## Package 'smile'

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Title Spatial Misalignment: Interpolation, Linkage, and Estimation

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Description Provides functions to estimate, predict and interpolate areal data. For estimation and prediction we assume areal data is an average of an underlying continuous spatial process as in Moraga et al. (2017) <doi:10.1016/j.spasta.2017.04.006>, Johnson et al. (2020) <doi:10.1186/s12942-020-00200-w>, and Wilson and Wakefield (2020) <doi:10.1093/biostatistics/kxy041>. The interpolation methodology is (mostly) based on Goodchild and Lam (1980, ISSN:01652273).

License GPL-3

Encoding UTF-8

LazyData true

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SystemRequirements GDAL (>= 2.0.1), GEOS (>= 3.4.0), PROJ (>= 4.8.0)

LinkingTo Rcpp, RcppArmadillo

Imports numDeriv, Rcpp, sf, mvtnorm, stats, parallel, Matrix

**Depends** R (>= 4.0)

URL https://lcgodoy.me/smile/, https://github.com/lcgodoy/smile/

BugReports https://github.com/lcgodoy/smile/issues/

Suggests knitr, rmarkdown, ggplot2, graphics, spelling

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AI

Areal Interpolation

#### Description

This function estimates variables observed at a "source" region into a "target" region. "Source" and "target" regions represent two different ways to divide a city, for example. For more details, see https://lcgodoy.me/smile/articles/sai.html.

#### Usage

```
ai(source, target, vars)
```

ai\_var(source, target, vars, vars\_var, sc\_vars = FALSE, var\_method = "CS")

source	a sf object - source spatial data.
target	a sf object - target spatial data.
vars	a character representing the variables (observed at the source) to be estimated at the target data.
vars_var	a scalar of type character representing the name of the variable in the source dataset that stores the variances of the variable to be estimated at the target data.
sc_vars	boolean indicating whether vars should be scaled by its observed variance (if available).
var_method	a character representing the method to approximate the variance of the AI estimates. Possible values are "CS" (Cauchy-Schwartz) or "MI" (Moran's I).

#### find\_phi

#### Value

the target (of type sf) with estimates of the variables observed at the source data.

find_phi	Find phi parameter for the Exponential spatial auto-correlation func-
	tion

#### Description

Function designed to find the phi parameter such that the correlation between points within a given distance d is at most a given value.

#### Usage

```
find_phi(
    d,
    nu,
    kappa,
    mu2,
    family = "matern",
    range = c(1e-04, 1000),
    cut = 0.05
)
```

#### Arguments

d	maximum distance for spatial dependence equal to cut.
nu	smoothness parameter associated with the Matern cov. function.
kappa	one of the smoothness parameters associated with the Generalized Wendland covariance function
mu2	one of the smoothness parameters associated with the Generalized Wendland covariance function
family	<pre>covariance function family, the options are c("matern","gw", "cs", "spher", "pexp", "gaussian").</pre>
range	Minimum and maximum distance to be considered. The default is range = $c(1e-04, 1000)$ .
cut	desired spatial correlation at a distance d, the default is cut = .05.

#### Value

a numeric value indicating the range parameter such that the spatial correlation between two points at distance d is cut.

fit\_spm

#### Description

Fitting an underlying continuous process to areal data

#### Usage

```
fit_spm(x, ...)
## S3 method for class 'spm'
fit_spm(
 х,
 model,
  theta_st,
 nu = NULL,
  tr = NULL,
  kappa = 1,
 mu2 = 1.5,
  apply_exp = FALSE,
  opt_method = "Nelder-Mead",
  control_opt = list(),
  comp_hess = TRUE,
)
fit_spm2(
  х,
 model,
  nu,
  tr,
  kappa = 1,
 mu2 = 1.5,
  comp_hess = TRUE,
  phi_min,
  phi_max,
 nphi = 10,
  cores = getOption("mc.cores", 1L)
)
```

#### ,

#### Arguments

an object of type spm. Note that, the dimension of theta\_st depends on the 2 factors. 1) the number of variables being analyzed, and 2) if the input is a spm object.

