13}*C, delta^{34}*S),
           col = clrs, xlab = expression("Isotope Ratio (per mille)"))
# niche overlap plots for 95% niche region sizes
# overlap calculation. use nsamples = nprob = 1e4 for higher accuracy.
nsamples <- 500
over.stat <- overlap(fish.par, nreps = nsamples, nprob = nsamples, alpha = .95)
# overlap plot
overlap.plot(over.stat, col = clrs, mean.cred.col = "turquoise",
             equal.axis = TRUE,
             xlab = "Overlap Probability (%) -- Niche Region Size: 95%")
```

ellipse

Description

Calculates coordinates of points for plotting a 2-dimensional ellipse based on user-defined parameters. Can be used for exploratory data analysis to produce ellipses at a given niche region size (e.g., $\alpha = 95\%$).

Usage

ellipse(mu, V, alpha = 0.95, n = 100)

Arguments

mu	Centre of ellipse. A vector of length 2.
V	Scale of ellipse. A 2x2 matrix. See 'Details'.
alpha	Niche region size. See 'Details'.
n	Number of points to return for plotting.

Details

This function provides the coordinates needed to plot a 2-dimensional ellipse based on user-defined parameters, such that X = c(x, y) satisfies the equation

$$(X - \mu)' V^{-1} (X - \mu) = C,$$

where $C = \operatorname{qchisq}(\operatorname{alpha}, \operatorname{df} = 2)$.

Value

Returns a matrix of coordinates cbind(x,y) to plot a 2-dimensional ellipse.

See Also

niche.plot() for plotting.

```
mu <- rnorm(2)
V <- crossprod(matrix(rnorm(4), 2, 2))
ell.pts <- ellipse(mu = mu, V = V, alpha = .9, n = 100)
plot(ell.pts, col = rainbow(110)[1:100], type = "o")
points(mu[1], mu[2], pch = "+")
```

fish

Description

A dataset containing values for three stable isotopes measured in the muscle tissue of four species of arctic fish. For use in examples.

Usage

fish

Format

A data frame with 278 rows (observations) and 4 columns (species, $\delta^{15}N$, $\delta^{13}C$, and $\delta^{34}S$).

Details

This dataset contains $\delta^{15}N$, $\delta^{13}C$, and $delta^{34}S$ values for the following fish species:

- ARCS Arctic Cisco (*Coregonus autumnalis*), n = 69.
- BDWF Broad Whitefish (*Coregonus nasus*), n = 71.
- LKWF Lake Whitefish (*Coregonus clupeaformis*), n = 67.
- LSCS Least Cisco (Coregonus sardinella), n = 70

Source

Fish were collected between 2007 and 2008 from an estuarine area of the Beaufort Sea, North and West of the Mackenzie Delta at Phillips Bay, Yukon Territory, Canada (69.28 N, 138.49 W).

Examples

```
head(fish)
aggregate(fish[2:4], fish[1], mean)
```

niche.par.plot Plot for niche parameters.

Description

For one or more species, plots some or all of the niche parameters μ and Σ .

Usage

```
niche.par.plot(
    niche.par,
    plot.mu = TRUE,
    plot.Sigma = TRUE,
    plot.index,
    col,
    ndens = 512,
    ylab
)
```

Arguments

niche.par	List with nspecies = length(niche.par), each element of which is a list with parameters mu and Sigma. See 'Details'.
plot.mu	Logical. If TRUE, plot the distribution of μ for each niche indicator (e.g., stable isotope). See 'Details'.
plot.Sigma	Logical. If TRUE, plot the distribution of Σ for each niche indicator. See 'Details'.
plot.index	Either a scalar of a numeric vector of length 2. If plot.index = i then plot the distribution of μ_i . If plot.index = c(i,j) then plot the distribution of Σ_{ij} .
col	Vector of colors in which to plot each species.
ndens	Number of points at which to evaluate density estimates.
ylab	Optional label for y-axis. If missing, defaults to $p(\mu_i X)$ and $p(\Sigma_{ij} X)$.

Details

Each element of the list niche.par is a distribution of niche parameters. That is, names(niche.par[[1]]) = c("mu", "Sigma"), and if niso is the number of niche indicators (e.g., stable isotopes), then dim(niche.par[[1]]\$mu) = c(nsamples, niso) and dim(niche.par[[1]]\$Sigma) = c(niso, niso, nsamples).

Value

Returns a plot of the distribution of some or all niche parameters.

See Also

niw.post(), niiw.post() for niche parameter output, stats::density() for density estimation
from sample data.

Examples

fish data
data(fish)