... additional parameters, either passed to stats::optim.

model	a character scalar indicating the family of the covariance function to be used. The options are c("matern", "pexp", "gaussian", "spherical", "gw").
theta_st	a numeric (named) vector containing the initial parameters.
nu	a numeric value indicating either the $\nu$ parameter from the Matern covariance function (controlling the process differentiability), or the "pexp" for the Powered Exponential family. If the model chosen by the user is Matern and nu is not informed, it is automatically set to .5. On the other hand, if the user chooses the Powered Exponential family and do not inform nu, then it is set to 1. In both cases, the covariance function becomes the so called exponential covariance function.
tr	tapper range
kappa	$\kappa \in \{0, \dots, 3\}$ parameter for the GW cov function.
mu2	the smoothness parameter $\mu$ for the GW function.
apply_exp	a logical scalar indicating whether the parameters that cannot assume negative values should be exponentiate or not.
opt_method	a character scalar indicating the optimization algorithm to be used. For details, see stats::optim.
control_opt	a named list containing the control arguments for the optimization algorithm to be used. For details, see stats::optim.
comp_hess	a boolean indicating whether the Hessian matrix should be computed.
phi_min	a numeric scalar representing the minimum $phi$ value to look for.
phi_max	a numeric scalar representing the maximum $phi$ value to look for.
nphi	a numeric scalar indicating the number of values to compute a grid-search over $phi$ .
cores	a integer scalar indicating number of cores to be used. Default is getOp- tion("mc.cores"). No effect on Windows.

#### Details

This function uses the stats::optim function optimization algorithms to find the Maximum Likelihood estimators, and their standard errors, from a model adapted from. The function allows the user to input the control parameters from the stats::optim function through the argument control\_opt, which is a named list. Additionally, the one can input lower and upper boundaries for the optimization problem, as well as the preferred optimization algorithm (as long as it is available for stats::optim). The preferred algorithm is selected by the argument opt\_method. In addition to the control of the optimization, the user can select a covariance function among the following: Matern, Exponential, Powered Exponential, Gaussian, and Spherical. The parameter apply\_exp is a logical scalar such that, if set to TRUE, the exp function is applied to the nonnegative parameters, allowing the optimization algorithm to search for all the parameters over the real numbers.

The model assumes \deqn{Y(\mathbf{s}) = \mu + S(\mathbf{s})} at the
point level. Where \eqn{S ~ GP(0, \sigma^2 C(\lVert \mathbf{s} \mathbf{s}\_2 \rVert; \theta))}. Further, the observed data is supposed
to be \eqn{Y(B) = \lvert B \rvert^{-1} \int\_{B} Y(\mathbf{s}) \,
 \textrm{d} \mathbf{s}}.

a spm\_fit object containing the information about the estimation of the model parameters.

#### Examples

```
data(liv_lsoa) ## loading the LSOA data
msoa_spm <- sf_to_spm(sf_obj = liv_msoa, n_pts = 500,</pre>
                      type = "regular", by_polygon = FALSE,
                      poly_ids = "msoa11cd",
                      var_ids = "leb_est")
## fitting model
theta_st_msoa <- c("phi" = 1) # initial value for the range parameter</pre>
fit_msoa <-
   fit_spm(x = msoa_spm,
           theta_st = theta_st_msoa,
           model = "matern",
           nu = .5,
           apply_exp = TRUE,
           opt_method = "L-BFGS-B",
           control = list(maxit = 500))
AIC(fit_msoa)
summary_spm_fit(fit_msoa, sig = .05)
```

goodness_of_fit	Akaike's (and Bayesian) An Information Criterion for spm_fit ob-
	jects.

#### Description

Akaike's (and Bayesian) An Information Criterion for spm\_fit objects.

#### Usage

```
## S3 method for class 'spm_fit'
AIC(object, ..., k = 2)
```

## S3 method for class 'spm\_fit'
BIC(object, ...)

object	a spm_fit object.
	optionally more fitted model objects.
k	numeric, the <i>penalty</i> per parameter to be used; the default 'k = 2' is the classical AIC. (for compatibility with stats::AIC.