```
\# generate parameter draws from the "default" posteriors of each fish nsamples <- 1e3
```

6

niche.plot

```
system.time({
  fish.par <- tapply(1:nrow(fish), fish$species,</pre>
                     function(ii) niw.post(nsamples = nsamples, X = fish[ii,2:4]))
})
# various parameter plots
clrs <- c("black", "red", "blue", "orange") # colors for each species</pre>
# mu1, mu2, and Sigma12
par(mar = c(4, 4, .5, .1)+.1, mfrow = c(1,3))
niche.par.plot(fish.par, col = clrs, plot.index = 1)
niche.par.plot(fish.par, col = clrs, plot.index = 2)
niche.par.plot(fish.par, col = clrs, plot.index = 1:2)
legend("topright", legend = names(fish.par), fill = clrs)
# all mu
niche.par.plot(fish.par, col = clrs, plot.mu = TRUE, plot.Sigma = FALSE)
legend("topright", legend = names(fish.par), fill = clrs)
# all mu and Sigma
par(mar = c(4.2, 4.2, 2, 1)+.1)
niche.par.plot(fish.par, col = clrs, plot.mu = TRUE, plot.Sigma = TRUE)
legend("topright", legend = names(fish.par), fill = clrs)
```

niche.plot

```
Plot for 2-d projection of niche regions.
```

Description

For one or more species, creates a series of plots: (i) the raw niche indicators (e.g., stable isotope) data, (ii) their density estimates, and (iii) 2-dimensional projections of probabilistic niche regions based on *n*-dimensional data.

Usage

```
niche.plot(
   niche.par,
   niche.data,
   alpha = 0.95,
   species.names,
   iso.names,
   lims,
   col,
   ndens = 512,
   pfrac = 0,
   xlab,
   legend = TRUE
)
```

Arguments

niche.par	A list of length nspecies, each element of which in turn is a list with elements mu and Sigma. Each of these will correspond to an ellipse being drawn for that species in the corresponding 2-d plane. See 'Example'.
niche.data	A list of length nspecies, each element of which is a matrix with observations along the rows and niche indicators (e.g., stable isotopes) along the columns.
alpha	Size of the niche region to plot. Defaults to 0.95.
species.names	Names of the species. Defaults to names(niche.par).
iso.names	Names of the niche indicators (or isotopes) to plot. Defaults to colnames(niche.par)
lims	Two-row matrix of range limits for each niche indicator. Defaults to include all ellipses.
col	Vector of colours in which each species will be drawn.
ndens	Number of points at which to evaluate kernel density estimates.
pfrac	Fraction of the plot on which to display 1-dimensional raw niche indicator data. pfrac = 0 means don't display the raw data in 1-d.
xlab	Title of plot, located on the bottom. Defaults to no title.
legend	Whether or not to add a legend. Defaults to TRUE.

Details

A set of plots is created for each pairwise combination of niche indicators. Below the diagonal are scatterplots for each species, above the diagonal are ellipses corresponding to 2-d projections of the probabilistic niche regions. The diagonal displays density estimates for each indicator, and optionally the raw 1-d data. See Swanson et al. (2015) for detailed description of the probabilistic niche region.

Value

Returns a series of plots displaying niche indicator data and their probabilistic niche projections.

References

Swanson, H.K., Lysy, M., Stasko, A.D., Power, M., Johnson, J.D., and Reist, J.D. "A new probabilistic method for quantifying n-dimensional ecological niches and niche overlap." *Ecology: Statistical Reports* 96:2 (2015): 318-324. doi:10.1890/140235.1.

See Also

overlap.plot(), niw.post(), niiw.post().

Examples

data(fish) # 4 fish, 3 isotopes

generate 10 parameter draws from the posteriors
of each fish with default prior

niche.runif

niche.runif Uniform sampling from an elliptical niche region.

Description

Uniform sampling from an elliptical niche region.

Usage

niche.runif(n, mu, Sigma, alpha = 0.95)

Arguments

n	Number of random draws.
mu	Mean vector.
Sigma	Variance matrix.
alpha	Probabilistic niche size

Value

IID draws from a uniform distribution on the elliptical niche region.

See Also

ellipse() and niche.size() for the definition of the elliptical niche region.

```
# 2d example
d <- 2 # number of dimensions
V <- crossprod(matrix(rnorm(4),d,d))
mu <- rnorm(d)
plot(ellipse(mu, V), type = "1")
points(niche.runif(1e4, mu, V), col = "brown", pch = ".")
```

niche.size

Description

Calculate the size of an elliptical niche region.

Usage

```
niche.size(Sigma, alpha = 0.95)
```

Arguments

Sigma	Variance matrix for normally distributed niche axes.
alpha	Probabilistic niche size.

Details

For a given niche region N_R , the niche size is defined as the hypervolume of this region: $N_S = \int_{x \in N_R} dx$.

Value

Hypervolume niche size.

Examples

```
# for each species, size of 95% niche region using sample variance
tapply(1:nrow(fish), fish$species, function(ind) {
  X <- fish[ind,2:4] # all measurements for given species
  Sighat <- var(X) # sample variance
  niche.size(Sigma = Sighat, alpha = .95)
})
```

niiw.post

Random draws from the posterior distribution with Normal-Independent-Inverse-Wishart (NIIW) prior.

Description

Given iid *d*-dimensional niche indicators $X = (X_1, \ldots, X_N)$ with $X_i \sim N(\mu, \Sigma)$, this function generates random draws from $p(\mu, \Sigma | X)$ for the Normal-Independent-Inverse-Wishart (NIIW) prior.

Usage

```
niiw.post(nsamples, X, lambda, Omega, Psi, nu, mu0 = lambda, burn)
```

niiw.post

Arguments

nsamples	The number of posterior draws.
Х	A data matrix with observations along the rows.
lambda	Mean of μ . See 'Details'.
Omega	Variance of μ . Defaults to Omega = 0. See 'Details'.
Psi	Scale matrix of Σ . Defaults to Psi = 0. See 'Details'.
nu	Degrees of freedom of Σ . Defaults to nu = ncol(X)+1. See 'Details'.
mu0	Initial value of μ to start the Gibbs sampler. See 'Details'.
burn	Burn-in for the MCMC sampling algorithm. Either an integer giving the number of initial samples to discard, or a fraction with $0 < burn < 1$. Defaults to burn = floor(nsamples/10).

Details

The NIIW distribution $p(\mu, \Sigma | \lambda, \kappa, \Psi, \nu)$ is defined as

$$\Sigma \sim W^{-1}(\Psi, \nu), \quad \mu | \Sigma \sim N(\lambda, \Omega).$$

The default value Omega = 0 uses the Lebesque prior on μ : $p(\mu) \propto 1$. In this case the NIW and NIIW priors produce identical resuls, but niw.post() is faster.

The default value Psi = 0 uses the scale-invariant prior on Σ : $p(\Sigma) \propto |\Sigma|^{-(\nu+d+1)/2}$.

The default value nu = ncol(X)+1 for Omega = 0 and Psi = 0 makes $E[\mu|X] = `colMeans(X)`$ and $E[\Sigma|X] = `var(X)`$.

Random draws are obtained by a Markov chain Monte Carlo (MCMC) algorithm; specifically, a Gibbs sampler alternates between draws from $p(\mu|\Sigma, X)$ and $p(\Sigma|\mu, X)$, which are Normal and Inverse-Wishart distributions respectively.

Value

Returns a list with elements mu and Sigma of sizes c(nsamples, length(lambda)) and c(dim(Psi), nsamples).

See Also

niw.post(), rwish().

```
# simulate normal data with mean and variance (mu0, Sigma0)
d <- 4
mu0 <- rnorm(d)
Sigma0 <- matrix(rnorm(d^2), d, d)
Sigma0 <- Sigma0 %*% t(Sigma0)
N <- 1e2
X <- matrix(rnorm(N*d), N, d) # iid N(0,1)
X <- t(t(X %*% chol(Sigma0)) + mu0) # each row is N(mu0, Sigma)</pre>
```

```
# prior parameters
# flat prior on mu
lambda <- 0
Omega <- 0
# informative prior on Sigma
Psi <- crossprod(matrix(rnorm(d^2), d, d))</pre>
nu <- 5
# sample from NIIW posterior
nsamples <- 2e3
system.time({
  siiw <- niiw.post(nsamples, X, lambda, Omega, Psi, nu, burn = 100)</pre>
})
# sample from NIW posterior
kappa <- 0
system.time({
  siw <- niw.post(nsamples, X, lambda, kappa, Psi, nu)</pre>
})
# check that posteriors are the same
# p(mu | X)
clrs <- c("black", "red")</pre>
par(mar = c(4.2, 4.2, 2, 1)+.1)
niche.par.plot(list(siiw, siw), col = clrs, plot.mu = TRUE, plot.Sigma = FALSE)
legend(x = "topright", legend = c("NIIW Prior", "NIW Prior"), fill = clrs)
# p(Sigma | X)
par(mar = c(4.2, 4.2, 2, 1)+.1)
niche.par.plot(list(siiw, siw), col = clrs, plot.mu = FALSE, plot.Sigma = TRUE)
legend(x = "topright", legend = c("NIIW Prior", "NIW Prior"), fill = clrs)
```