#### liv\_lsoa

#### Value

a numeric scalar corresponding to the goodness of fit measure.

liv\_lsoa

#### Liverpool Lower Super Output Area.

#### Description

A dataset containing containing the LSOA's for Liverpool along with estimates for Index of Multiple Deprivation. Data taken from Johnson et al. 2020

#### Usage

liv\_lsoa

#### Format

A sf data frame with 298 rows and 6 variables:

**Isoa11cd** LSOA code

Isoa11cd LSOA name

male Male population

female Female population

imdscore Index of Multiple Deprivation

area LMSOA area, in  $km^2$ 

#### Details

The data was projected to EPSG 27700 and units changed to km

#### Source

https://ij-healthgeographics.biomedcentral.com/articles/10.1186/s12942-020-00200-w

liv\_msoa

#### Description

A dataset containing containing the MSOA's for Liverpool along with estimates for Life Expectancy at Birth. Data taken from Johnson et al. 2020

#### Usage

liv\_msoa

#### Format

A sf data frame with 61 rows and 4 variables:

msoallcd MSOA code

msoal1cd MSOA name

lev\_est Estimated life expectancy at birth, in years

area MSOA area, in  $km^2$ 

#### Details

The data was projected to EPSG 27700 and units changed to km

#### Source

https://ij-healthgeographics.biomedcentral.com/articles/10.1186/s12942-020-00200-w

nl\_ct

Nova Lima census tracts

#### Description

A dataset containing containing the census tracts for the city of Nova Lima in Minas Gerais - Brazil.

#### Usage

nl\_ct

#### predict\_spm

#### Format

A sf data frame with 113 rows and 14 variables:

cd\_setor unique identifier

hh\_density average household density

var\_hhd variance of the household density

avg\_income average income per household

var\_income variance of the income per household

pop population in the census tract

avg\_age average age of the inhabitants in the census tract

var\_age variance of the variable age in the census tract

prop\_women proportion of women

prop\_elder proportion of people with 55 years of age or older

illit\_rate illiteracy rate

prop\_white proportion of self-declared white people

prop\_black proportion of self-declared black people

prop\_native proportion of self-declared native people

#### Details

The data is project using the SIRGAS 2000.

predict\_spm

Prediction over the same or a different set of regions (or points).

#### Description

Realizes predictions that can be useful when researchers are interested in predict a variable observed in one political division of a city (or state) on another division of the same region.

#### Usage

```
predict_spm(x, ...)
## S3 method for class 'spm_fit'
predict_spm(x, .aggregate = TRUE, ...)
## S3 method for class 'sf'
predict_spm(x, spm_obj, n_pts, type, outer_poly = NULL, id_var, ...)
```

#### Arguments

x	a sf object such that its geometries are either points or polygons.
	additional parameters
.aggregate	logical. Should the predictions be aggregated? In case the input is only a "fit" object, the aggregation is made over the polygons on which the original data was observed. In case the input x is composed by sf POLYGONS, the aggregation is made over this new partition of the study region.
spm_obj	an object of either class spm_fit or mspm_fit
n_pts	a numeric scalar standing for number of points to form a grid over the whole region to make the predictions
type	character type of grid to be generated. See st_sample in the package sf.
outer_poly	(object) sf geometry storing the "outer map" we want to compute the predictions in.
id_var	if x is a set of POLYGONS (areal data) instead of a set of points, the id_var is the name (or index) of the unique identifier associated to each polygon.

#### Value

a list of size 4 belonging to the class spm\_pred. This list contains the predicted values and the mean and covariance matrix associated with the conditional distribution used to compute the predictions.