```
niw.coeffs
```

Posterior coefficients of the Normal-Inverse-Wishart distribution with its conjugate prior.

Description

Given iid *d*-dimensional niche indicators $X = (X_1, \ldots, X_N)$ with $X_i \sim N(\mu, \Sigma)$, this function calculates the coefficients of the Normal-Inverse-Wishart (NIW) posterior $p(\mu, \Sigma|X)$ for a conjugate NIW prior. Together with niw.mom(), this can be used to rapidly compute the point estimates $E[\mu|X]$ and $E[\Sigma|X]$.

Usage

niw.coeffs(X, lambda, kappa, Psi, nu)

12

niw.coeffs

Arguments

Х	A data matrix with observations along the rows.
lambda	Location parameter. See 'Details'.
kappa	Scale parameter. Defaults to kappa = 0. See 'Details'.
Psi	Scale matrix. Defaults to Psi = 0. See 'Details'.
nu	Degrees of freedom. Defaults to $nu = ncol(X)+1$. See 'Details'.

Details

The NIW distribution $p(\mu, \Sigma | \lambda, \kappa, \Psi, \nu)$ is defined as

$$\Sigma \sim W^{-1}(\Psi, \nu), \quad \mu | \Sigma \sim N(\lambda, \Sigma/\kappa).$$

The default value kappa = 0 uses the Lebesque prior on μ : $p(\mu) \propto 1$.

The default value Psi = 0 uses the scale-invariant prior on Σ : $p(\Sigma) \propto |\Sigma|^{-(\nu+d+1)/2}$.

The default value nu = ncol(X)+1 for kappa = 0 and Psi = 0 makes $E[\mu|X] = 'colMeans(X)'$ and $E[\Sigma|X] = 'var(X)'$.

Value

Returns a list with elements lambda, kappa, Psi, nu corresponding to the coefficients of the NIW posterior distribution $p(\mu, \Sigma | X)$.

See Also

rniw(), niw.mom(), niw.post().

```
# NIW prior coefficients
d <- 3
lambda <- rnorm(d)</pre>
kappa <- 5
Psi <- crossprod(matrix(rnorm(d^2), d, d))</pre>
nu <- 10
# data
data(fish)
X <- fish[fish$species == "ARCS",2:4]</pre>
# NIW posterior coefficients
post.coef <- niw.coeffs(X, lambda, kappa, Psi, nu)</pre>
# compare
mu.mean <- niw.mom(post.coef$lambda, post.coef$kappa, post.coef$Psi, post.coef$nu)$mu$mean</pre>
mu.est <- rbind(prior = niw.mom(lambda, kappa, Psi, nu)$mu$mean,</pre>
                 data = colMeans(X),
                 post = mu.mean)
round(mu.est, 2)
```

niw.mom

Description

This function computes the mean and variance of the Normal-Inverse-Wishart (NIW) distribution. Can be used to very quickly compute Bayesian point estimates for the conjugate NIW prior.

Usage

niw.mom(lambda, kappa, Psi, nu)

Arguments

lambda	Location parameter. See 'Details'.
kappa	Scale parameter. See 'Details'.
Psi	Scale matrix. See 'Details'.
nu	Degrees of freedom. See 'Details'.

Details

The NIW distribution $p(\mu, \Sigma | \lambda, \kappa, \Psi, \nu)$ is defined as

$$\Sigma \sim W^{-1}(\Psi, \nu), \quad \mu | \Sigma \sim N(\lambda, \Sigma/\kappa).$$

Note that $cov(\mu, \Sigma) = 0$.

Value

Returns a list with elements mu and Sigma, each containing lists with elements mean and var. For mu these elements are of size length(lambda) and c(length(lambda),length(lambda)). For Sigma they are of size dim(Psi) and c(dim(Psi), dim(Psi)), such that $cov(\Sigma_{ij}, \Sigma_{kl}) = Sigmavr[i, j, k, l]$.

See Also

rniw(), niw.coeffs(), niw.post().

```
# NIW parameters
d <- 3 # number of dimensions
lambda <- rnorm(d)
kappa <- 2
Psi <- crossprod(matrix(rnorm(d^2), d, d))
nu <- 10
# simulate data
niw.sim <- rniw(n = 1e4, lambda, kappa, Psi, nu)</pre>
```

niw.post

```
# check moments
niw.mV <- niw.mom(lambda, kappa, Psi, nu)
# mean of mu
ii <- 1
c(true = niw.mV$mu$mean[ii], sim = mean(niw.sim$mu[,ii]))
# variance of Sigma
II <- c(1,2)
JJ <- c(2,3)
c(true = niw.mV$var[II[1],II[2],JJ[1],JJ[2]],
    sim = cov(niw.sim$Sigma[II[1],II[2],], niw.sim$Sigma[JJ[1],JJ[2],]))
```

niw.post	Random draws from the posterior distribution with Normal-Inverse-
	Wishart (NIW) prior.

Description

Given iid *d*-dimensional niche indicators $X = (X_1, ..., X_N)$ with $X_i \sim N(\mu, \Sigma)$, this function generates random draws from $p(\mu, \Sigma | X)$ for the Normal-Inverse-Wishart (NIW) prior.

Usage

```
niw.post(nsamples, X, lambda, kappa, Psi, nu)
```

Arguments

nsamples	The number of posterior draws.
Х	A data matrix with observations along the rows.
lambda	Location parameter. See 'Details'.
kappa	Scale parameter. Defaults to kappa = 0. See 'Details'.
Psi	Scale matrix. Defaults to Psi = 0. See Details.
nu	Degrees of freedom. Defaults to nu = ncol(X)+1. See Details.

Details

The NIW distribution $p(\mu, \Sigma | \lambda, \kappa, \Psi, \nu)$ is defined as

 $\Sigma \sim W^{-1}(\Psi, \nu), \quad \mu | \Sigma \sim N(\lambda, \Sigma/\kappa).$

The default value kappa = 0 uses the Lebesque prior on μ : $p(\mu) \propto 1$.

The default value Psi = 0 uses the scale-invariant prior on Σ : $p(\Sigma) \propto |\Sigma|^{-(\nu+d+1)/2}$.

The default value nu = ncol(X)+1 for kappa = 0 and Psi = 0 makes $E[\mu|X] = \text{colMeans}(X)$ and $E[\Sigma|X] = \text{var}(X)$.

Value

Returns a list with elements mu and Sigma of sizes c(nsamples, length(lambda)) and c(dim(Psi), nsamples).

See Also

rniw(), niiw.post().

```
# compare the default non-informative prior to an arbitrary informative prior
# for simulated data
# simulate normal data with mean and variance (mu0, Sigma0)
d <- 4
mu0 <- rnorm(d)
Sigma0 <- matrix(rnorm(d^2), d, d)</pre>
Sigma0 <- Sigma0 %*% t(Sigma0)</pre>
N <- 1e2
X <- matrix(rnorm(N*d), N, d) # iid N(0,1)</pre>
X <- t(t(X %*% chol(Sigma0)) + mu0) # each row is N(mu0, Sigma)</pre>
# informative prior parameters
lambda <- rnorm(d)</pre>
kappa <- 20
Psi <- crossprod(matrix(rnorm(d^2), d, d))</pre>
nu <- 5
# iid draws from informative prior pi(mu, Sigma)
nsamples <- 2e3
siw0 <- rniw(nsamples, lambda, kappa, Psi, nu)</pre>
# iid draws from posterior p(mu, Sigma | X) with informative prior
siw1 <- niw.post(nsamples, X, lambda, kappa, Psi, nu)</pre>
# iid draws from posterior p(mu, Sigma | X) with default noninformative prior
siw2 <- niw.post(nsamples, X)</pre>
# compare
# prior and posterior densities of mu
clrs <- c("orange", "red", "blue", "black")</pre>
ii <- 1
par(mar = c(4.2, 4.2, 2, 1)+.1)
niche.par.plot(list(siw0, siw1, siw2), col = clrs[1:3],
               plot.index = ii, ylab = "Density")
abline(v = mu0[ii], col = clrs[4]) # true value of mu
legend(x = "topright",
       legend = c(parse(text = paste0("pi(mu[", ii, "])")),
                parse(text = paste0("p(mu[", ii, "]*\" | \"*X)*\", Informative Prior\"")),
             parse(text = paste0("p(mu[", ii, "]*\" | \"*X)*\", Noninformative Prior\"")),
                   parse(text = paste0("\"True value of \"*mu[", ii, "]"))),
```

overlap