#### Examples

```
data(liv_lsoa) ## loading the LSOA data
data(liv_msoa) ## loading the MSOA data
msoa_spm <- sf_to_spm(sf_obj = liv_msoa, n_pts = 500,</pre>
                      type = "regular", by_polygon = FALSE,
                      poly_ids = "msoallcd",
                      var_ids = "leb_est")
## fitting model
theta_st_msoa <- c("phi" = 1) # initial value for the range parameter
fit_msoa <-
   fit_spm(x = msoa_spm,
           theta_st = theta_st_msoa,
           model = "matern",
           nu = .5,
           apply_exp = TRUE,
           opt_method = "L-BFGS-B",
           control = list(maxit = 500))
```

pred\_lsoa <- predict\_spm(x = liv\_lsoa, spm\_obj = fit\_msoa, id\_var = "lsoa11cd")</pre>

sf\_to\_spm

#### Description

Transforming a sf into a spm object (Internal use)

#### Usage

```
single_sf_to_spm(
  sf_obj,
  n_pts,
  type = "regular",
  by_polygon = FALSE,
 poly_ids = NULL,
 var_ids = NULL,
  trunc_d = NULL
)
sf_to_spm(
  sf_obj,
 n_pts,
  type = "regular",
 by_polygon = FALSE,
 poly_ids = NULL,
 var_ids = NULL,
  trunc_d = NULL
)
```

sf_obj	a sf object s.t. its geometries are polygons.
n_pts	a numeric scalar representing the number of points to create a grid in the study region on which the polygons in sf_obj is observed. Alternatively, it can be a vector of the same length as nrow(sf_obj). In this case, it generates the given number of points for each polygon in sf_obj.
type	a character indicating the type of grid to be generated. The options are c("random", "regular", "hexagonal"). For more details, see st_sample in the sf package.
by_polygon	a logical indicating whether we should generate n_pts by polygon or for the n_pts for the whole study region.
poly_ids	a character vector informing the name of the variable in sf_obj that represents the polygons unique identifiers. In case this is not informed, we assume the id of the polygons are given by their row numbers.
var_ids	a scalar or vector of type character indicating the (numerical) variables that are going to be analyzed.

trunc\_d truncation distance for grid points. Consider using half of the maximum distance between polygons

#### Value

a named list of size 6 belonging to the class spm. This list stores all the objects necessary to fit models using the fit\_spm.

#### Examples

data(liv\_lsoa) # loading the LSOA data

```
msoa_spm <- sf_to_spm(sf_obj = liv_msoa, n_pts = 1000,
    type = "regular", by_polygon = FALSE,
    poly_ids = "msoa11cd",
    var_ids = "leb_est")
```

```
smile
```

smile: Spatial MIsaLignment Estimation

#### Description

smile: Spatial MIsaLignment Estimation

|--|

#### Description

Provides a data.frame with point estimates and confidence intervals for the parameters of the model fitted using the spm\_fit function.

#### Usage

summary\_spm\_fit(x, sig = 0.05)

#### Arguments

х	a spm_fit object.
sig	a real number between 0 and 1 indicating significance level to be used to com-
	pute the confidence intervals for the parameter estimates.

#### Value

a data.frame summarizing the parameters estimated by the fit\_spm function.

#### vdl

#### Description

Reminder, have to create an example. This will be exported after we submit the paper for publication.

### Usage

vdl(coords\_sf, areal\_sf, vars, buff)

#### Arguments

coords_sf	sf POINT target dataset.
areal_sf	sf POLYGON source dataset.
vars	a character representing the variables (observed at the source - polygon) to be estimated at the target data.
buff	scalar numeric. Mostly for internal use.

#### Value

a sf object for the coords\_sf spatial data set.

vdl_var Voronoi Data Linkage - Single variable and variance	
---	--

#### Description

Reminder, have to create an example. This will be exported after we submit the paper for publication.

#### Usage

```
vdl_var(coords_sf, areal_sf, res_var, variance, var_method = "CS", buff)
```

coords_sf	sf POINT target dataset.
areal_sf	sf POLYGON source dataset.
res_var	a character - the name of the variable in the <code>areal_sf</code> to be estimated in the <code>coords_sf</code> .
variance	a character - the name of the variable variance in the areal_sf to be estimated in the coords_sf.
var_method	a character representing the method to approximate the variance of the AI estimates. Possible values are "CS" (Cauchy-Schwartz) or "MI" (Moran's I).
buff	scalar numeric. Mostly for internal use.

## Value

a sf object, containing the id\_coords variable and the list\_vars for the coords\_sf spatial data set.

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