```
overlap
```

Monte Carlo calculation of niche region overlap metrics.

Description

Calculates the distribution of a niche region overlap metric for each pairwise species combination and user-specified niche region sizes.

Usage

```
overlap(
  niche.par,
  nreps,
  nprob,
  alpha = 0.95,
  species.names,
  norm.redraw = TRUE
)
```

Arguments

niche.par	A list with nspecies = length(niche.par), each element of which in turn is a list with elements mu and Sigma. See Details.
nreps	The number of overlap metric calculations for each species. Defaults to the smallest number of parameter samples supplied by niche.par. See 'Details'.
nprob	The number of normal draws for each Monte Carlo overlap metric calculation. See 'Details'.
alpha	Scalar or vector of niche region sizes for calculating the niche overlap metric. Defaults to 0.95.

overlap

species.names	Names of the species. Defaults to names(niche.par).
norm.redraw	Logical. If FALSE, the same nprob*nspecies iid ${\cal N}(0,1)$ draws are used for
	each calculation of the overlap metric. This increases the Monte Carlo error, but
	the procedure is about 1.5x faster. Defaults to TRUE.

Details

The overlap metric is the probability that a randomly drawn individual from species A will be found within the niche region of species B (for a given niche region size, e.g., alpha = .95). It is a single number which is a function of the parameters for each species, $\Theta_A = (\mu_A, \Sigma_A)$ and $\Theta_B = (\mu_B, \Sigma_B)$. This number is difficult to calculate directly, but easy to approximate stochastically by generating nprob draws from the distribution of species A and counting the fraction of them which fall in the niche region of species B.

Typically the true values of Θ_A and Θ_B are unknown and must be estimated from the data. Thus, the overlap metric is calculated for nreps combinations of samples from $p(\Theta_A|X)$ and $p(\Theta_B|X)$ which are supplied in niche.par.

See Swanson et al. (2015) for a detailed description of niche overlap and its calculation.

Value

Returns an array of size c(nspecies, nspecies, nreps, nlevels), where nlevels is the number of alpha levels at which to calculate the overlap metric. For each of the last two dimensions of the output array, the first two dimensions form an nspecies by nspecies matrix giving each pairwise calculation of overlap metric between two species for given Θ_A , Θ_B , and alpha. In each of these matrices, Species A is along the rows of this matrix and Species B is along the columns.

References

Swanson, H.K., Lysy, M., Stasko, A.D., Power, M., Johnson, J.D., and Reist, J.D. "A new probabilistic method for quantifying n-dimensional ecological niches and niche overlap." *Ecology: Statistical Reports* 96:2 (2015): 318-324. doi:10.1890/140235.1.

See Also

overlap.plot(), niw.post(), niiw.post().

overlap.plot

overlap.plot *Plot the overlap metric.*

Description

Plots the posterior distribution of the niche region overlap metric calculated for each pairwise combination of species.

Usage

```
overlap.plot(
   over.stat,
   nbreaks = 50,
   equal.axis = FALSE,
   species.names,
   col,
   mean.cred = TRUE,
   mean.cred.col = "green",
   xlab
)
```

Arguments

over.stat	An array with dim(over.stat) = c(nspecies, nspecies, nreps) containing nreps calculations of the overlap metric for each pair of species. See 'Details'.
nbreaks	Number of breaks in the histogram. Defaults to 50.
equal.axis	Logical. If TRUE, all histograms in a given column of the output (corresponding to different Species A for the same Species B) are plotted on the same range.
species.names	A vector of species names. Defaults to dimnames(over.stat)[[1]].
col	A vector of the colours in which each species will be drawn.
mean.cred	Logical. If TRUE, vertical lines for mean and 95% credible intervals will be included in the historgram of each overlap metric.
mean.cred.col	Colour of the mean and credible interval lines in the histogram.
xlab	Optional plot title, located on the bottom. Default is no title.

Details

This function uses the overlap metric information in over.stat calculated by overlap() to create 2-dimensional plots of interspecific niche region overlap.

Value

Returns a series of histograms illustrating the probability of pairwise species overlap.

See Also

```
overlap(), niw.post(), niiw.post().
```

Examples

```
# fish data
data(fish)
# parameter draws from the "default" posteriors of each fish
nsamples <- 500
system.time({
 fish.par <- tapply(1:nrow(fish), fish$species,</pre>
                     function(ii) niw.post(nsamples = nsamples,
                                            X = fish[ii,2:4]))
})
# overlap calculation
system.time({
 over <- overlap(fish.par, nreps = nsamples, nprob = nsamples,</pre>
                  alpha = c(.95, .99))
})
# overlap plot
clrs <- c("black", "red", "blue", "orange") # color for each species</pre>
ii <- 1 # which niche region alpha level to use
overlap.plot(over[,,,ii], col = clrs, mean.cred.col = "turquoise",
             xlab = paste0("Overlap Probability (%) -- Niche Region Size: ",
                            dimnames(over)[[4]][ii]))
```

```
overlap.unif Overlap calculation for uniform niche regions.
```

Description

Overlap calculation for uniform niche regions.

Usage

```
overlap.unif(muA, SigmaA, muB, SigmaB, alphaA = 0.95, alphaB = 0.95, nprob)
overlap.sphere(muA, sigmaA, muB, sigmaB, alphaA = 0.95, alphaB = 0.95)
```

20

overlap.unif

Arguments

muA, muB	Mean of niche regions.
SigmaA, SigmaB	Variance matrix of elliptical niche regions.
alphaA, alphaB	Probabilistic size of niche regions.
nprob	Number of uniform draws from niche region A.
sigmaA, sigmaB	standard deviations (scalars) of spherical niche regions.

Details

The overlap between niche regions A and B is defined as $vol(A \cap B)/vol(A \cup B)$, where the hypervolume of an n-dimensional region S is $vol(S) = \int_S dx$. For elliptical niche regions, there are simple formulas for vol(A) and vol(B). Thus, we need only determine the volume of the intersection $vol(A \cap B)$, as the volume of the union is given by the formula $vol(A \cup B) = vol(A) + vol(B) - vol(A \cap B)$.

For spherical niche regions, $vol(A \cap B)$ has a closed-form expression (see 'References'). For elliptical regions, no such formula exists and a Monte Carlo method is used instead. That is, $vol(A \cap B)$ is calculated by sampling uniformly from A, then multiplying vol(A) by the fraction of sampled points which fall into B.

While the uniform overlap metric is invariant to permutation of niche regions A and B, the accuracy of the Monte Carlo calculation of $vol(A \cap B)$ is not: higher accuracy is obtained when a higher fraction of sampled points are in the opposite niche region. overlap.unif() does not attempt to determine for which region this is the case, though the choice can be informed by plotting the niche regions, e.g., with niche.plot().

Value

A Monte Carlo estimate of the niche overlap for overlap.unif(), and an analytic calculation for overlap.sphere().

References

Li, S. "Concise formulas for the area and volume of a hyperspherical cap." *Asian Journal of Mathematics & Statistics* 4.1 (2011): 66-70. doi:10.3923/ajms.2011.66.70.

Examples

spherical case: compare Monte Carlo method to analytic formula

```
d <- 2 # 2D example
mA <- rnorm(d)
mB <- rnorm(d)
sigA <- rexp(1)
SigA <- sigA^2 * diag(d)
sigB <- rexp(1)
SigB <- sigB^2 * diag(d)
# plot circles
ellA <- ellipse(mA, SigA)</pre>
```

```
ellB <- ellipse(mB, SigB)
plot(0, type = "n",
    xlim = range(ellA[,1], ellB[,1]),
    ylim = range(ellA[,2], ellB[,2]), xlab = "x", ylab = "y")
lines(ellA, col = "red")
lines(ellB, col = "blue")
legend("topright", legend = c("niche A", "niche B"),
    fill = c("red", "blue"), bg = "white")
# compare niche calculations
overlap.sphere(mA, sigA, mB, sigB)
overlap.unif(mA, SigA, mB, SigB, nprob = 1e5)</pre>
```

rniw

Random draws from a Normal-Inverse-Wishart distribution.

Description

Generates random draws from a Normal-Inverse-Wishart (NIW) distribution. Can be used to compare prior to posterior parameter distributions.

Usage

rniw(n, lambda, kappa, Psi, nu)

Arguments

n	Number of samples to draw.
lambda	Location parameter. See 'Details'.
kappa	Scale parameter. See 'Details'.
Psi	Scale matrix. See 'Details'.
nu	Degrees of freedom. See 'Details'.

Details

The NIW distribution $p(\mu, \Sigma | \lambda, \kappa, \Psi, \nu)$ is defined as

$$\Sigma \sim W^{-1}(\Psi, \nu), \quad \mu | \Sigma \sim N(\lambda, \Sigma/\kappa).$$

Value

Returns a list with elements mu and Sigma of sizes c(n, length(lambda)) and c(nrow(Psi), ncol(Psi), n).

See Also

rwish(), niw.mom(), niw.coeffs().

22

rwish

Examples

```
d <- 4 # number of dimensions
nu <- 7 # degrees of freedom
Psi <- crossprod(matrix(rnorm(d^2), d, d)) # scale</pre>
lambda <- rnorm(d)</pre>
kappa <- 2
n <- 1e4
niw.sim <- rniw(n, lambda, kappa, Psi, nu)</pre>
# diagonal elements of Sigma^{-1} are const * chi^2
S <- apply(niw.sim$Sigma, 3, function(M) diag(solve(M)))</pre>
ii <- 2
const <- solve(Psi)[ii,ii]</pre>
hist(S[ii,], breaks = 100, freq = FALSE,
     main = parse(text = paste0("\"Histogram of \"*(Sigma^{-1})[", ii,ii,"]")),
     xlab = parse(text = paste0("(Sigma^{-1})[", ii,ii,"]")))
curve(dchisq(x/const, df = nu)/const,
      from = min(S[ii,]), to = max(S[ii,]), col = "red", add = TRUE)
# elements of mu have a t-distribution
mu <- niw.sim$mu
ii <- 4
const <- sqrt(Psi[ii,ii]/(kappa*(nu-d+1)))</pre>
hist(mu[,ii], breaks = 100, freq = FALSE,
     main = parse(text = paste0("\"Histogram of \"*mu[", ii, "]")),
     xlab = parse(text = paste0("mu[", ii, "]")))
curve(dt((x-lambda[ii])/const, df = nu-d+1)/const, add = TRUE, col = "red")
```

rwish

Random draws from a Wishart (or Inverse-Wishart) distribution.

Description

Generates a random samples from a Wishart distribution defined as $W(\Psi, \nu)$, or an Inverse-Wishart distribution defined as $W^{-1}(\Psi, \nu)$.

Usage

rwish(n, Psi, nu, inv = FALSE)

Arguments

n	Number of samples to draw.
Psi	Scale matrix.
nu	Degrees of freedom.
inv	Logical. Setting inv = TRUE returns random matrices from an Inverse-Wishart distribution. See 'Details'.

Details

Setting inv = TRUE replaces Ψ by Psi^{-1} and inverts the output random matrices, such that they are being generated from an Inverse-Wishart $W^{-1}(\Psi, \nu)$ distribution.

Value

Returns an array of Wishart (or Inverse-Wishart) draws of size c(nrow(Psi),ncol(Psi),n).

See Also

rniw()

```
d <- 4 # number of dimensions
nu <- 7 # degrees of freedom
Psi <- crossprod(matrix(rnorm(d^2), d, d)) # scale matrix
n <- 1e4
Sigma <- rwish(n, Psi, nu)
# for any vector a, X = (a' Sigma a) has a const * chi^2 distribution
a <- rnorm(d)
X <- apply(Sigma, 3, function(S) crossprod(a, S %*% a))
const <- c(a %*% Psi %*% a)
hist(X, breaks = 100, freq = FALSE,
    main = parse(text = "\"Histogram of \"*X==a*minute*Sigma*a"),
    xlab = parse(text = "X==a*minute*Sigma*a"))
curve(dchisq(x/const, df = nu)/const,
    from = min(X), to = max(X), col = "red", add = TRUE)
```

Index

* datasets fish, 5 ellipse, 4 ellipse(), 9 fish,5 niche.par.plot, 5niche.plot, 7 niche.plot(), 4, 21 niche.runif,9 niche.size, 10 niche.size(), 9 nicheROVER (nicheROVER-package), 2 nicheROVER-package, 2 niiw.post, 10 niiw.post(), 6, 8, 16, 18, 20 niw.coeffs, 12 niw.coeffs(), *14*, 22 niw.mom, 14 niw.mom(), *12*, *13*, *22* niw.post, 15 niw.post(), 6, 8, 11, 13, 14, 18, 20 overlap, 17 overlap(), 20 overlap.plot, 19 overlap.plot(), 8, 18 overlap.sphere (overlap.unif), 20 overlap.sphere(), 21 overlap.unif, 20 overlap.unif(), 21 rniw, 22 rniw(), *13*, *14*, *16*, *24* rwish,23 rwish(), 11, 22

stats::density(), 6